

Lecture 1: Overview and the Night Sky at a Glance

...

Learning Objectives and Overview

By the end of this course, students will be able to:

...identify major stars and constellations in the night sky, recount the life-cycle of a star from the Main Sequence to supernova, and distinguish between White Dwarfs, Neutron Stars, and Black Holes.

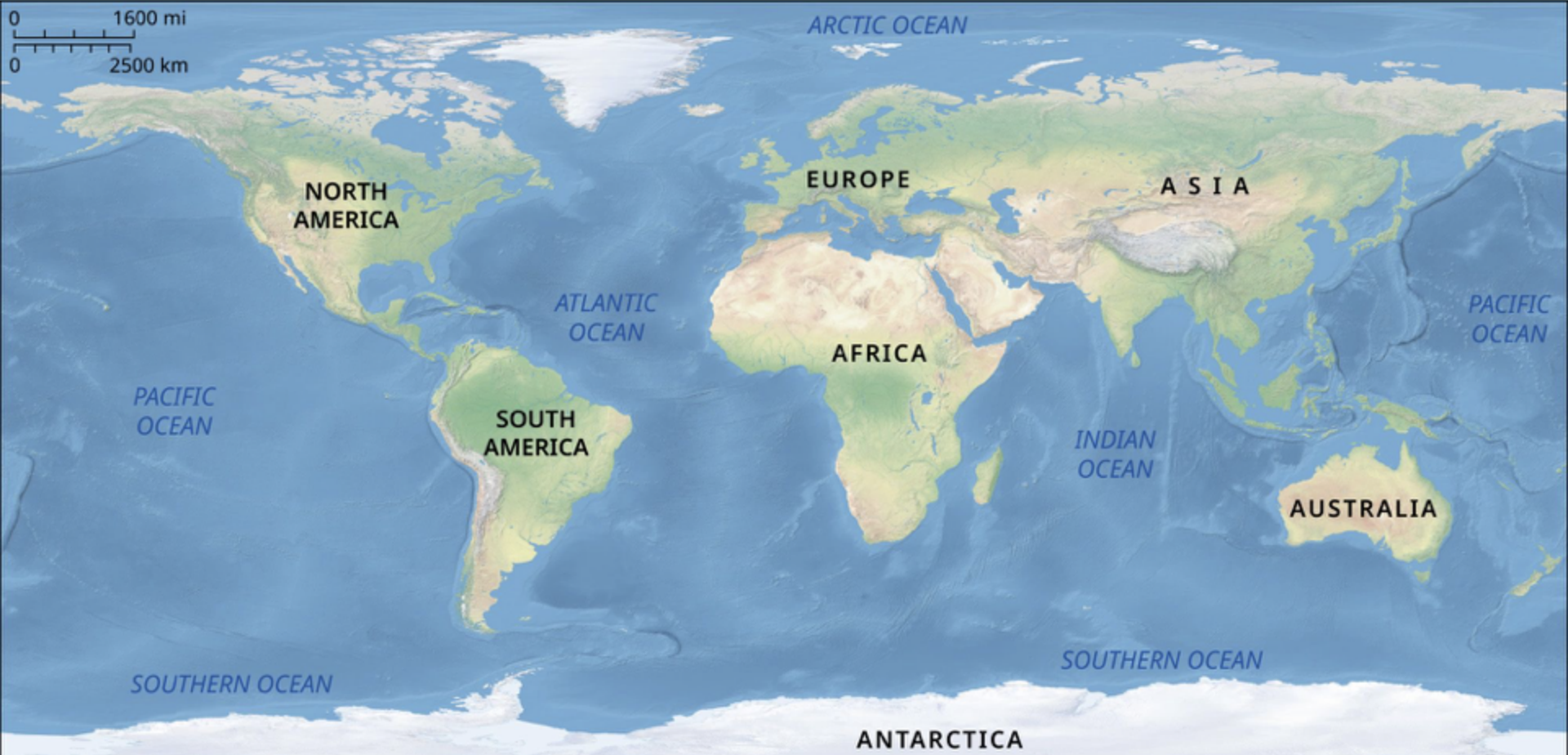
...describe the basic components of an optical telescope, explain the major differences between optical, infrared, and UV astronomy, describe why X-ray and gamma ray telescopes operate differently from OIR and UV telescopes.

...describe the basic components of a radio antenna, explain how radio interferometers work, and list the astrophysical sources of radio waves.

...describe the components of a galaxy (disk, bulge, ISM, halo, CGM), define cosmology, how it is studied (redshift, CMB, 21 cm cosmology, simulations, FRBs), explain how distance, redshift, and time are related within general relativity, and understand how the presence of dark matter and dark energy affect our picture of the Universe.

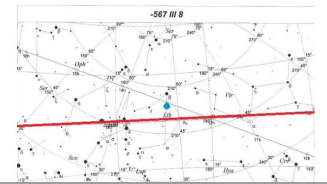
...list some of the major questions in astronomy today and refer to resources to continue exploring astronomy within and around Pasadena.

0 1600 mi
0 2500 km



Aristotle's "Heavenly Spheres" model (c. 384-322 B.C.E.)

Night of the 8th, first part of the night, the Moon stood 2 1/2 cubits below β Librae.

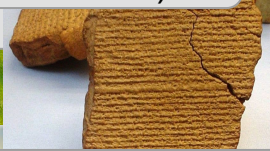
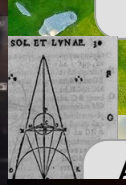


Babylonian Astronomical Diaries (c. 652-262 B.C.E.)

Antikythera Mechanism (c. 150-100 B.C.E.)



Nebra Sky Disc (c. 1600 B.C.E.)



Aristarchus Uses Lunar Eclipse to Measure Moon's Size (c. 300-200 B.C.E.)

Nabta Playa (9000-3500 B.C.E.)



Astrolabe Developed in Greece and spread to Western World by Arab Astronomers (c. 600 C.E.)

ATLANTIC OCEAN

AFRICA

SOUTH AMERICA

INDIAN OCEAN

Mayan Calendar: the
Haab, *Tzolk'in*, and
the Long Count)
(c. 500 B.C.E)



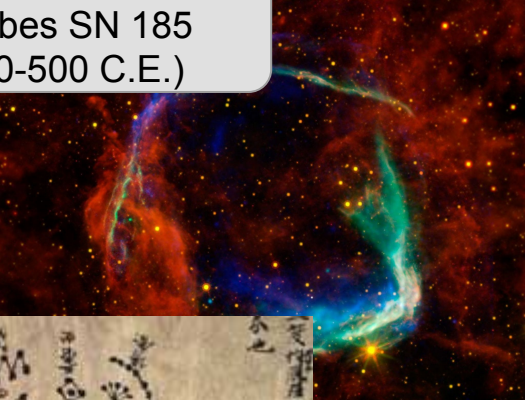
Dresden Codex
(c. 1000-1100 C.E.)



PACIFIC
OCEAN

AMERICA

The Book of Later Han
Describes SN 185
(c. 400-500 C.E.)



伯升次仲故南陽蔡陽人南陽郡今鄧州縣也蔡
字文叔焉注世祖謚法能紹前注曰秀之子曰茂
陽縣西南
定王發長沙郡今潭州縣也發生春陵節侯買春陵
本屬零陵冷道縣在今永州唐興縣北元帝時徙南
陽仍號春陵故城今在隨州棗陽縣東事具宗室四

光武皇帝
九世祖諡法能紹前
注曰秀之子曰茂



Chinese Star Maps (c. 1200
B.C.E.; copies from Tang Dynasty
c. 800-900 C.E.)

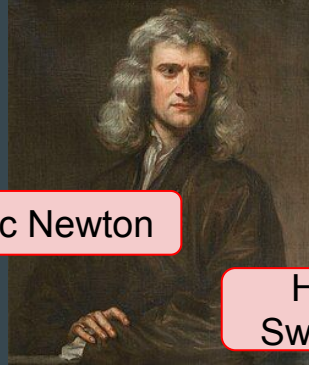
EUROPE

AFRICA

PACIFIC OCEAN

INDIAN OCEAN

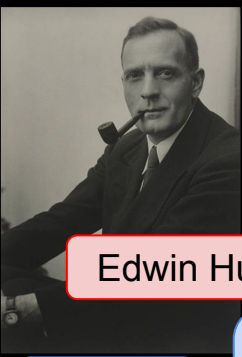
Milestones in Modern Astronomy



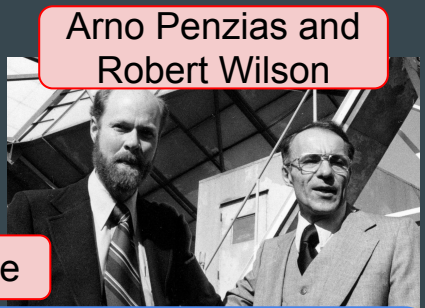
Isaac Newton



Henrietta Swan Leavitt



Edwin Hubble



Arno Penzias and Robert Wilson

1608 – Invention of the Telescope

1687 – Newton's Laws of Gravity

1918 - Galaxy Center

1920s - Hubble's Law of Universal Expansion & Einstein's Theory of General Relativity

1543 – Heliocentric Solar System

1609 – Kepler's Laws of Elliptical Motion

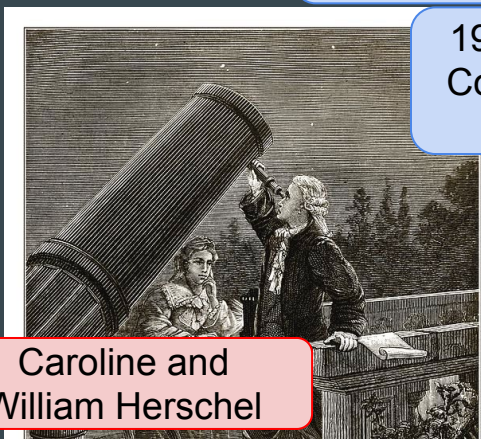
1800 - Discovery of IR Radiation

1964 - Cosmic Microwave Background

1908 - Distance/Period Correlation for Cepheid Variable Stars



Galileo Galilei

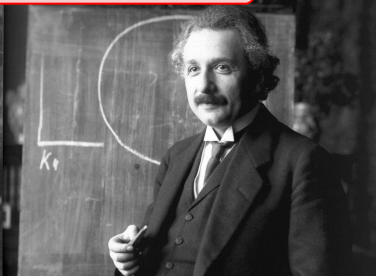


Caroline and William Herschel



Alexander Friedmann

Albert Einstein



Distance Scales

AU=Astronomical Unit

ly=light-year

pc=parsec

8 kpc = 1.6 billion AU

2.5 million ly = 765 kpc

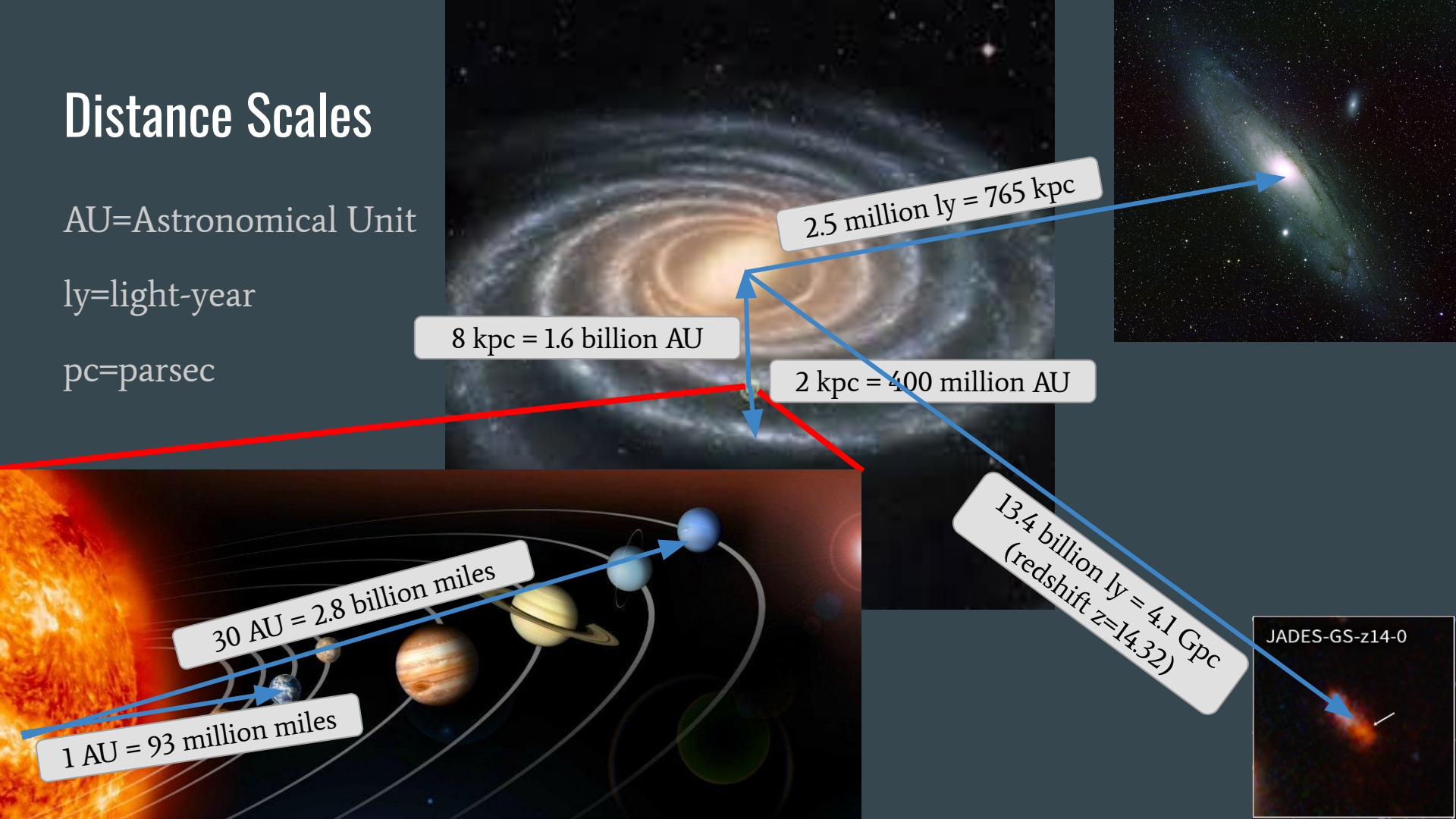
2 kpc = 400 million AU

13.4 billion ly = 4.1 Gpc
(redshift $z=14.32$)

30 AU = 2.8 billion miles

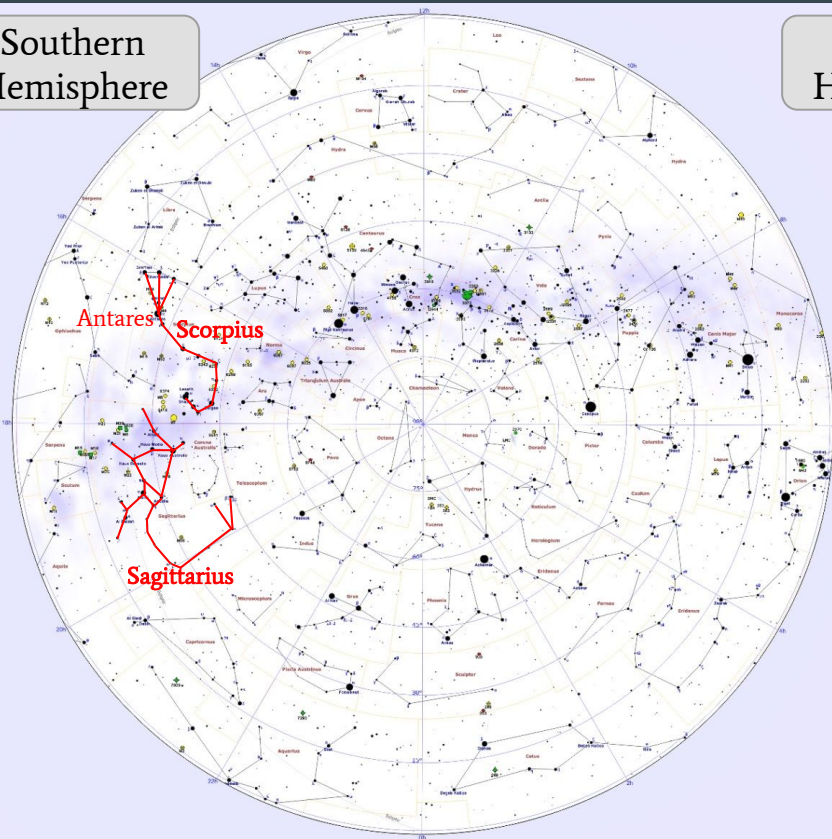
1 AU = 93 million miles

JADES-GS-z14-0

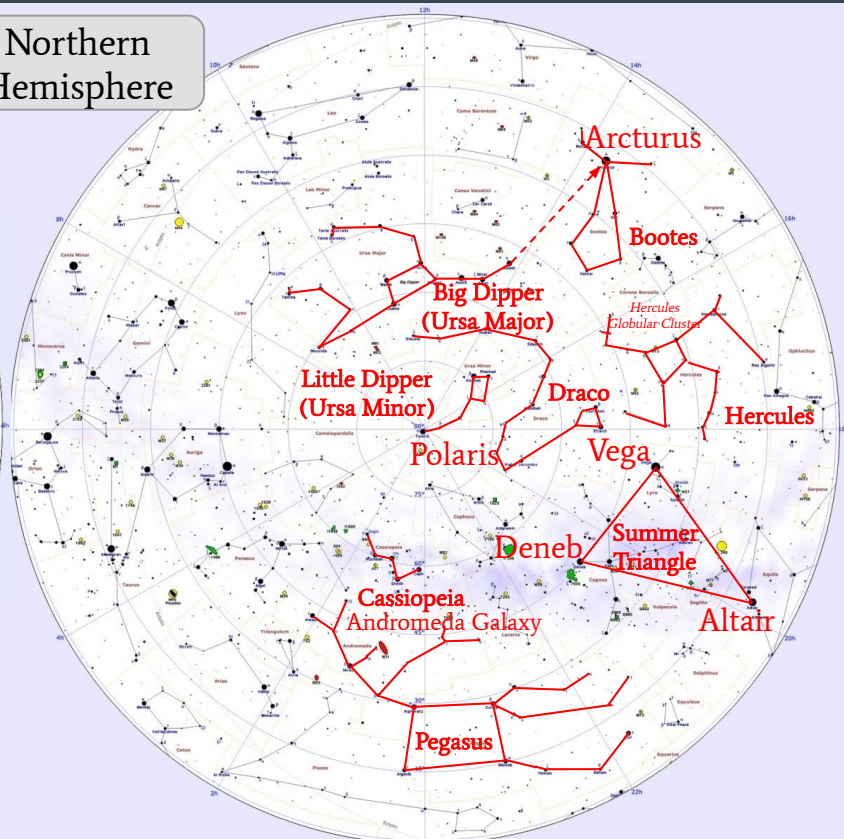


Navigating with Constellations and Asterisms: **Summer in Pasadena**

Southern Hemisphere

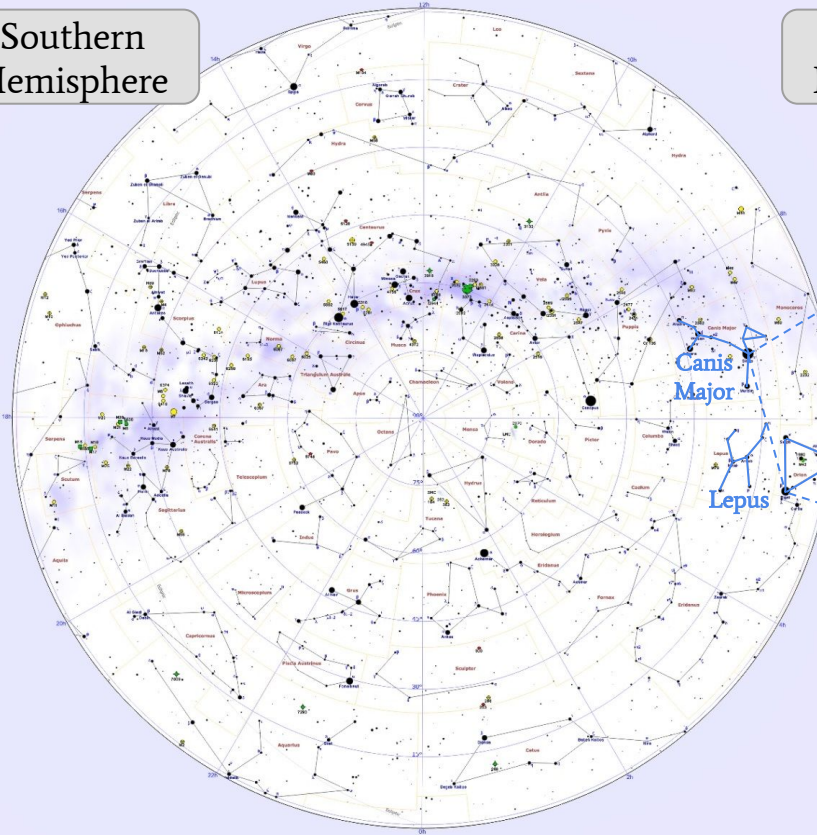


Northern Hemisphere

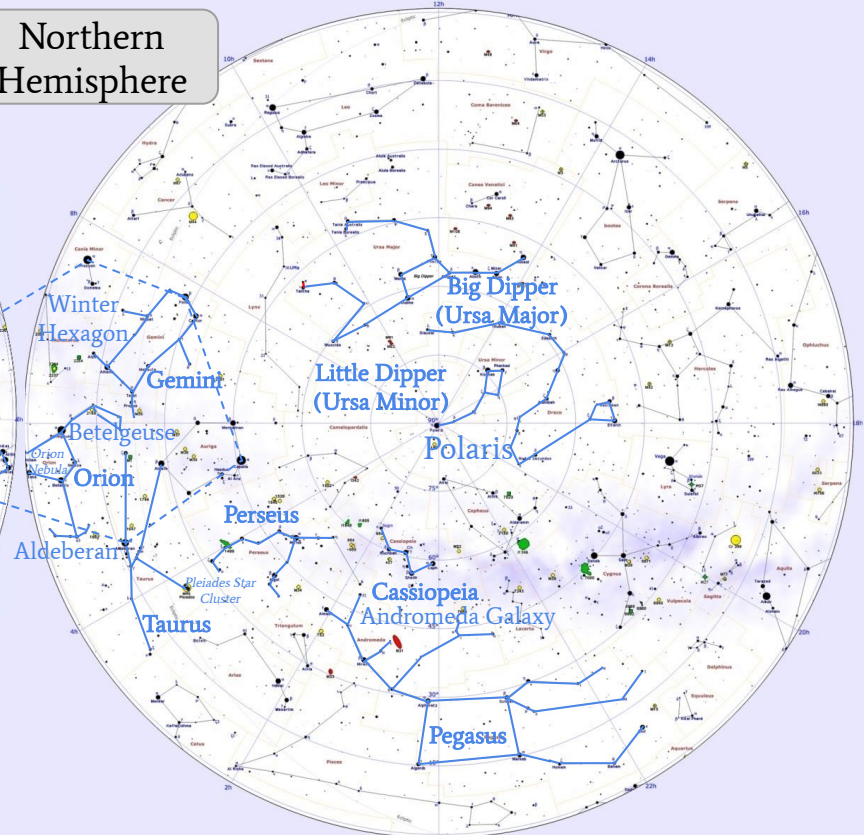


Navigating with Constellations and Asterisms: *Winter in Pasadena*

Southern Hemisphere



Northern Hemisphere



Celestial Coordinates

Sidereal Time: time measured relative to field stars instead of the Sun

1 Sidereal Day = 23 hours 56 minutes

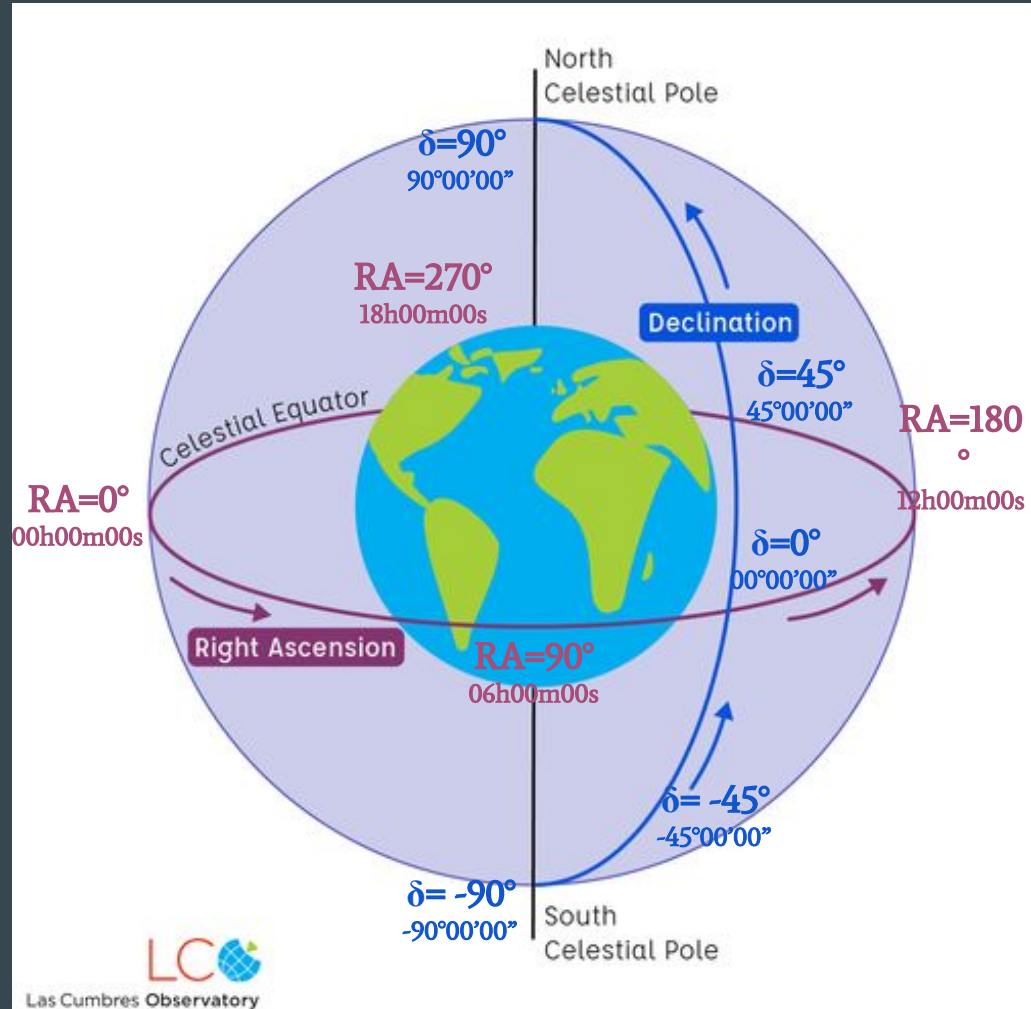
Centered on Earth and aligned with Equator and Poles:

- **Right Ascension (RA;** Celestial Longitude)
- **Declination** (Celestial Latitude)

RA can be specified in **degrees (0 - 360)** or **hours (0 - 24)**

$$\text{RA}[\text{degrees}] = 15 \times \text{RA}[\text{hours}]$$

Local Sidereal Time (LST): current RA overhead at the observer's location



Celestial Coordinates

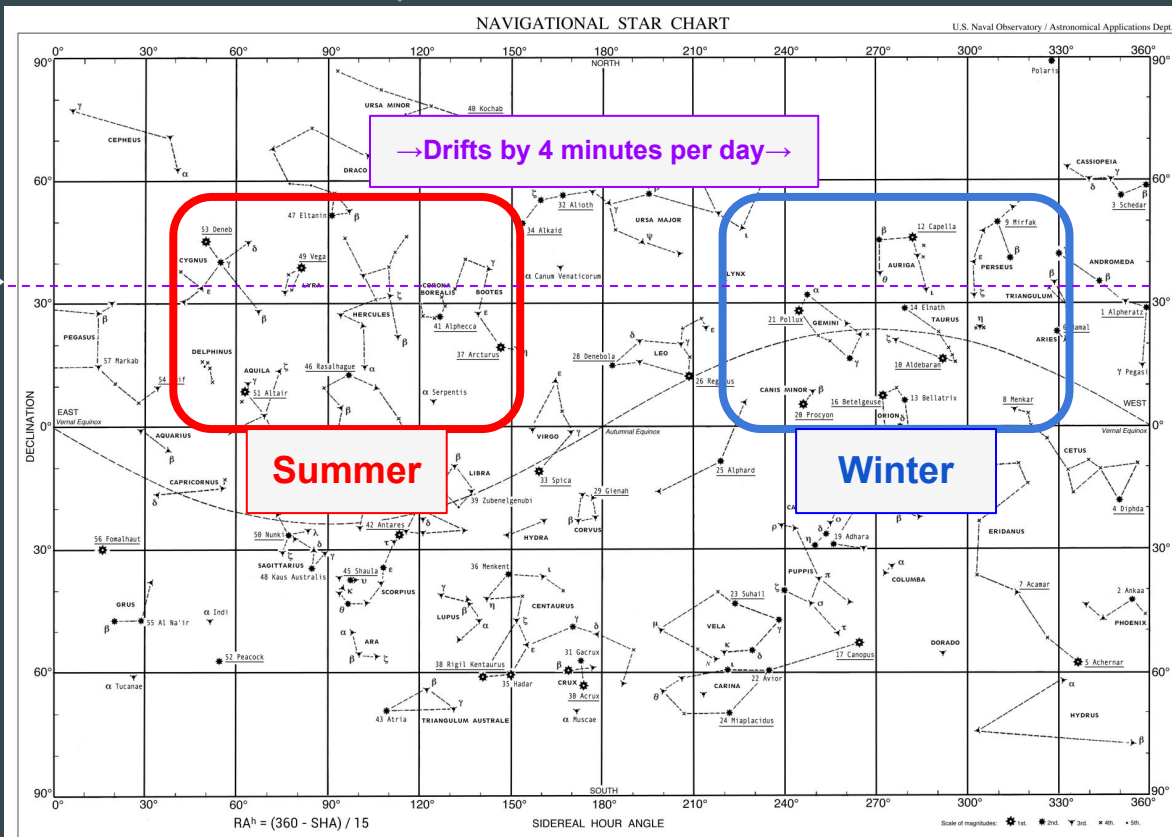
Note: PST = UTC + 8 hours

Pasadena is at latitude 34.15°

Lookup LST here:

<https://aa.usno.navy.mil/data/siderealtime>

Pasadena is at longitude 118.1°



Thank You

THE NUMBER OF EACH DAY OF THE YEAR

Day	Jan.	Feb.	Mar.	Apr.	May	Jun.	Jul.	Aug.	Sept.	Oct.	Nov.	Dec.
1	1	31	61	91	121	151	181	211	241	271	301	331
2	2	32	62	92	122	152	182	212	242	272	302	332
3	3	33	63	93	123	153	183	213	243	273	303	333
4	4	34	64	94	124	154	184	214	244	274	304	334
5	5	35	65	95	125	155	185	215	245	275	305	335
6	6	36	66	96	126	156	186	216	246	276	306	336
7	7	37	67	97	127	157	187	217	247	277	307	337
8	8	38	68	98	128	158	188	218	248	278	308	338
9	9	39	69	99	129	159	189	219	249	279	309	339
10	10	40	70	100	130	160	190	220	250	280	310	340
11	11	41	71	101	131	161	191	221	251	281	311	341
12	12	42	72	102	132	162	192	222	252	282	312	342
13	13	43	73	103	133	163	193	223	253	283	313	343
14	14	44	74	104	134	164	194	224	254	284	314	344
15	15	45	75	105	135	165	195	225	255	285	315	345
16	16	46	76	106	136	166	196	226	256	286	316	346
17	17	47	77	107	137	167	197	227	257	287	317	347
18	18	48	78	108	138	168	198	228	258	288	318	348
19	19	49	79	109	139	169	199	229	259	289	319	349
20	20	50	80	110	140	170	200	230	260	290	320	350
21	21	51	81	111	141	171	201	231	261	291	321	351
22	22	52	82	112	142	172	202	232	262	292	322	352
23	23	53	83	113	143	173	203	233	263	293	323	353
24	24	54	84	114	144	174	204	234	264	294	324	354
25	25	55	85	115	145	175	205	235	265	295	325	355
26	26	56	86	116	146	176	206	236	266	296	326	356
27	27	57	87	117	147	177	207	237	267	297	327	357
28	28	58	88	118	148	178	208	238	268	298	328	358
29	29	59	89	119	149	179	209	239	269	299	329	359
30	30	60	90	120	150	180	210	240	270	300	330	360
31	31	61	91	121	151	181	211	241	271	301	331	361
32	32	62	92	122	152	182	212	242	272	302	332	362
33	33	63	93	123	153	183	213	243	273	303	333	363
34	34	64	94	124	154	184	214	244	274	304	334	364
35	35	65	95	125	155	185	215	245	275	305	335	365
36	36	66	96	126	156	186	216	246	276	306	336	366
37	37	67	97	127	157	187	217	247	277	307	337	367
38	38	68	98	128	158	188	218	248	278	308	338	368
39	39	69	99	129	159	189	219	249	279	309	339	369
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41	41	71	101	131	161	191	221	251	281	311	341	371
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44	44	74	104	134	164	194	224	254	284	314	344	374
45	45	75	105	135	165	195	225	255	285	315	345	375
46	46	76	106	136	166	196	226	256	286	316	346	376
47	47	77	107	137	167	197	227	257	287	317	347	377
48	48	78	108	138	168	198	228	258	288	318	348	378
49	49	79	109	139	169	199	229	259	289	319	349	379
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55	55	85	115	145	175	205	235	265	295	325	355	385
56	56	86	116	146	176	206	236	266	296	326	356	386
57	57	87	117	147	177	207	237	267	297	327	357	387
58	58	88	118	148	178	208	238	268	298	328	358	388
59	59	89	119	149	179	209	239	269	299	329	359	389
60	60	90	120	150	180	210	240	270	300	330	360	390
61	61	91	121	151	181	211	241	271	301	331	361	391
62	62	92	122	152	182	212	242	272	302	332	362	392
63	63	93	123	153	183	213	243	273	303	333	363	393
64	64	94	124	154	184	214	244	274	304	334	364	394
65	65	95	125	155	185	215	245	275	305	335	365	395
66	66	96	126	156	186	216	246	276	306	336	366	396
67	67	97	127	157	187	217	247	277	307	337	367	397
68	68	98	128	158	188	218	248	278	308	338	368	398
69	69	99	129	159	189	219	249	279	309	339	369	399
70	70	100	130	160	190	220	250	280	310	340	370	400

THE NUMBER OF EACH DAY OF THE YEAR FOR LEAP YEAR

Day	Jan.	Feb.	Mar.	Apr.	May	Jun.	Jul.	Aug.	Sept.	Oct.	Nov.	Dec.
1	1	31	61	91	121	151	181	211	241	271	301	331
2	2	32	62	92	122	152	182	212	242	272	302	332
3	3	33	63	93	123	153	183	213	243	273	303	333
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23	23	53	83	113	143	173	203	233	263	293	323	353
24	24	54	84	114	144	174	204	234	264	294	324	354
25	25	55	85	115	145	175	205	235	265	295		

At-Home Astronomy: Online Star Maps

Stellarium: <https://stellarium-web.org/>

Make Your Own Star Wheel (*Sky & Telescope*):
<https://stellarium-web.org/>

Aladin: <https://aladin.cds.unistra.fr/AladinLite/>

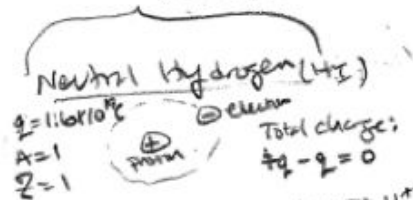
Pan-Starrs (Northern Sky Survey):
<https://pslimages.stsci.edu/cgi-bin/pslcutouts>

SkyMapper (Southern Sky Survey):
<https://skymapper.anu.edu.au/image-cutout/>

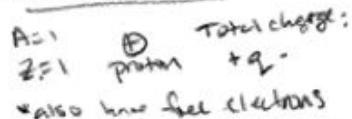


Interstellar Medium (ISM) - gas & dust between stars in the Galaxy

~70% of ISM is Hydrogen



Ionized Hydrogen (H^{II} , H^+)



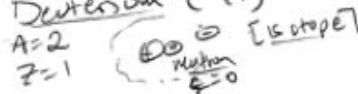
$N_{SM} \sim 1$ loop particles per cubic cm (cm^{-3})

Molecular Hydrogen (H_2)



molecular clouds

Deuterium (2H)



~28% of ISM is Helium

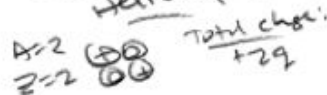
Neutral Helium (He)



Singly-ionized Helium (He^+)



Doubly-ionized Helium (He^{2+})

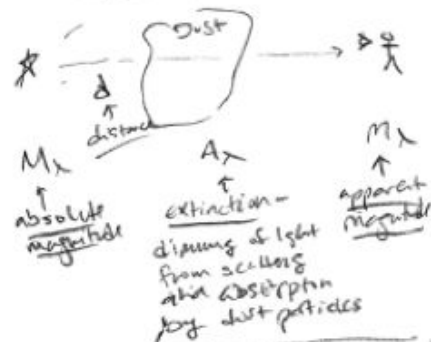


~1.5% of ISM are Metals - any element with $Z > 2$ (heavier than Helium)

~0.5% of ISM is Dust

- silicates, carbon molecules, hydrocarbons, graphite

↳ Carbon (C): $A=6$



$$M_x = M_x + 5 \log \left(\frac{d}{10} \right) - 5 + A_x$$

1.21

Energy - "ability to move or change matter in some way"

- energy is always conserved: $E_{\text{initial}} = E_{\text{final}}$

Kinetic Energy

$m = \text{mass}$
 $v = \text{velocity}$

$$E_{\text{kinetic}} = \frac{1}{2} m |\vec{v}|^2 > 0$$

Boltzmann Dist.
 $f(v) = \left(\frac{m}{2\pi kT}\right)^{3/2} \exp\left(-\frac{mv^2}{2kT}\right)$

Thermal Energy

Ideal gas law: $PV = NkT$



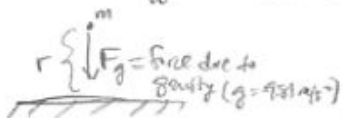
$N = \# \text{ particles}$
 $k = 1.38 \times 10^{-23} \text{ J/K}$
 $T = \text{temperature (K)}$

$$E_{\text{thermal}} = \frac{3}{2} NkT > 0$$



Potential Energy - stored energy that can change to another form

Gravitational Potential Energy



$$E_{\text{grav}} = mgr < 0 \quad \rho_0 \text{ near } R$$

Newton's Gravitational Constant

$$G = 6.67 \times 10^{-11} \frac{\text{m}^3}{\text{kg} \cdot \text{s}^2}$$

For 2 masses M and m separated by distance r :

$$E_{\text{grav}} = -\frac{GMm}{r} < 0$$

For extended object (radius R):

$$E_{\text{grav}} = -\frac{3}{5} \frac{GM^2}{R} < 0$$

Free-fall time scale $t_{\text{ff}} = \sqrt{\frac{3\pi}{32G\rho_0}}$

Total Energy

$$E_{\text{tot}} = E_{\text{kinetic}} + E_{\text{grav}}$$

$< 0 \rightarrow \text{bound}$
 $> 0 \rightarrow \text{unbound}$

Virial Theorem: $2E_{\text{kinetic}} + E_{\text{grav}} \approx 0$ (equilibrium)

How does a cloud of gas collapse into a star?



initial density: $\rho_0 = \frac{M}{\frac{4}{3}\pi R^3}$

$$R = \left(\frac{M}{\frac{4}{3}\pi \rho_0}\right)^{1/3}$$

System will collapse if $2E_{\text{kinetic}} + E_{\text{grav}} < 0$

$$2\left(\frac{3MkT}{4\pi}\right) < \frac{3GM^2}{R}$$

$$\frac{1 \cdot R}{G} \left(\frac{kT}{m}\right) < M \Rightarrow \frac{10}{9} \left(\frac{4}{3}\pi\right)^{1/3} \left(\frac{kT}{Gm}\right) < M^{2/3}$$

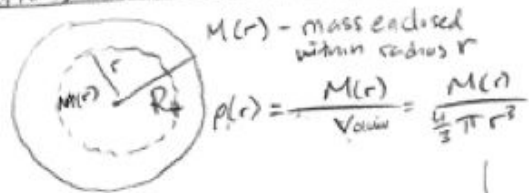
Jean's criteria

$$M_J \equiv \left(\frac{1}{\frac{4}{3}\pi}\right) \left(\frac{10kT}{9Gm}\right)^{3/2} < M$$

$$R_J \equiv \sqrt{\frac{15kT}{4\pi G \rho_0}} < R$$

1.3

Equations of Stellar Structure:



① Hydrostatic Equilibrium
balance of gravity and pressure:

$$\frac{dP}{dr} = -\frac{GM(r)\rho}{r^2} \quad \left(\begin{array}{l} \text{star is only supported} \\ \text{if pressure is higher} \\ \text{at center of the star} \end{array} \right)$$

② Mass Conservation

$$\frac{dM}{dr} = 4\pi r^2 \rho(r)$$

for constant density:

$$\frac{dM}{dr} = 4\pi r^2 \rho$$

$$\rho dM = M = \int_0^{R_*} 4\pi r^2 \rho dr$$

$$M = \frac{4}{3}\pi R_*^3 \rho$$

③ Pressure Equation of state - tells us how gas is composed and behaves

- Ideal gas - gas w/ negligible volume, similar sized particles & no interaction between particles.

$$P = \frac{N}{V} kT = \frac{\rho kT}{\mu m_H} \quad \text{velocity}$$

for any other gas: $P = \frac{1}{3} \int_0^\infty n p v dp$

n = density \rightarrow k = momentum

radiation pressure - pressure exerted by photons in thermal equilibrium

$$P = \frac{1}{3} a T^4 \quad \text{where } a = 7.56 \times 10^{-16} \text{ J/m}^3 \text{K}^4$$

⑤ Radiative Transport - describes how energy is transported within the star

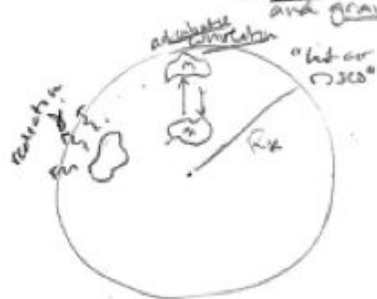
$$\frac{dT}{dr} = \left\{ \begin{array}{l} \frac{3}{4ac} \frac{\kappa_p}{T^3} \frac{L}{4\pi r^2} \quad \text{radiation} \\ \left(\frac{1}{\beta} - 1\right) \frac{4M}{k} \frac{GM}{r^2} \quad \text{adiabatic convection} \end{array} \right.$$

④ Luminosity Gradient

- luminosity - power (energy produced per unit time)

$$\frac{dL}{dr} = 4\pi r^2 \rho(r) \epsilon(r)$$

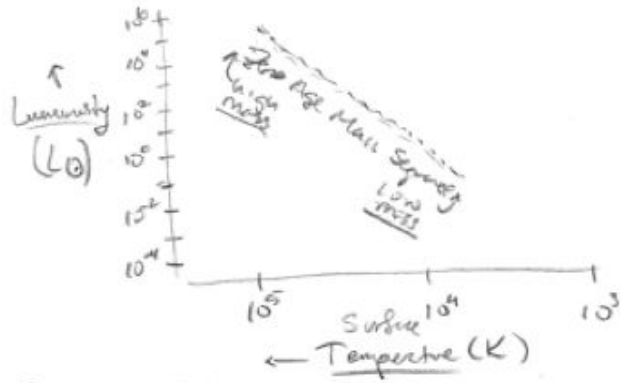
total power released per unit area by nuclear reactions and gravity



1.4 |

Stellar Evolution

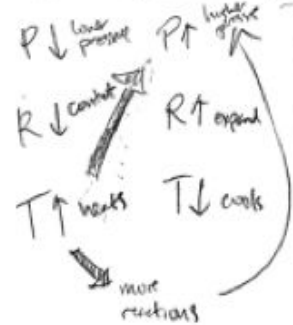
The Hertzsprung Russell Diagram



Feedback Stability

$M \uparrow = \frac{\text{net mass}}{\text{molecular weight}}$

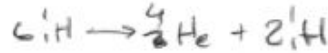
$M=1$ for Hydrogen
 $M=2$ for Helium



radiated energy
Energy $\approx 25 \text{ MeV}$
(γ, ν, e^+, p^+)

$PV = NkT$

Main Sequence - hydrogen being to fuse into helium:

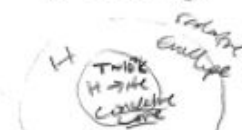


Low Mass Stars
(0.3 - 1.2 M_{\odot})



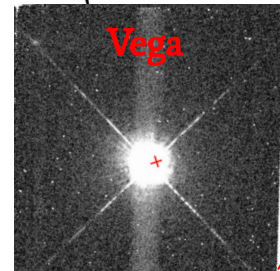
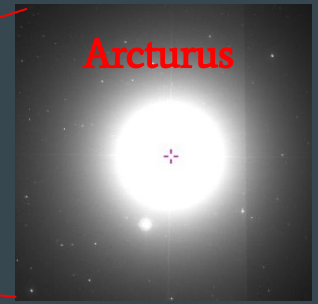
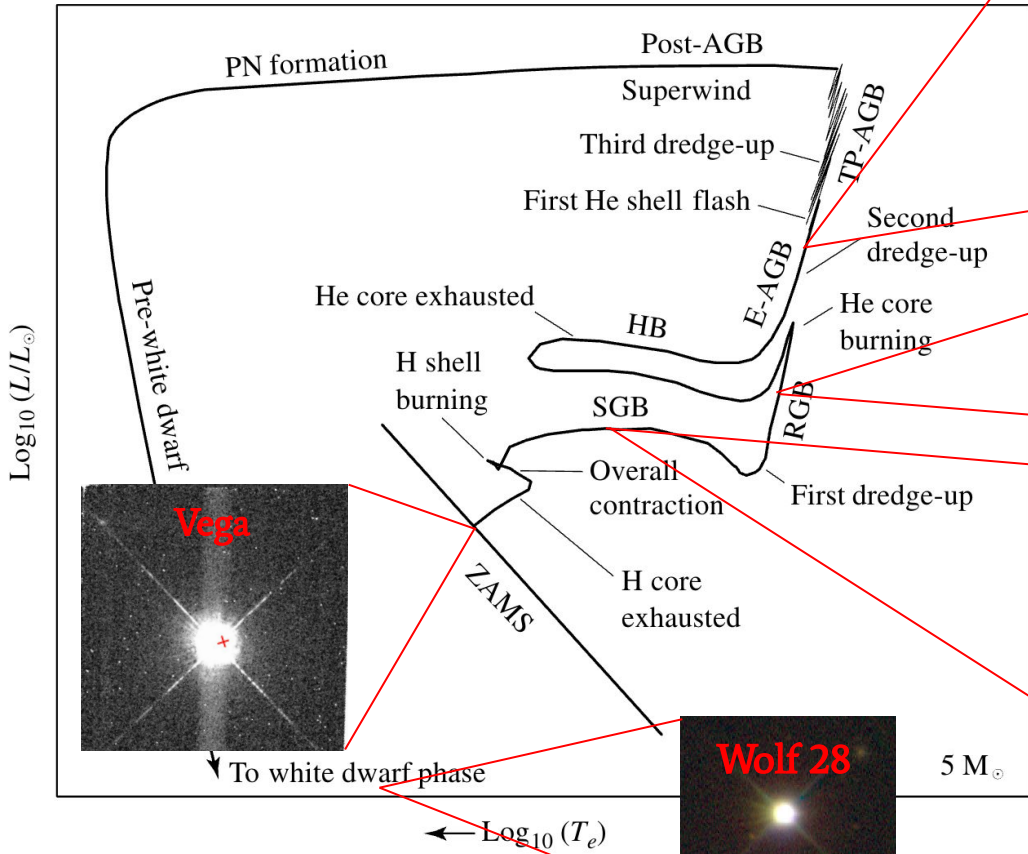
proton-proton chain

High Mass Stars
($> 1.2 M_{\odot}$)



CNO cycle





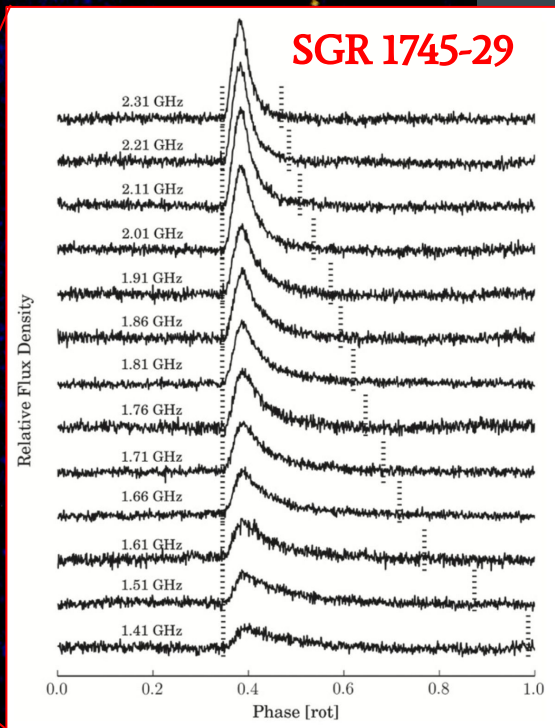
Black Hole

Sagittarius A*

Radio

Neutron Star

SGR 1745-29



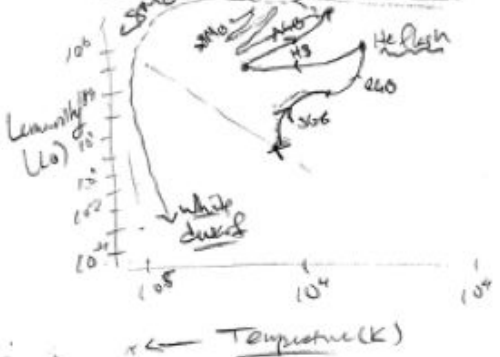
Radio

X-ray

1.5

Stellar Evolution

The Hertzsprung Russell Diagram



Sub-Giant Branch - after hydrogen finished burning, needs to get to T and P to begin He fusion

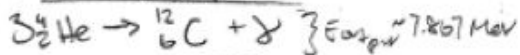
Red Giant Branch
↓
Convective Mixing
↳ LT faster



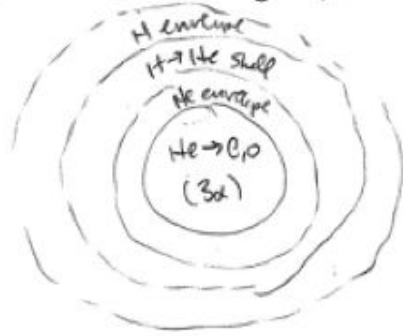
core: contracts (R↓)
- heats (T↑)
releases gravitational energy + radiation

shell - continues hydrogen burning, deposits mass into core

Horizontal Branch - Helium burning, fusing to Carbon
↳ triple alpha process



envelope - Reddening process from core (R↑)
Luminosity increase (L↑)
expands (R↑) & T & P cools (T↓, P↓)



Asymptotic Giant Branch

Outer layers expand away
↓
core contracts
↓
β⁻ decay energy production
white dwarf star



Continues burning cycle until core
↓
helium fusion
core collapses → Helium shell flash

Same as Sub-giant/Red Giant

1.6)

White Dwarf Stars (for $M_* < 8M_\odot$)

- central star exposed gradually as envelope expands ($T_{eff} \uparrow \rightarrow$ blue)



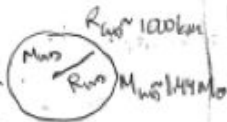
supported by e^- degeneracy pressure + quantum mechanical pressure

↳ Pauli exclusion principle - 2 electrons can't occupy the same energy state

↳ forces free electrons in core into higher energy states \rightarrow higher velocities \rightarrow "pressure"

$$P_e \propto \rho^{5/3}$$

↳ Chandrasekhar mass limit - maximum mass before e^- degeneracy pressure fails $\Rightarrow M_{WD} \sim 1.44M_\odot$



- for $M_* < 4M_\odot \rightarrow$ C, O white dwarf
- $4M_\odot < M_* < 8M_\odot \rightarrow$ O, Ne, Mg white dwarf

- mass loss accelerates (expanding envelope \rightarrow wind)

$$\dot{M} = dM/dt = 10^{-4} M_\odot/\text{yr}$$

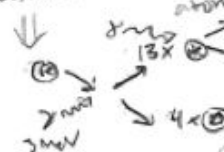
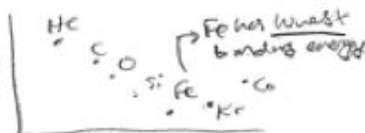
Neutron Stars & Black Holes (for $M_* > 8M_\odot$)

(Supergiant)

- continues burn until fuses iron (Fe) in core

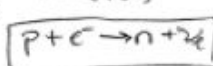
- photodissociation binding energy

↳ $T > 10^{10} K$
 ↳ overcome pressure required to break down Fe atoms



energy released to break down Fe atoms into $13 \times \alpha$ + $4 \times p$

neutronization
 ↳ protons capture e^- and decay to neutrons



- core collapse

↳ outer layers infall under gravity

↳ "bounced" off central star

$M_{core} > 1.44M_\odot$

↳ collapses further into Black Hole

$M_{core} \leq 1.44M_\odot$

↳ neutron star



↳ core supported by neutron degeneracy pressure

(since neutrons into high energy states)

$$P_n \propto \rho^{4/3}$$

↳ Chandrasekhar limit =

$$M_{Ch} = 1.4M_\odot$$

Think-Pair-Share

How would you classify a new star given its apparent magnitude?

Think-Pair-Share

How would you classify a new star given its apparent magnitude?

How might a binary companion star impact a star's evolution?

1.7 | BINARY STARS

	<u>Single</u>	<u>Binary</u>	<u>Triplet</u>
Sun-like stars	60%	30%	10%
O-type stars	6%	21%	73%

Most high mass stars are in orbit with other stars

Types of Binaries:

- Cataclysmic variables (CVs)



accretion disk

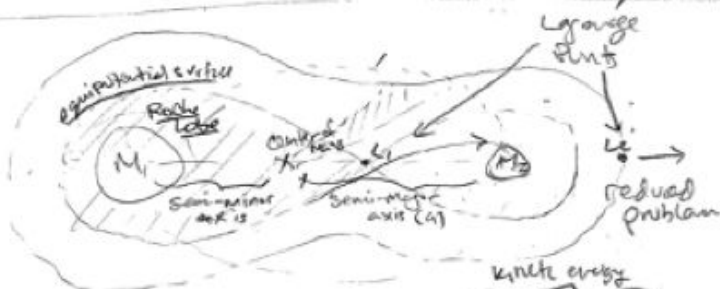
↳ Type Ia SNe - accrete mass until it exceeds Chandrasekhar limit

- X-ray Binaries: $M_{tot} = M_1 + M_2$



Center of MASS:

$$r_{CM} = \frac{M_1 r_1 + M_2 r_2}{M_1 + M_2}$$

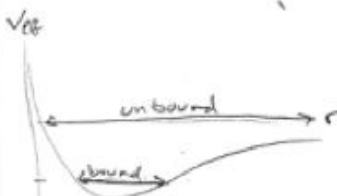


total energy: $E = E_{kin} + E_{pot} = \frac{1}{2} M \dot{r}^2 + \frac{1}{2} M \omega^2 r^2 - \frac{GM_1 M_2}{r}$

effective kinetic energy $K_{eff} = \frac{1}{2} M \dot{r}^2 + M \omega^2 r^2 - \frac{1}{2} M \omega^2 r^2$

effective potential energy $U_{eff} = -\frac{GM_1 M_2}{r}$

effective potential: $V_{eff} = \frac{U_{eff}}{M} = -\frac{1}{2} \omega^2 r^2 - \frac{G(M_1 + M_2)}{r}$

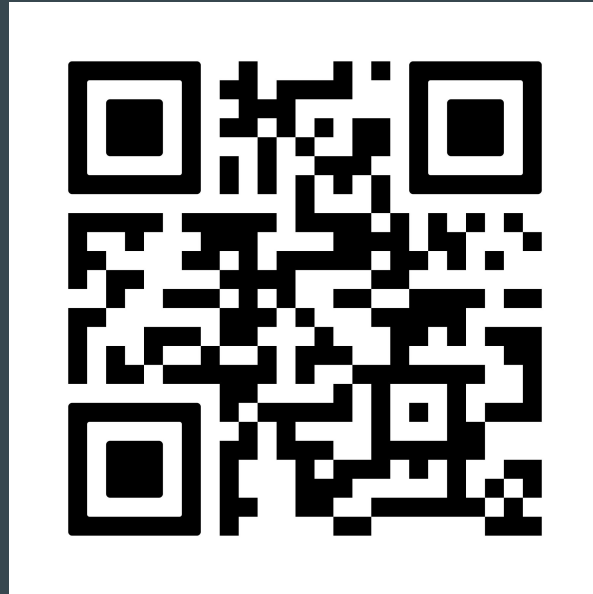


Kepler's Laws

- Stars & Planets in bound systems move in elliptical orbits around the center of mass
- Area swept out by a radius vector is constant: $dA/dt = \text{constant}$
- Orbital period squared is proportional to the semi-major axis cubed: $T_{orb}^2 = \frac{4\pi^2}{G(M_1 + M_2)} a^3$

Questions, Comments, or Concerns?

<https://forms.gle/ywP1THADKCq1nDPy9>



Lecture 2: Electromagnetic Radiation from Infrared to Gamma Rays

...

Learning Objectives and Overview

By the end of this course, students will be able to:

...identify major stars and constellations in the night sky, recount the life-cycle of a star from the Main Sequence to supernova, and distinguish between White Dwarfs, Neutron Stars, and Black Holes.

...describe the basic components of an optical telescope, explain the major differences between optical, infrared, and UV astronomy, describe why X-ray and gamma ray telescopes operate differently from OIR and UV telescopes.

...describe the basic components of a radio antenna, explain how radio interferometers work, and list the astrophysical sources of radio waves.

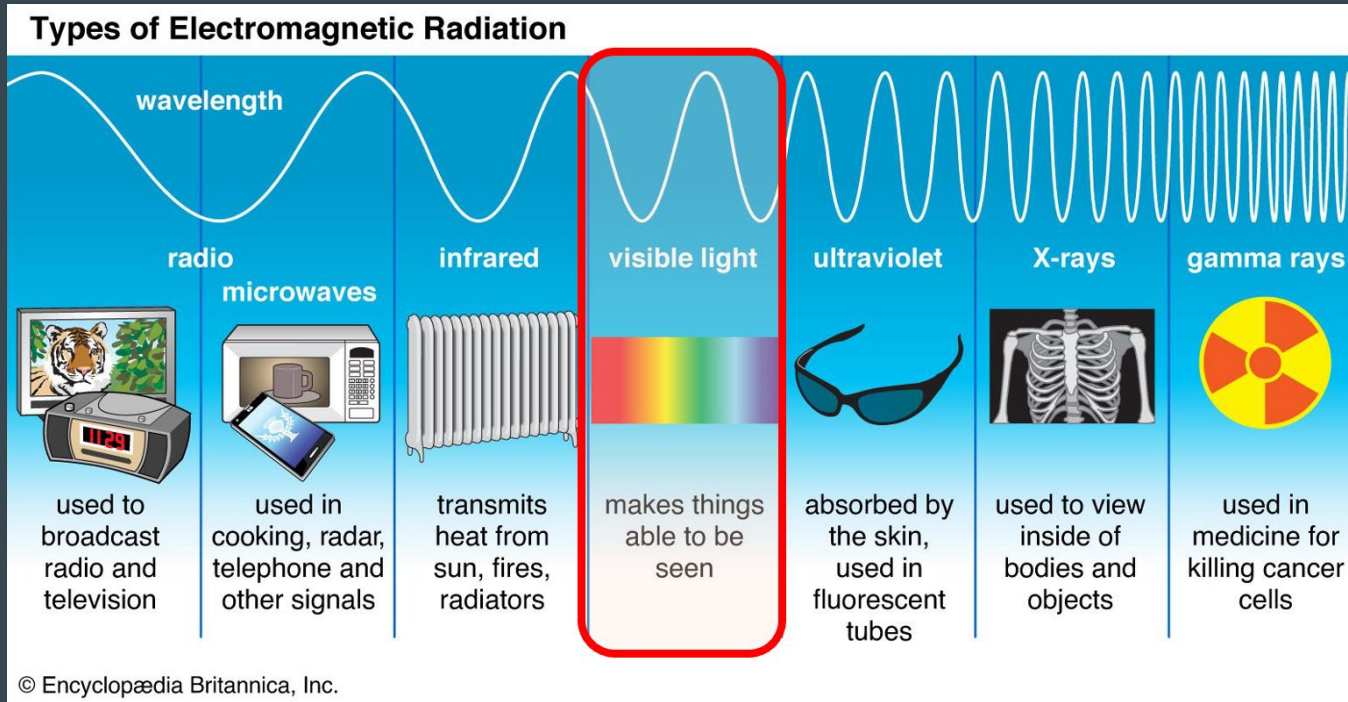
...describe the components of a galaxy (disk, bulge, ISM, halo, CGM), define cosmology, how it is studied (redshift, CMB, 21 cm cosmology, simulations, FRBs), explain how distance, redshift, and time are related within general relativity, and understand how the presence of dark matter and dark energy affect our picture of the Universe.

...list some of the major questions in astronomy today and refer to resources to continue exploring astronomy within and around Pasadena.

What is Light?

Light is **energy** that travels in **waves** carried by electric and magnetic fields

All waves have a wavelength and speed $c=671$ million miles per hour = 299 million meters per second

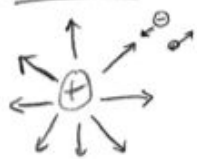


Light can also be defined as particles, **photons**, which are discrete **quanta** of electromagnetic fields

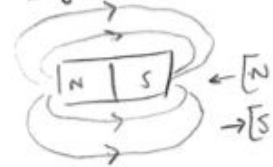
2.11

Electromagnetic Radiation (Light) -

Electric field



Magnetic field



Wavelength (λ) - distance between wave crests

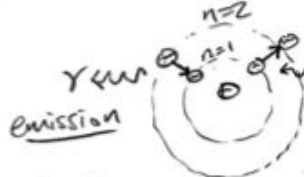
frequency (ν): $\nu = c/\lambda$

Energy: $E = h\nu = pc$
Planck's Constant

speed of light
 $c = 300 \text{ million meters/second}$

Photon - packet of light energy that behaves like a massless particle

$E = h\nu$

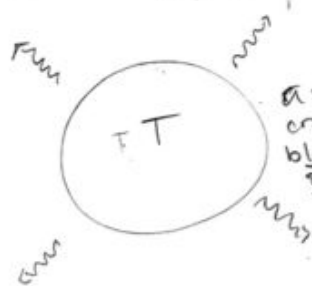


absorption

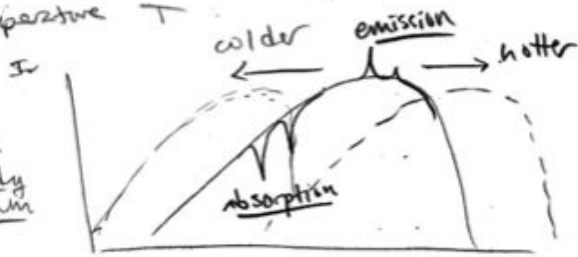
$E = E_2 - E_1$
 $\lambda = \frac{hc}{E}$

\Rightarrow each chemical has unique absorption & emission lines

Blackbody Radiation - radiation from an object with temperature T



a star creates a blackbody spectrum



lower frequency
 longer wavelengths
 (redder)

higher frequency
 shorter wavelengths
 (bluer)

e.g. Hydrogen Balmer lines

- $n=3 \rightarrow 2$: 626.279 nm \rightarrow red
- $n=4 \rightarrow 2$: 486.176 nm \rightarrow cyan
- $n=5 \rightarrow 2$: 434.5412 nm \rightarrow blue

Blackbody Radiation

Radiation that is in thermal equilibrium (all photons at the same temperature)

Hotter = BLUE

Colder = RED

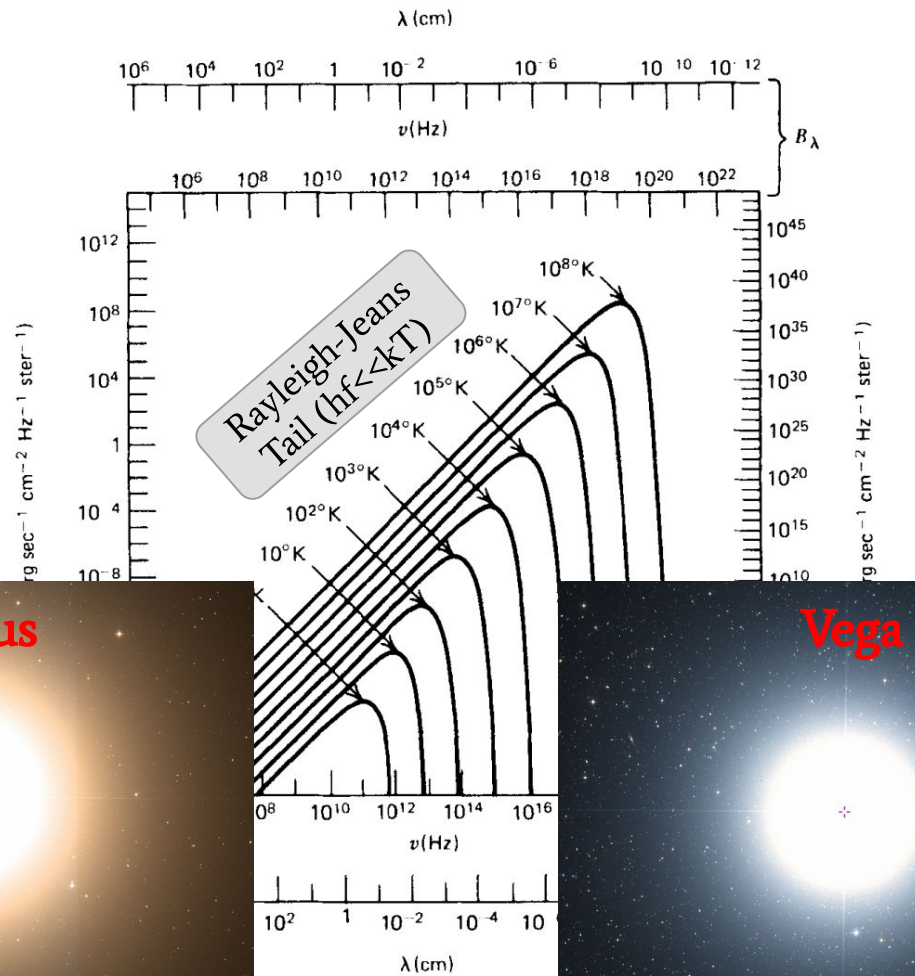
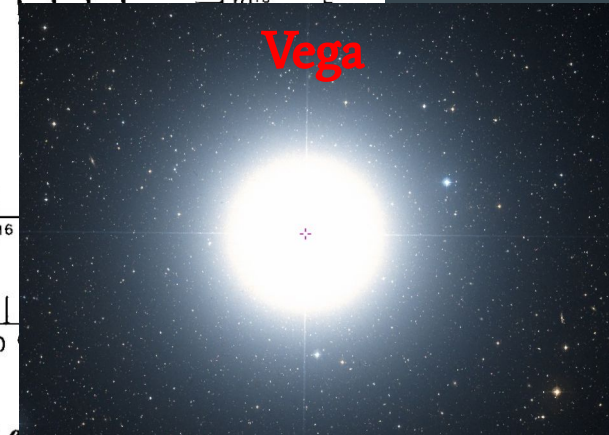
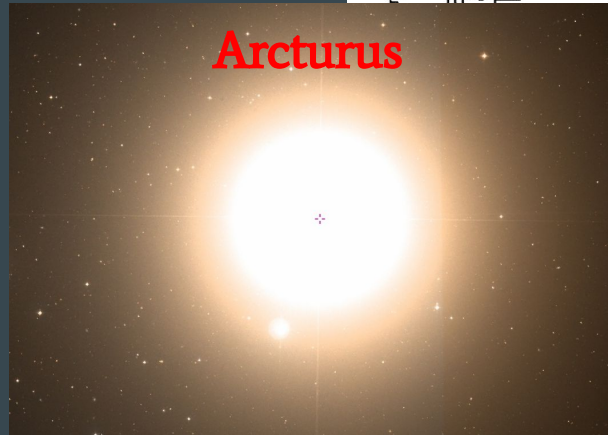


Figure 1.11 Spectrum of blackbody radiation at various temperatures (taken from Kraus, J. D. 1966, Radio Astronomy, McGraw-Hill Book Company)

Stellar Spectra

Stars' spectra tell us about their chemical content, environment, age, and speed!

Kirchoff's Laws:

1. perfect blackbody has continuous spectrum with no spectral lines
2. **hot diffuse gas** produces bright **emission** lines
3. **cool dense gas** in front of continuous spectrum source produces dark **absorption** lines

Spectra can be used to measure **radial velocities** of stars and **cosmological redshifts** (distances) of galaxies using the **doppler effect**:

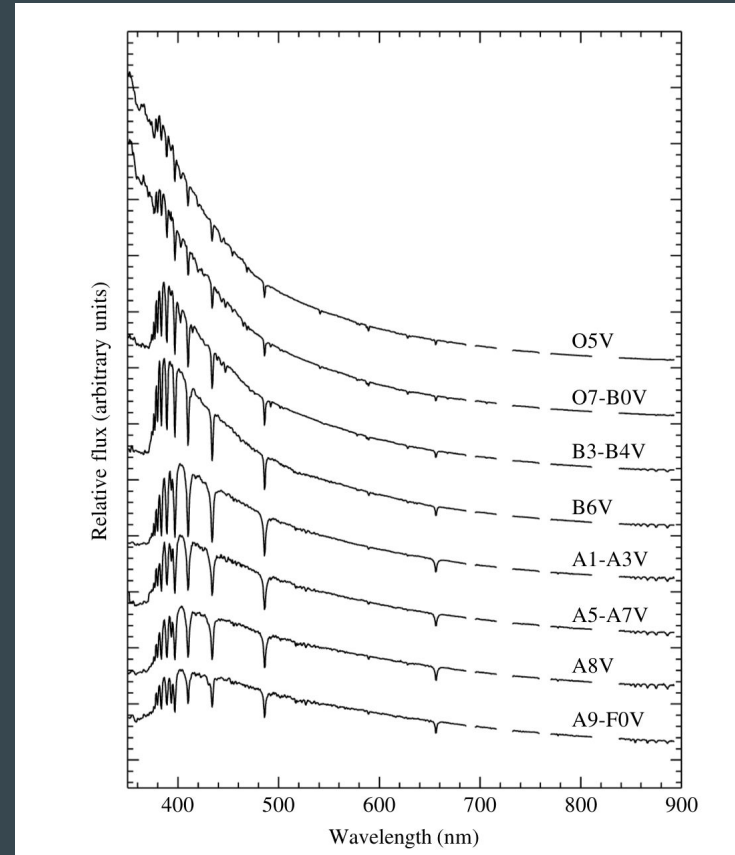
$$\text{Radial velocity: } v = (\lambda c) \Delta \lambda$$

$$\text{Cosmological redshift: } z = \Delta \lambda / \lambda - 1$$

$$\text{Luminosity distance: } D = cz / H_0 \text{ (Hubble's constant } H_0 \approx 70 \text{ km/s/Mpc)}$$

Demo:

https://phys.libretexts.org/Courses/HACC_Central_Pennsylvania's_Community_College/Astronomy_103%3A_Introduction_to_Planetary_Astronomy/04%3A_Electromagnetic_Radiation/4.04%3A_Kirchhoffs_Laws

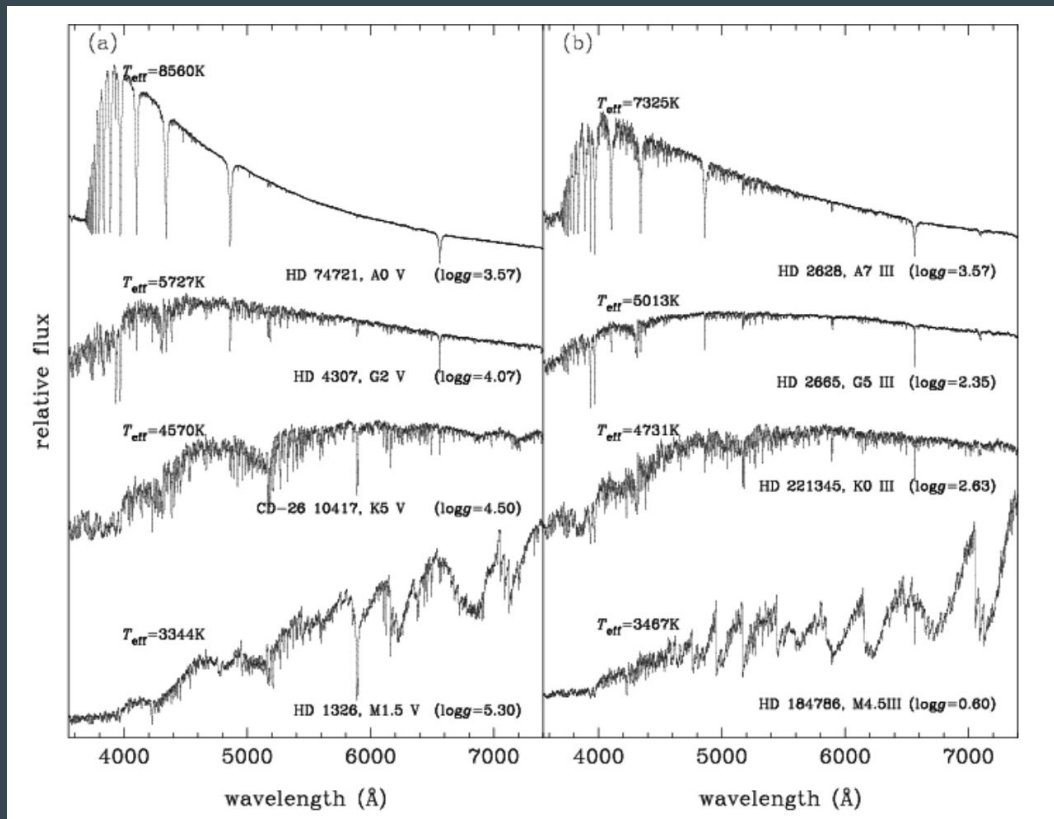


Sub-Giant Star Spectra
(Silva & Cornell 1992)

Think-Pair-Share

How would you distinguish which spectral lines come from the star and which ones come from gas in the Interstellar Medium?

Stellar Spectra Examples



MILES Stellar Spectra
Library
(Falcón-Barroso+2011)
<https://research.iac.es/proyecto/miles/pages/stellar-libraries/miles-library.php>

Spectral Class	Color	Approximate Temperature (K)	Principal Features	Examples
O	Blue	> 30,000	Neutral and ionized helium lines, weak hydrogen lines	10 Lacertae
B	Blue-white	10,000–30,000	Neutral helium lines, strong hydrogen lines	Rigel, Spica
A	White	7500–10,000	Strongest hydrogen lines, weak ionized calcium lines, weak ionized metal (e.g., iron, magnesium) lines	Sirius, Vega
F	Yellow-white	6000–7500	Strong hydrogen lines, strong ionized calcium lines, weak sodium lines, many ionized metal lines	Canopus, Procyon
G	Yellow	5200–6000	Weaker hydrogen lines, strong ionized calcium lines, strong sodium lines, many lines of ionized and neutral metals	Sun, Capella
K	Orange	3700–5200	Very weak hydrogen lines, strong ionized calcium lines, strong sodium lines, many lines of neutral metals	Arcturus, Aldebaran
M	Red	2400–3700	Strong lines of neutral metals and molecular bands of titanium oxide dominate	Betelgeuse, Antares
L	Red	1300–2400	Metal hydride lines, alkali metal lines (e.g., sodium, potassium, rubidium)	Teide 1
T	Magenta	700–1300	Methane lines	Gliese 229B
Y	Infrared ¹	< 700	Ammonia lines	WISE 1828+2650

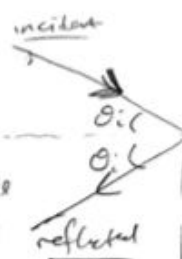
Geometric Optics



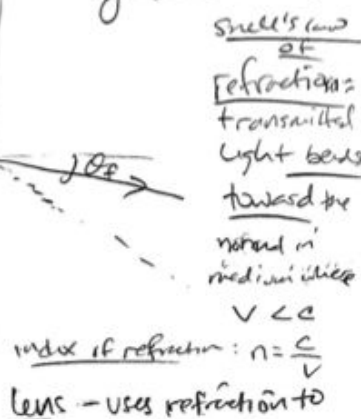
Stars emit light in all directions (isotropic)

Law of reflection:
light is reflected at the angle of incidence

air ($n=1$)

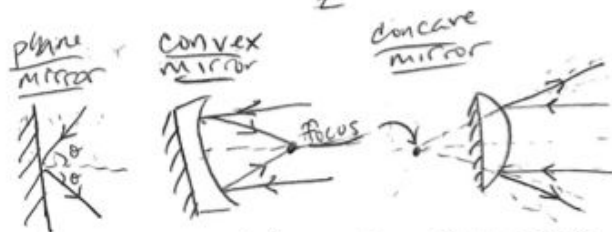


glass ($n > 1$)

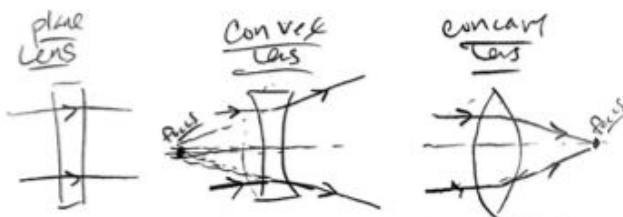


Snell's law of refraction:
transmitted light bends towards the normal in medium with $v < c$

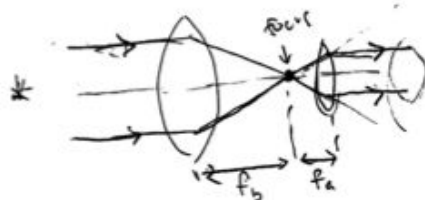
index of refraction: $n = \frac{c}{v}$
lens - uses refraction to



reflective telescope - uses mirrors to focus & magnify light



refractive telescope - uses lenses to focus & magnify light



magnification
$$M = \left(\frac{f_o}{f_e} \right)^2$$

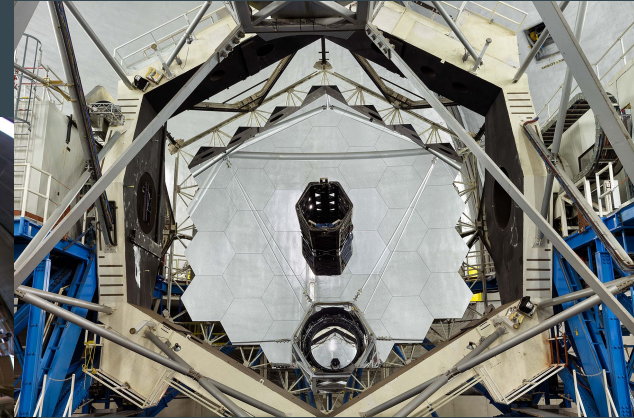
Telescope Design Examples

Palomar Hale Telescope - 200 inch Cassegrain telescope

Las Cumbres Observatories - 1 meter Ritchey-Chretien reflecting telescopes



Keck I & II telescopes - 10 meter Ritchey-Chretien reflecting telescopes with adaptive optics



Think-Pair-Share

Why are modern telescopes almost exclusively *reflective* telescopes?

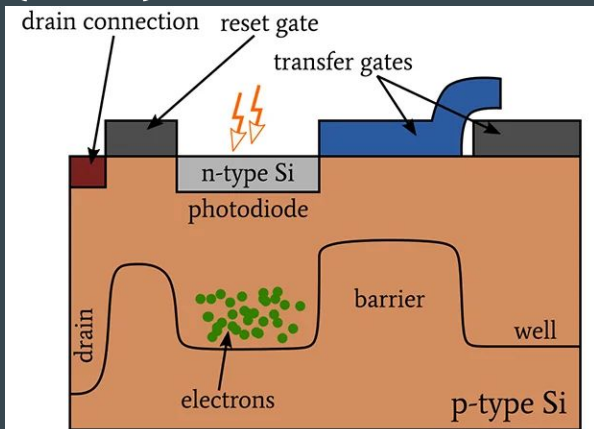
Demo: Let's go through the components of refractive binoculars and a reflective Gskyer telescope!

Detectors: Photographic Film/Plates

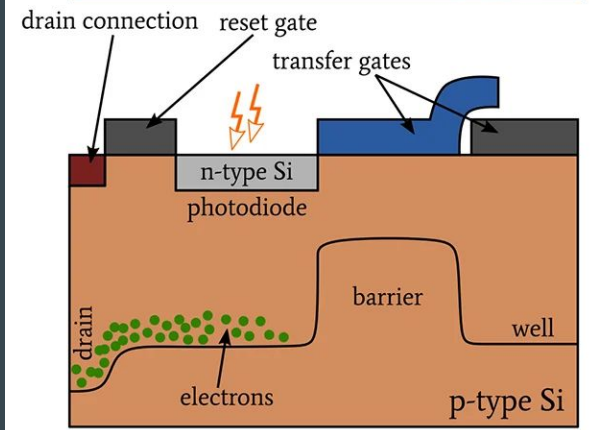


Detectors: Charge-Coupled Devices (CCD) & CMOS Detectors

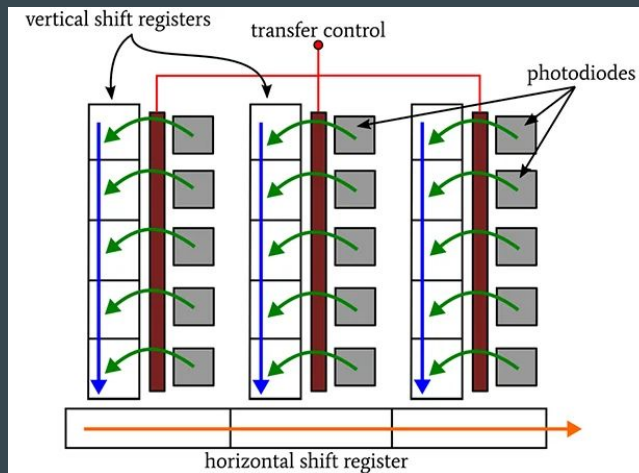
Detection



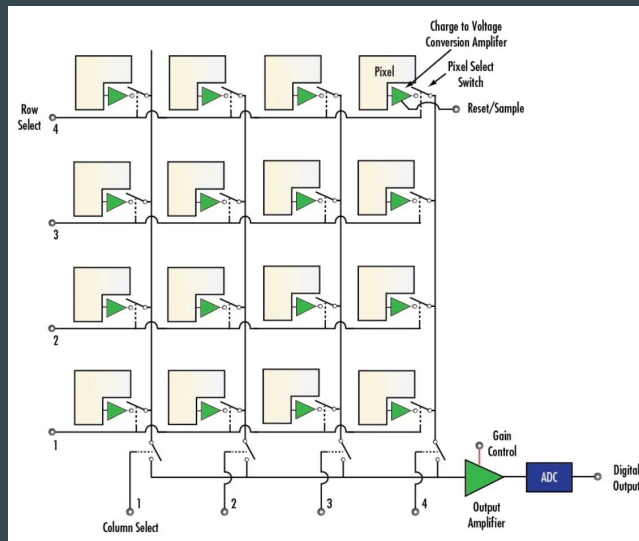
Readout



CCD

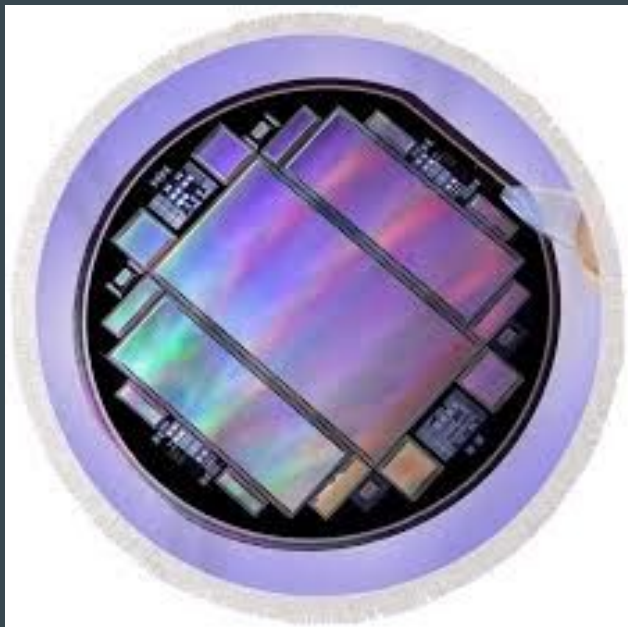


CMOS



Detectors: Charge-Coupled Devices (CCD) & CMOS Detectors

Keck Echelle Spectrograph
Imager (ESI) 2048 x 4096
CCD (15 μm pixels)

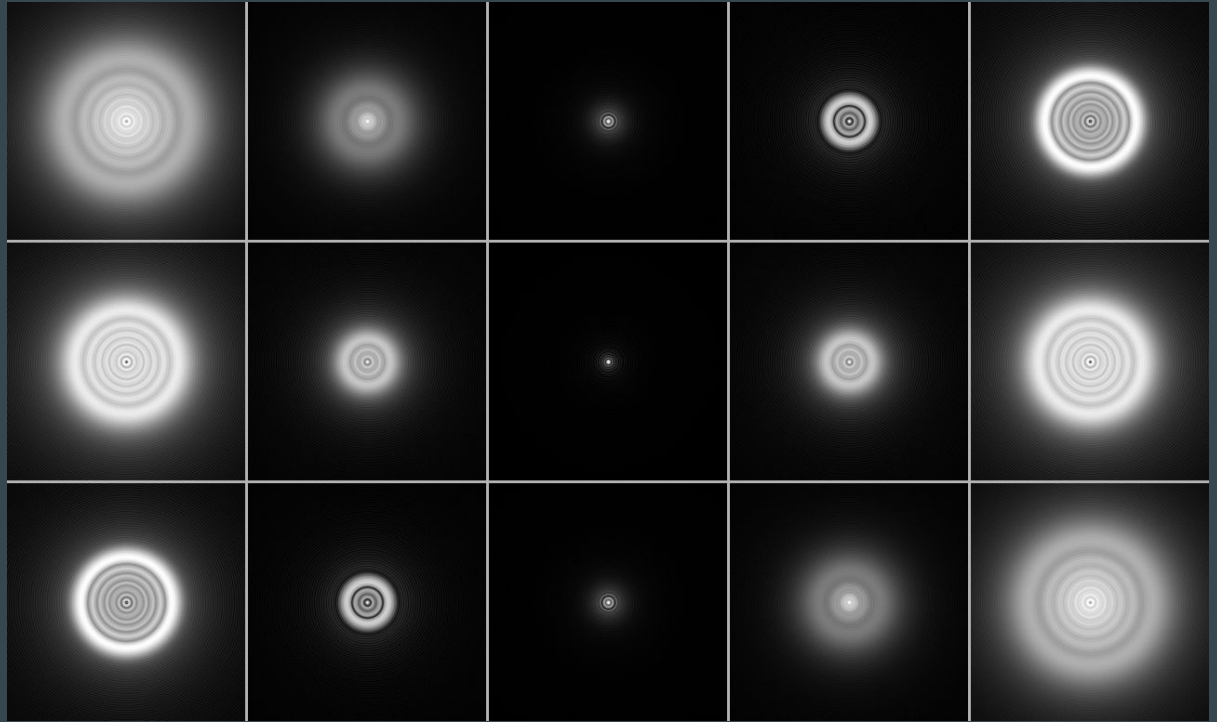


ESI CCD Characteristics	
Full-well depth	105,000e-
Read noise	2.7e-
Dark current (-120C)	2 e-/pix/hour
Gain (low)	1.29 e-/DN
Gain (high)	0.5 e-/DN
Serial CTE (fast readout)	0.99998
Serial CTE (normal readout)	0.99998
Serial CTE (slow readout)	0.99999
Readout time (fast)	39 sec
Readout time (normal)	57 sec
Readout time (slow)	120 sec

ESI CCD Q.E.	
3200 \AA	10.2%
3500 \AA	12.1%
4000 \AA	60.8%
4500 \AA	75.5%
5000 \AA	82.4%
6000 \AA	80.3%
6500 \AA	79.7%
7000 \AA	77.1%
8000 \AA	68.9%
9000 \AA	45.0%
10000 \AA	11.3%

Point Spread Function

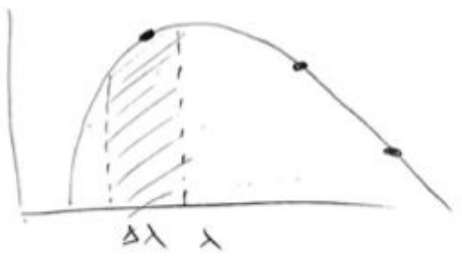
Spatial response of the detector due to the aperture size ; single lens makes an Airy function PSF (“spherical aberration”)



2.3/

Photometry - measuring brightness (flux) of a star in particular wavelength range using filters

- b Ultraviolet $100 \text{ nm} < \lambda < 400 \text{ nm}$
 - Optical $380 \text{ nm} < \lambda < 750 \text{ nm}$
 - Infrared $700 \text{ nm} < \lambda < 1 \text{ mm}$
- Photometric Systems
 extended ranges based on telescope filters
 e.g. UBVRI
 JHK



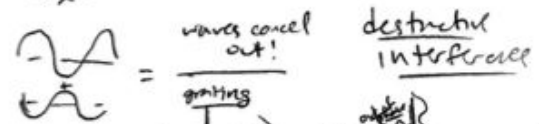
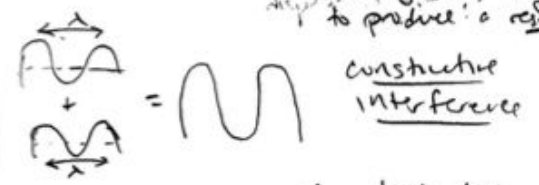
Magnitude - brightness in wavelength range (m_v)
color - difference in magnitude between different filters ($m_v - m_b$)

Spectroscopy - breaking light into its component wavelengths (dispersion) to measure high resolution spectrum

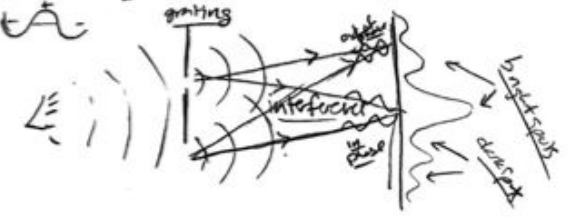
- Prism - uses wavelength dependence of index of refraction for dispersion



Superposition Principle - when 2 light waves add together, they interfere to produce a resultant

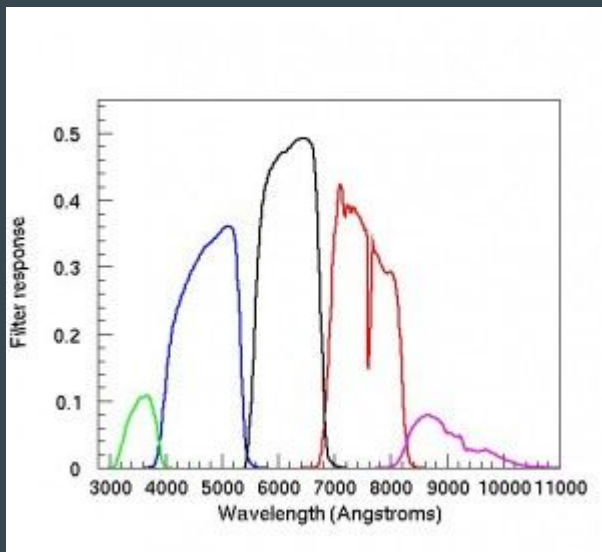


- Diffraction Grating - uses interference to disperse light

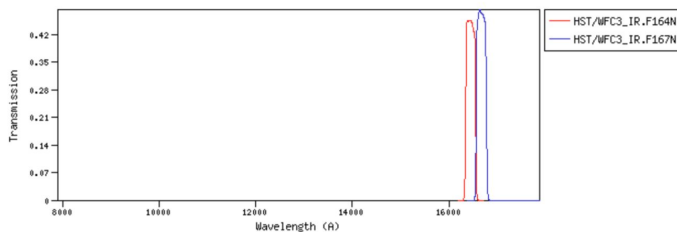
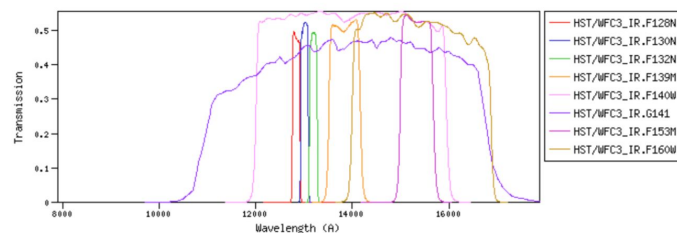
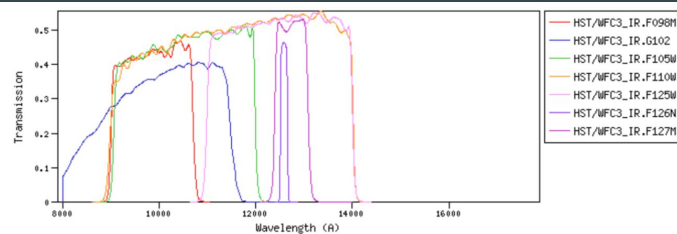


Photometric System Examples

SDSS

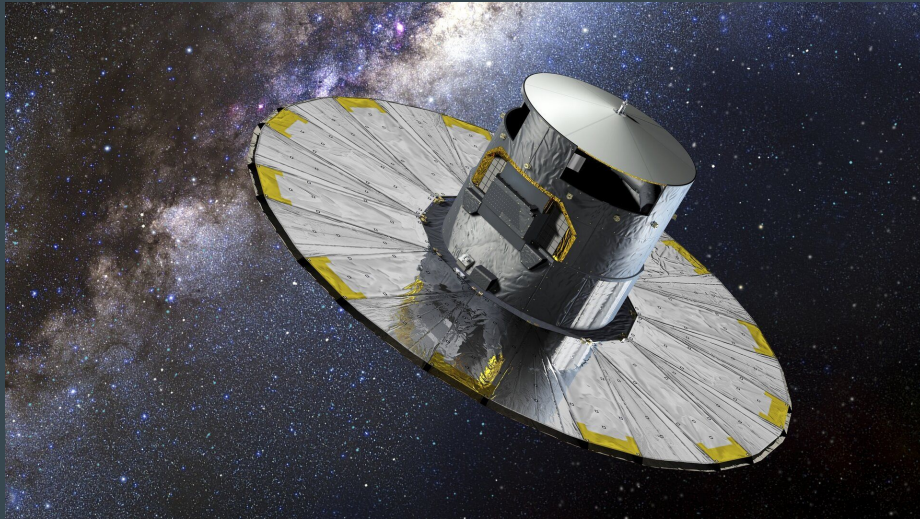


HST WideField IR Camera

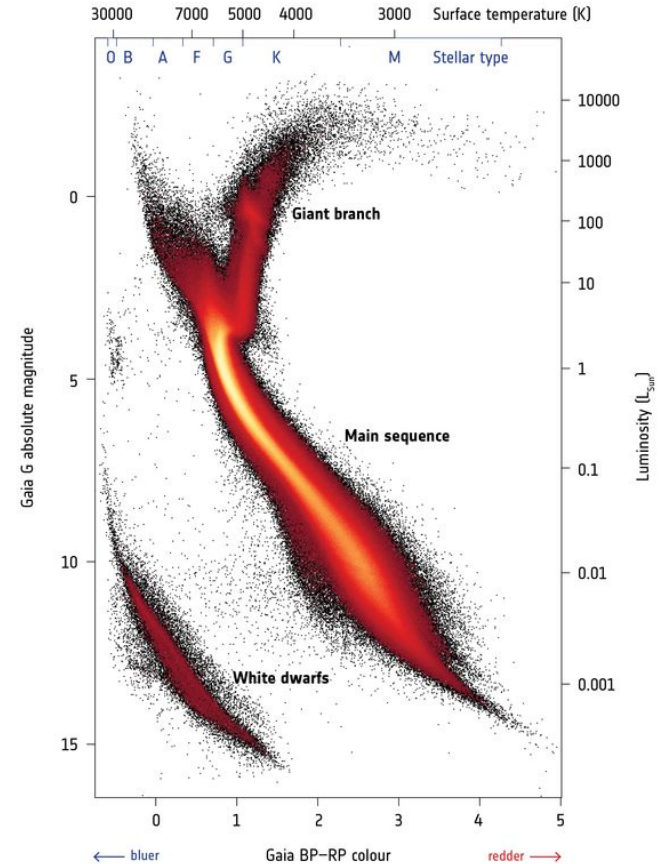


The Hertzsprung-Russell Diagram

- **Color-Index** (B-V or BP-RP) closely relates to **stellar type (O-M)** and **effective surface temperature**
- European Space Agency's *Gaia* telescope has mapped over 2 billion stars to the H-R diagram!



→ GAIA'S HERTZSPRUNG-RUSSELL DIAGRAM



$$d\sin\theta=2\lambda$$

Diffraction Gratings

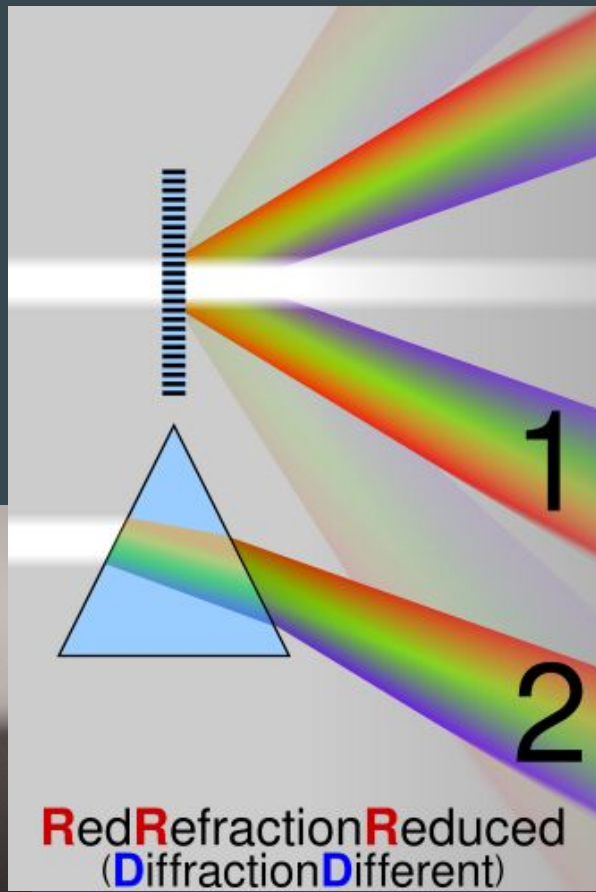
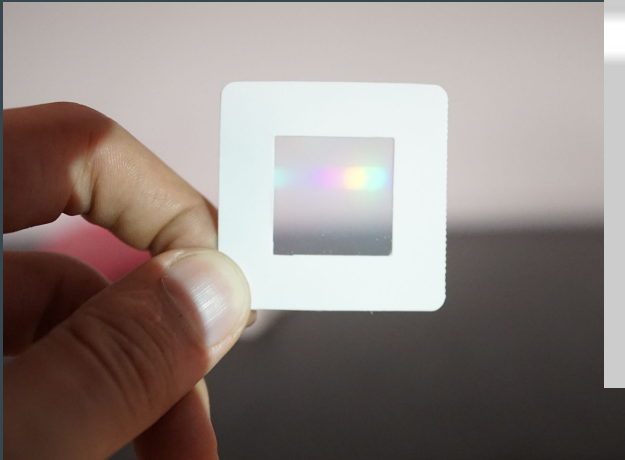
Series of N slits creates **interference** , or **diffraction** between light passing through

constructive interference : $d\sin\theta = m\lambda$

destructive interference: $d\sin\theta = (m+1/2)\lambda$

Resolution:

$$R = \Delta\lambda/\lambda = Nm$$



$$d\sin\theta=\lambda$$

$$d\sin\theta=0$$

$$d\sin\theta=-\lambda$$

Atmospheric Windows and Telescope Examples

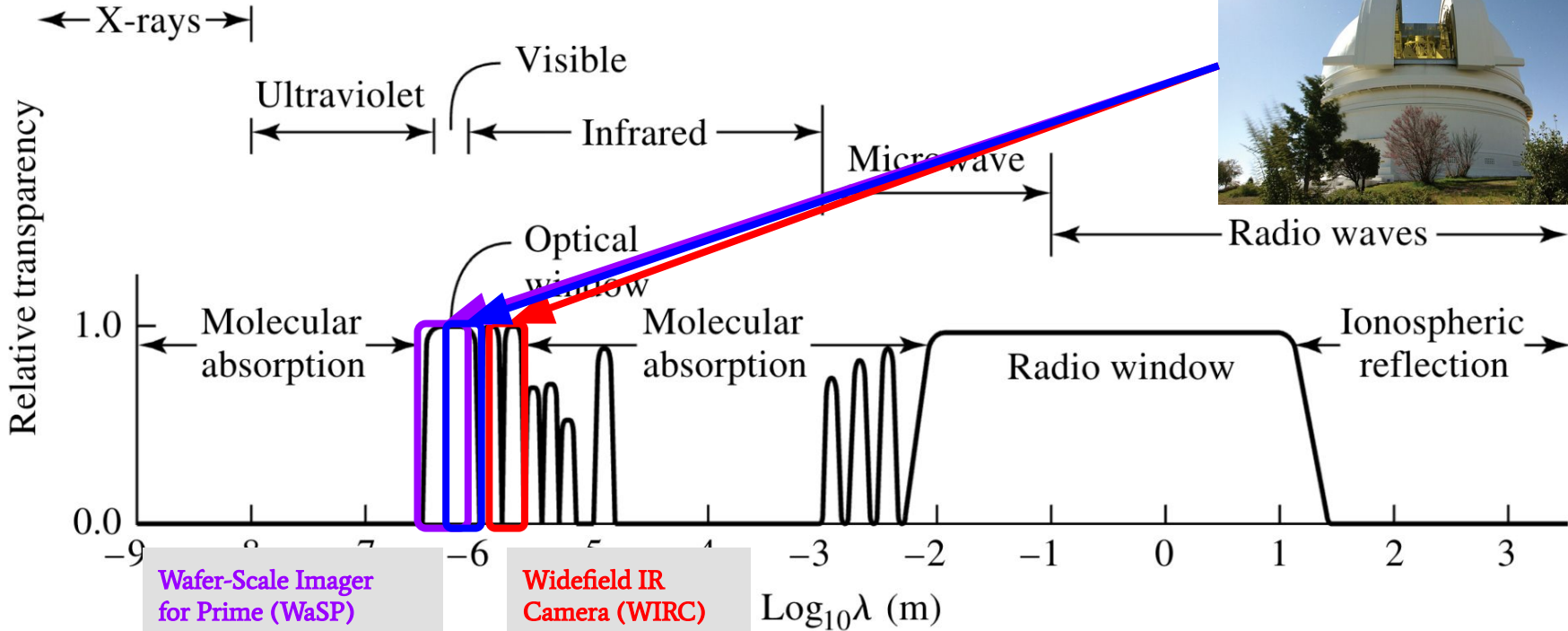


FIGURE 0.25 THE USE OF THE ATMOSPHERE AS A FUNCTION OF WAVELENGTH.

Atmospheric Windows and Telescope Examples

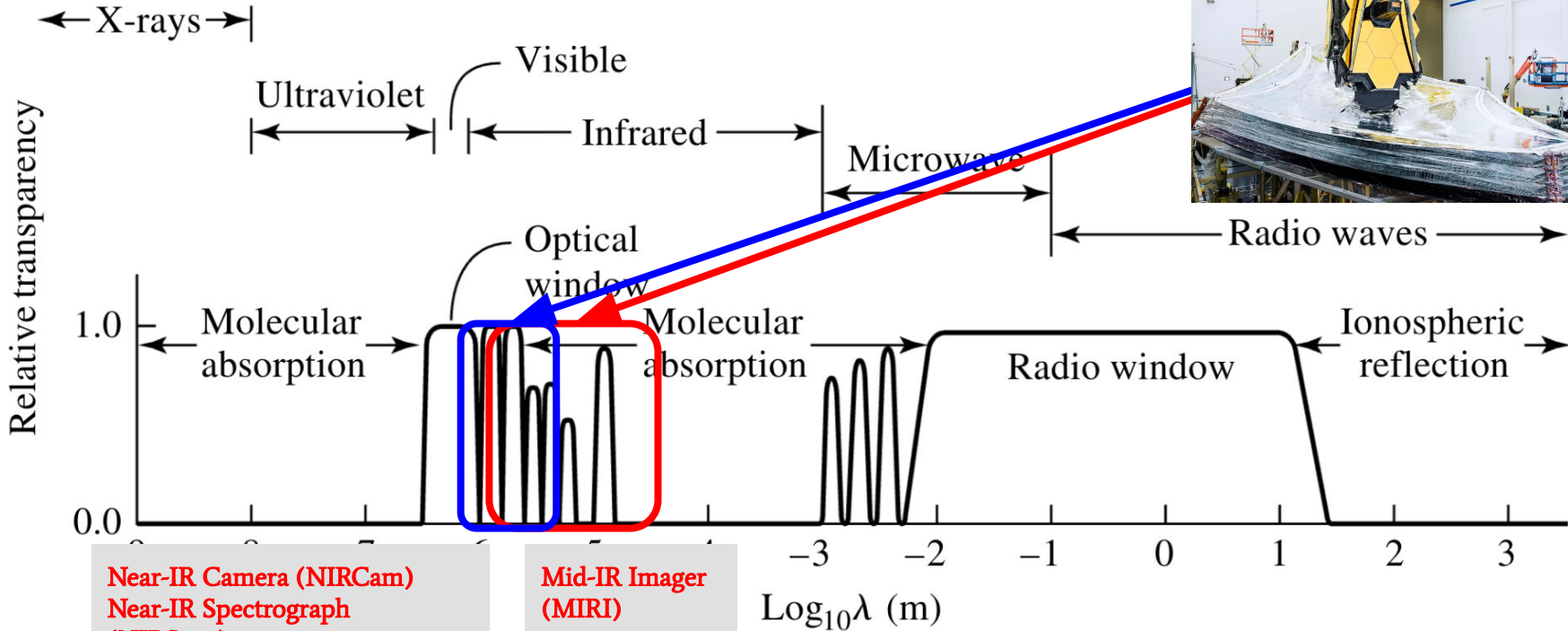


FIG. Transparency of Earth's atmosphere as a function of wavelength.

Atmospheric Windows and Telescope Examples

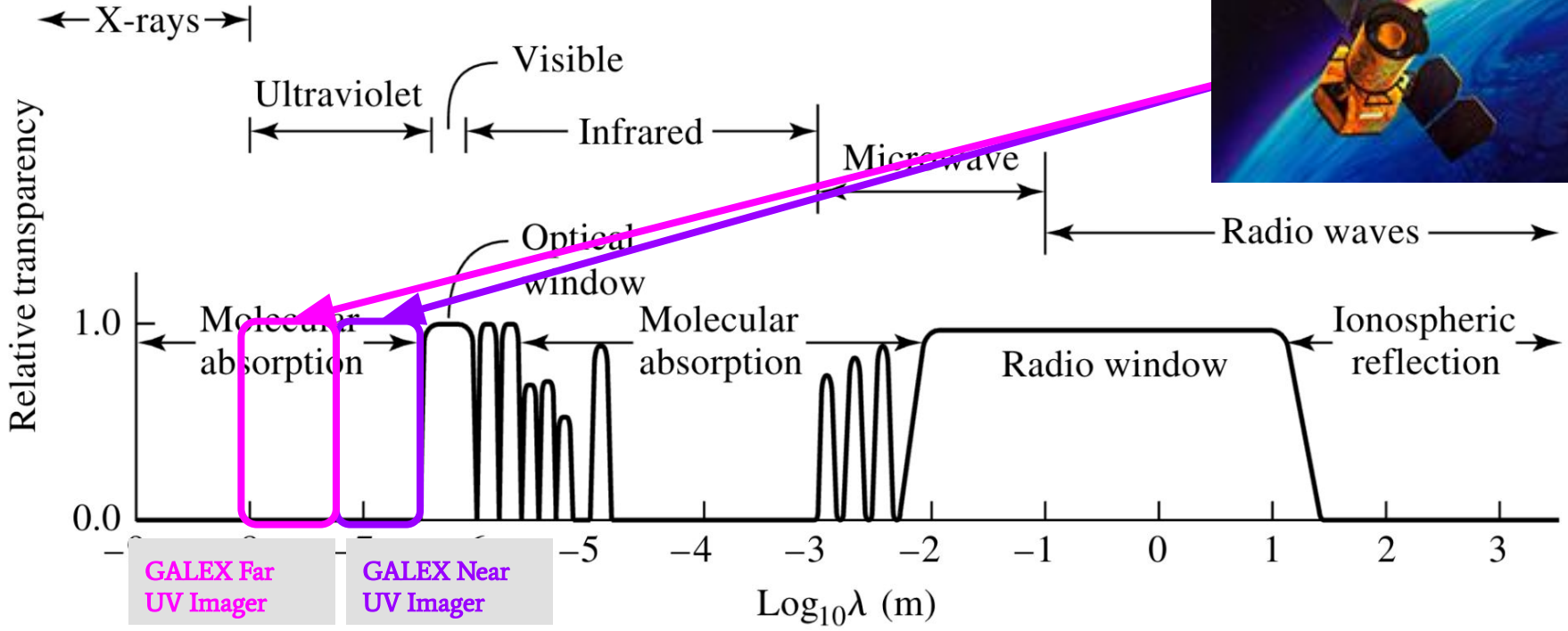
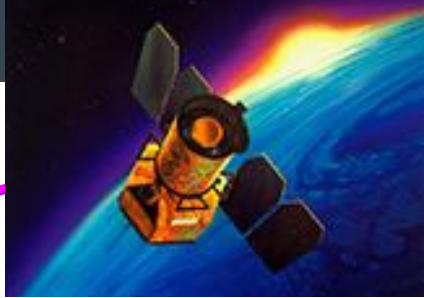


FIGURE 6.25 The transparency of Earth's atmosphere as a function of wavelength.

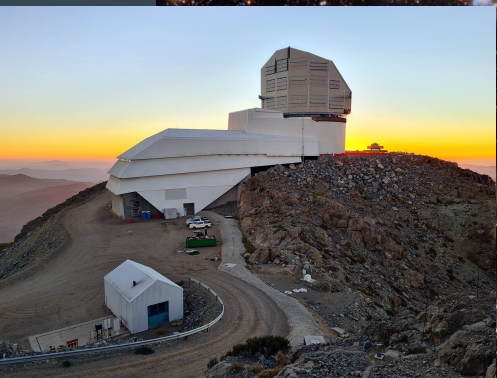
New Observatories

James Webb
Space
Telescope
(JWST)



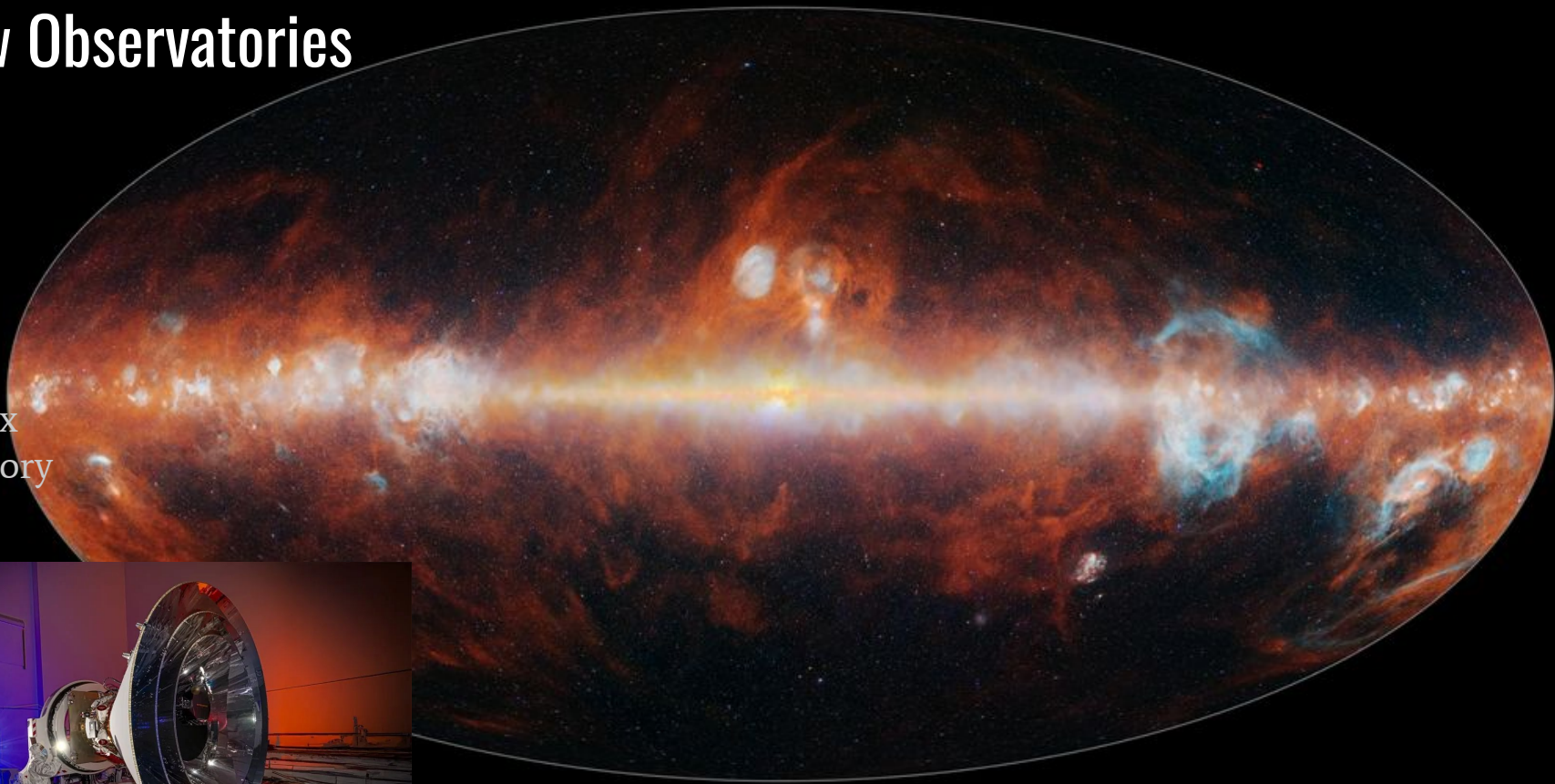
New Observatories

Vera Rubin
Observatory

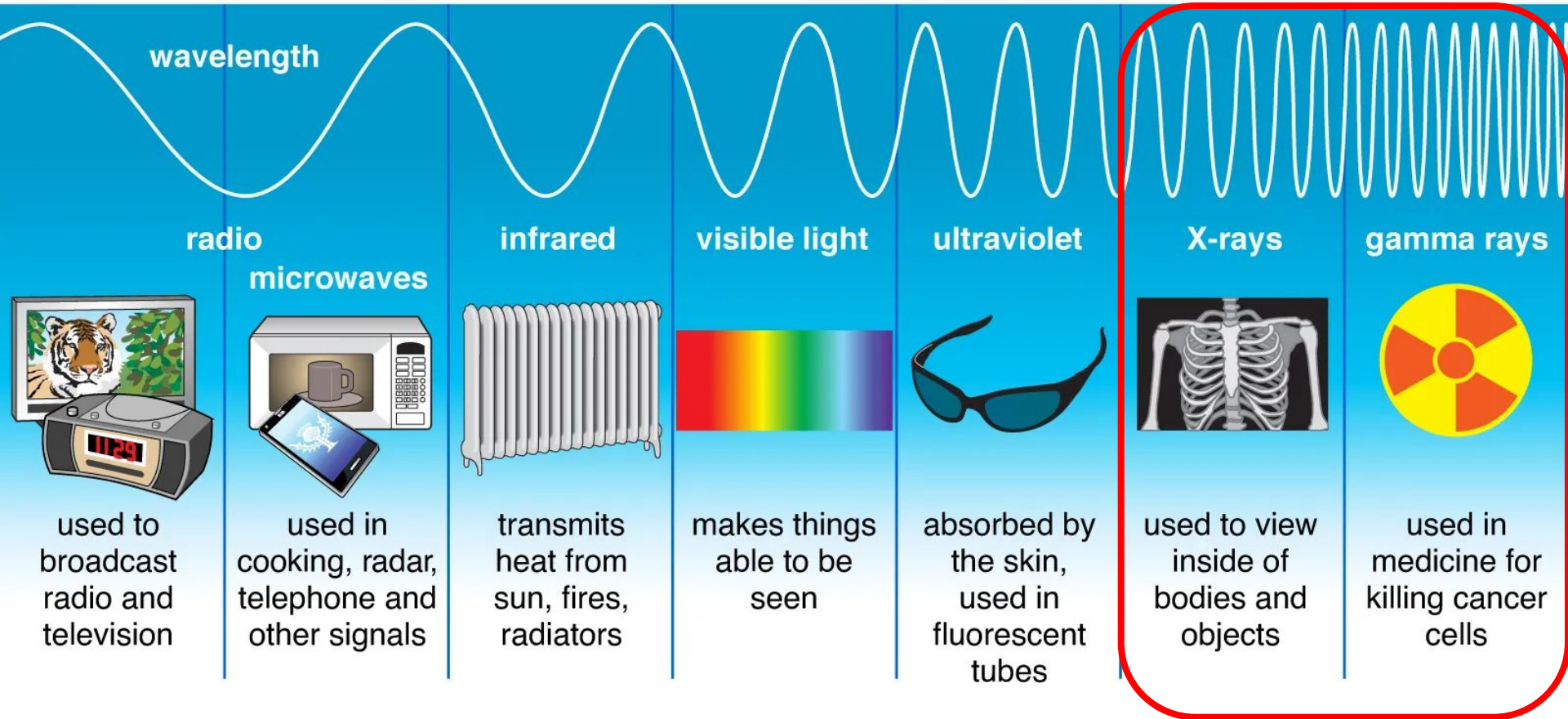


New Observatories

SPHEREx
Observatory



Types of Electromagnetic Radiation

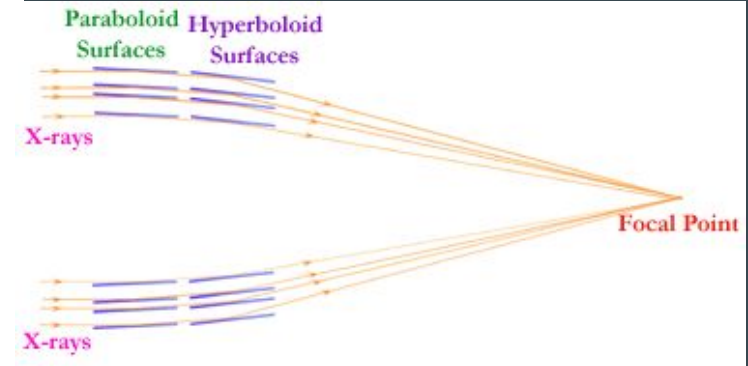
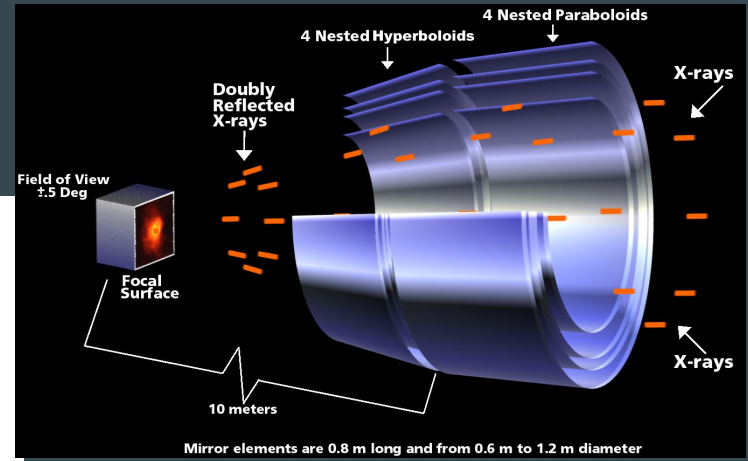
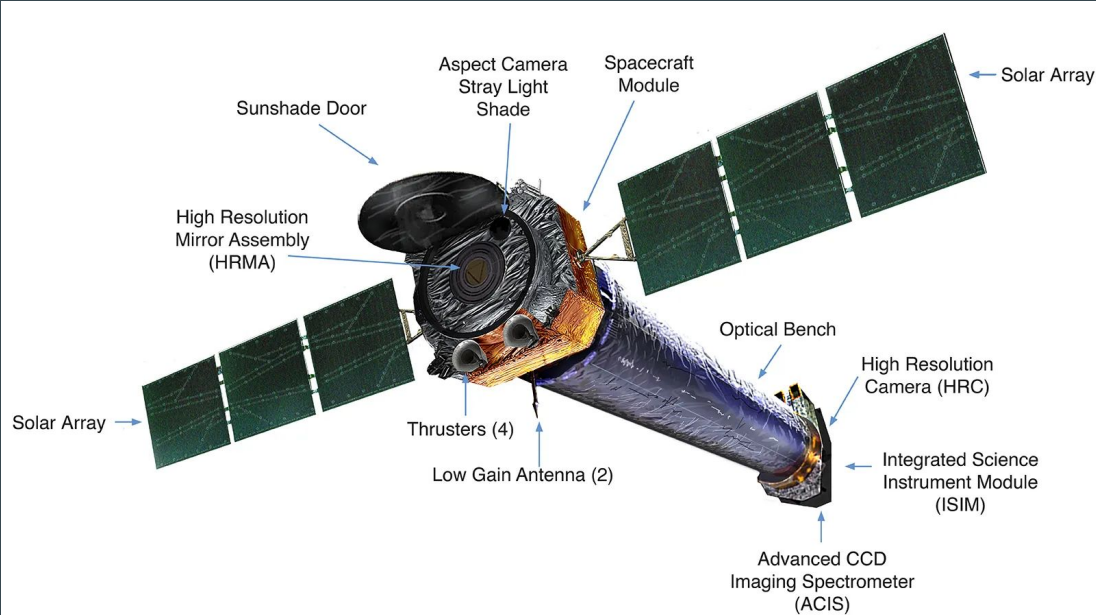


**Remember: energy $E[\text{eV}] = hc/\lambda[\text{m}]$

Chandra X-Ray Telescope - grazing incidence

Soft X-rays: 100 electronVolts (eV) - 500 eV

Hard X-rays: 500 eV - 100 keV

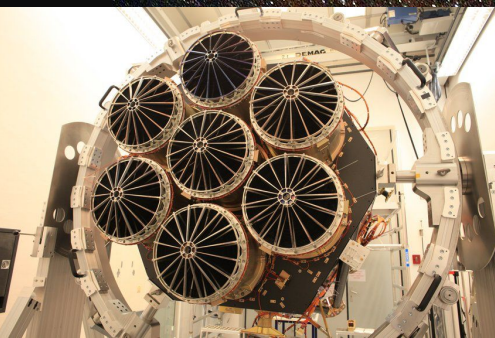


SRG/eROSITA

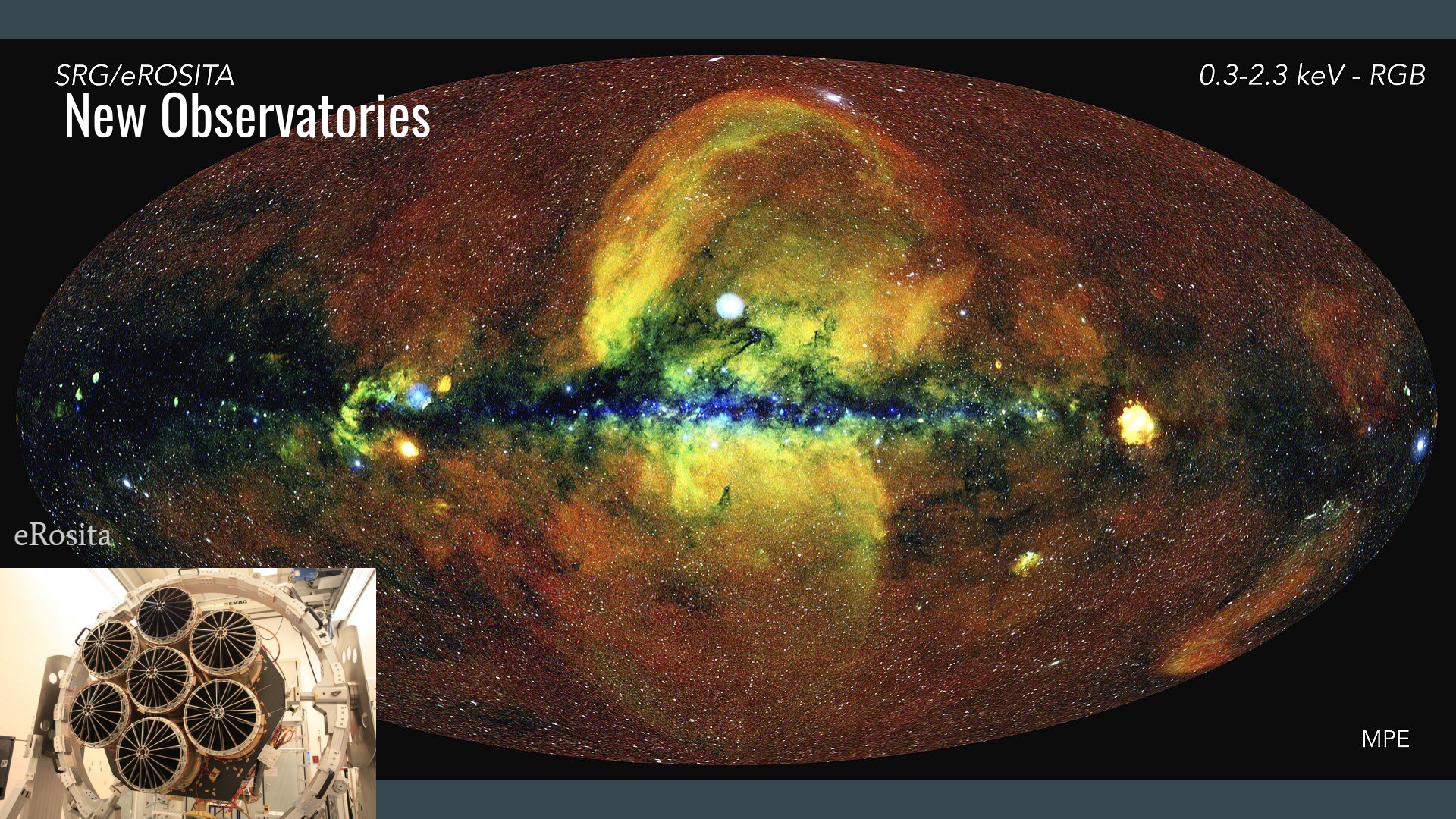
New Observatories

0.3-2.3 keV - RGB

eRosita

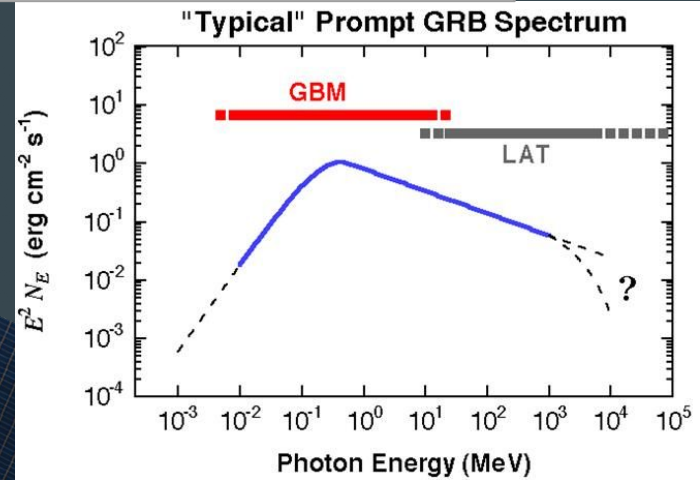
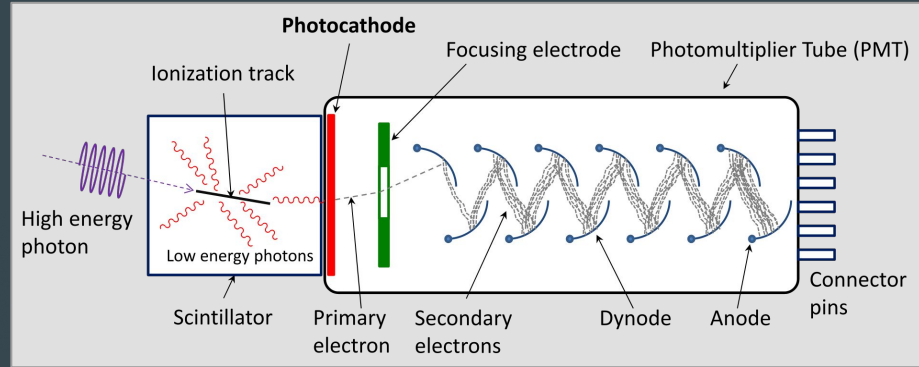
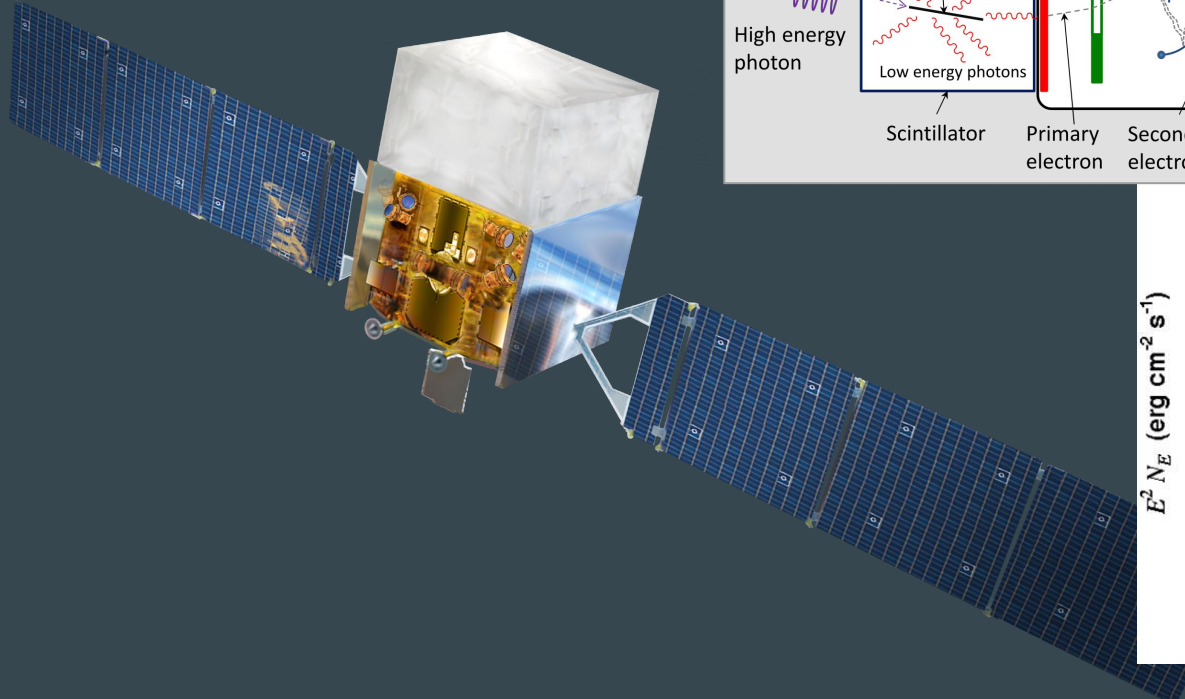


MPE



Fermi Gamma-Ray Burst Monitor - scintillometry

Gamma Rays: 100 keV - 1000 TeV



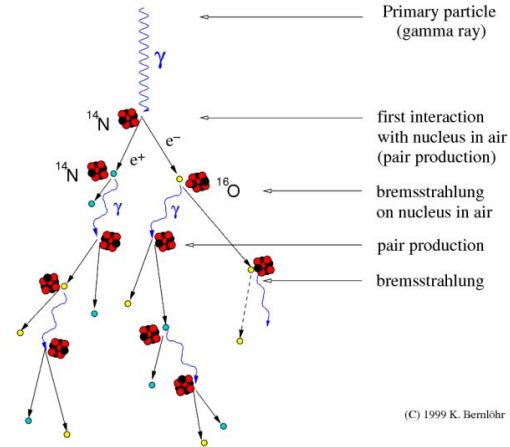
VERITAS - atmospheric Cherenkov detection

Gamma Rays: 100 keV - 1000 TeV

VERITAS uses the **atmosphere itself** as a scintillator!

****Remember: energy $E[\text{eV}]$
 $= hc/\lambda[\text{m}]$**

Development of gamma-ray air showers





Atacama Large
Millimeter Array
(ALMA)



At-Home Astronomy: Stellar Spectra and X-ray Images

Stargazing Nights are a Great Way to learn to use telescopes!

- LA Astronomical Society - <https://www.laas.org/>
 - Every Wednesday at Garvey Ranch 7:30-10pm
 - Monthly Star Parties at Griffith Park 2pm-9:45pm (next one is Feb 21)
<https://griffithobservatory.org/event/public-star-party-february-21-2026/>
- Caltech Stargazing Lectures - <https://www.astro.caltech.edu/outreach/stargazing-lecture-series>

Tools for Stellar Spectra:

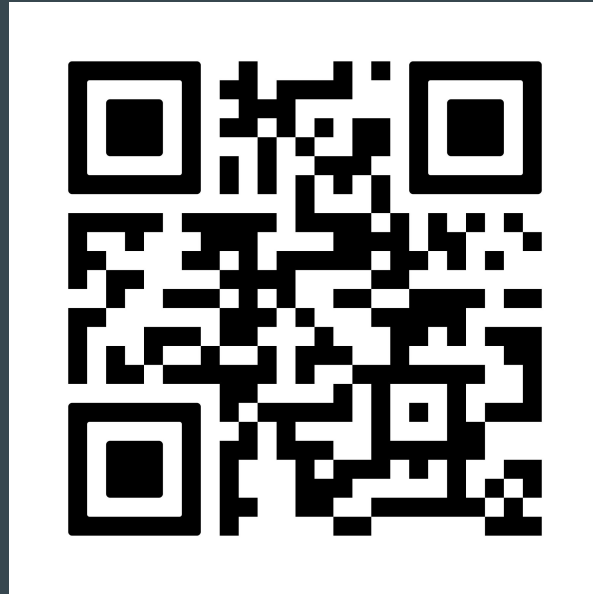
- SVO Filter Profile Service: <https://svo2.cab.inta-csic.es/theory/fps>
- MILES Library of Stellar Spectra: <https://research.iac.es/proyecto/miles/pages/stellar-libraries/miles-library.php>
- NIST Atomic Spectra Database: https://physics.nist.gov/PhysRefData/ASD/lines_form.html

Tools for X-ray Data:

- eRosita X-ray Image Skyview: <https://erosita.mpe.mpg.de/dr1/erodat/skyview/sky/>
- Chandra video of Kepler's Supernova Remnant: <https://chandra.harvard.edu/photo/2026/kepler/>

Questions, Comments, or Concerns?

<https://forms.gle/ywP1THADKCq1nDPy9>



Lecture 3: Radio Astronomy and Compact Stellar Remnants

...

Learning Objectives and Overview

By the end of this course, students will be able to:

...identify major stars and constellations in the night sky, recount the life-cycle of a star from the Main Sequence to supernova, and distinguish between White Dwarfs, Neutron Stars, and Black Holes.

...describe the basic components of an optical telescope, explain the major differences between optical, infrared, and UV astronomy, describe why X-ray and gamma ray telescopes operate differently from OIR and UV telescopes.

...describe the basic components of a radio antenna, explain how radio interferometers work, and list the astrophysical sources of radio waves.

...describe the components of a galaxy (disk, bulge, ISM, halo, CGM), define cosmology, how it is studied (redshift, CMB, 21 cm cosmology, simulations, FRBs), explain how distance, redshift, and time are related within general relativity, and understand how the presence of dark matter and dark energy affect our picture of the Universe.

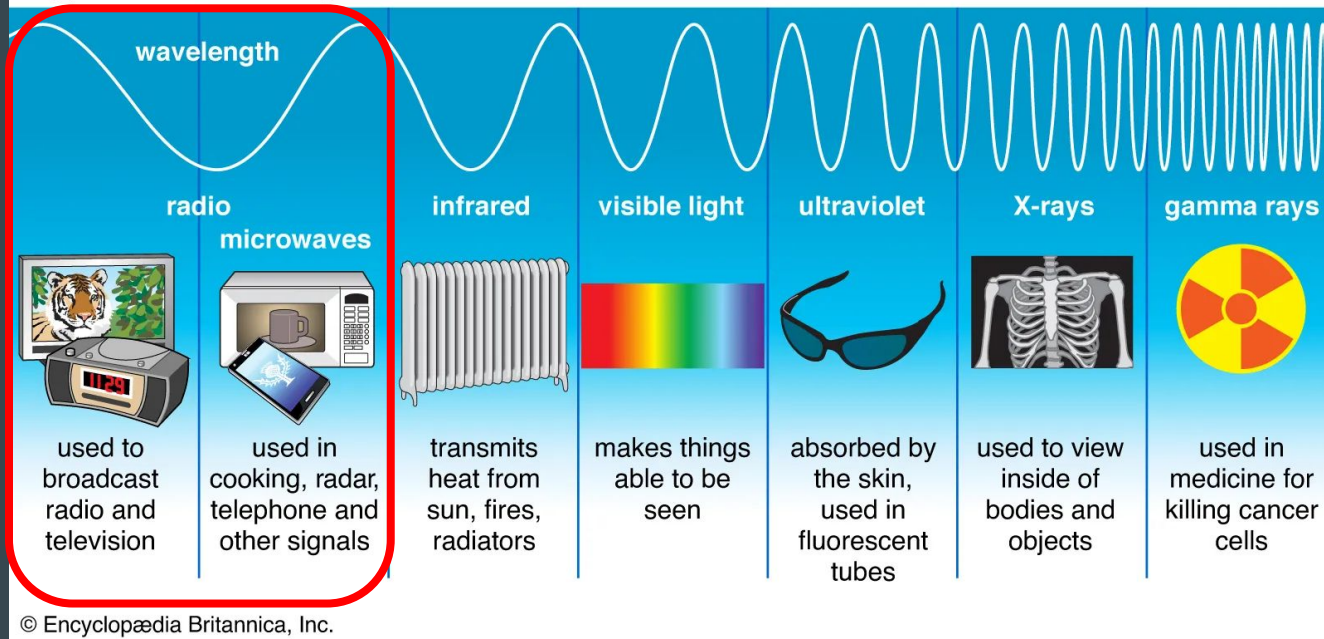
...list some of the major questions in astronomy today and refer to resources to continue exploring astronomy within and around Pasadena.

Recap: What is Light?

Light is **energy** that travels in **waves** carried by **electric and magnetic fields**

All waves have a wavelength and speed $c=671$ million miles per hour = 299 million meters per second

Types of Electromagnetic Radiation



Light can also be defined as particles, **photons**, which are discrete **quanta** of electromagnetic fields

Recall: Atmospheric Windows

Radio light has
wavelengths from
1 mm - 10 m

frequencies
from 10 kHz
- 3 THz

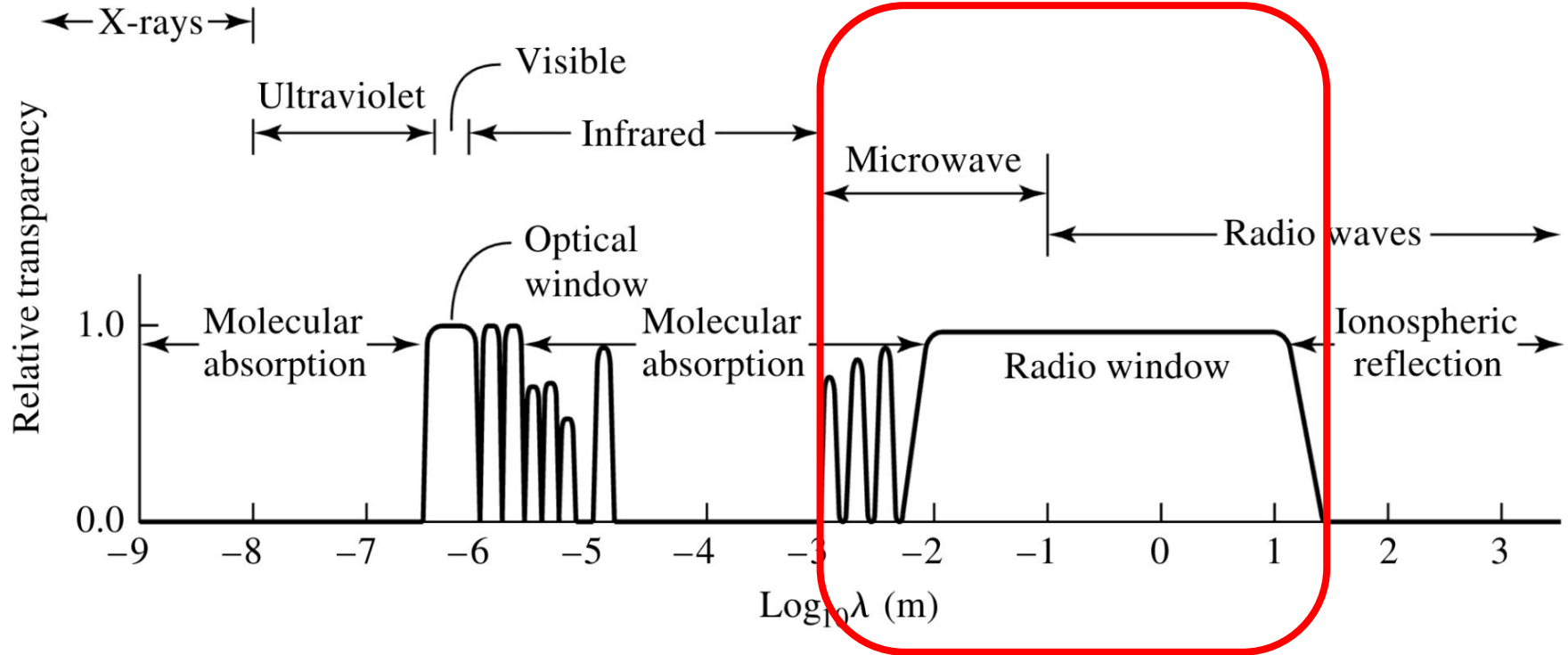
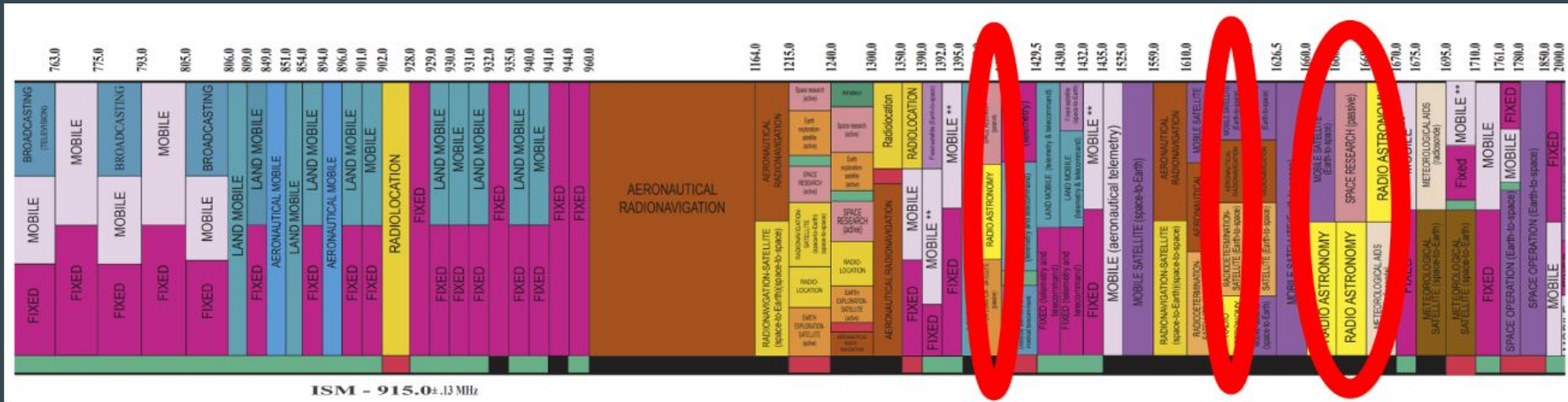


FIGURE 6.25 The transparency of Earth's atmosphere as a function of wavelength.

Radio Spectrum Allocations



The Federal Communications Commission (FCC) and International Telecommunications Union (ITU) regulate the frequency spectrum and reserve specific “bands” (frequency/wavelength ranges) for communications, television, GPS, satellites, HAM radio, radio astronomy, and more.

For example, FM radio uses 88-108 MHz while radio astronomy often uses 400-800 MHz various sub-bands between 1-2 GHz

IEEE Standard Radio Bands

Band Designation	Nominal Frequency Range
HF	3-30 MHz
VHF	30-300 MHz
UHF	300-1000 MHz (Note 5)
L	1-2 GHz
S	2-4 GHz
C	4-8 GHz
X	8-12 GHz
Ku	12-18 GHz
K	18-27 GHz
Ka	27-40 GHz
V	40-75 GHz
W	75-110 GHz
mm (Note 9)	110-300 GHz
Sub-mm	>300 GHz

Recall: Blackbody Radiation

Radiation that is in thermal equilibrium (all photons at the same temperature)

Rayleigh-Jeans Law:

$$I_{\nu} = 2\nu^2 kT / c^2$$

Brightness Temperature:

$$T_b = c^2 I_{\nu} / 2k\nu^2$$

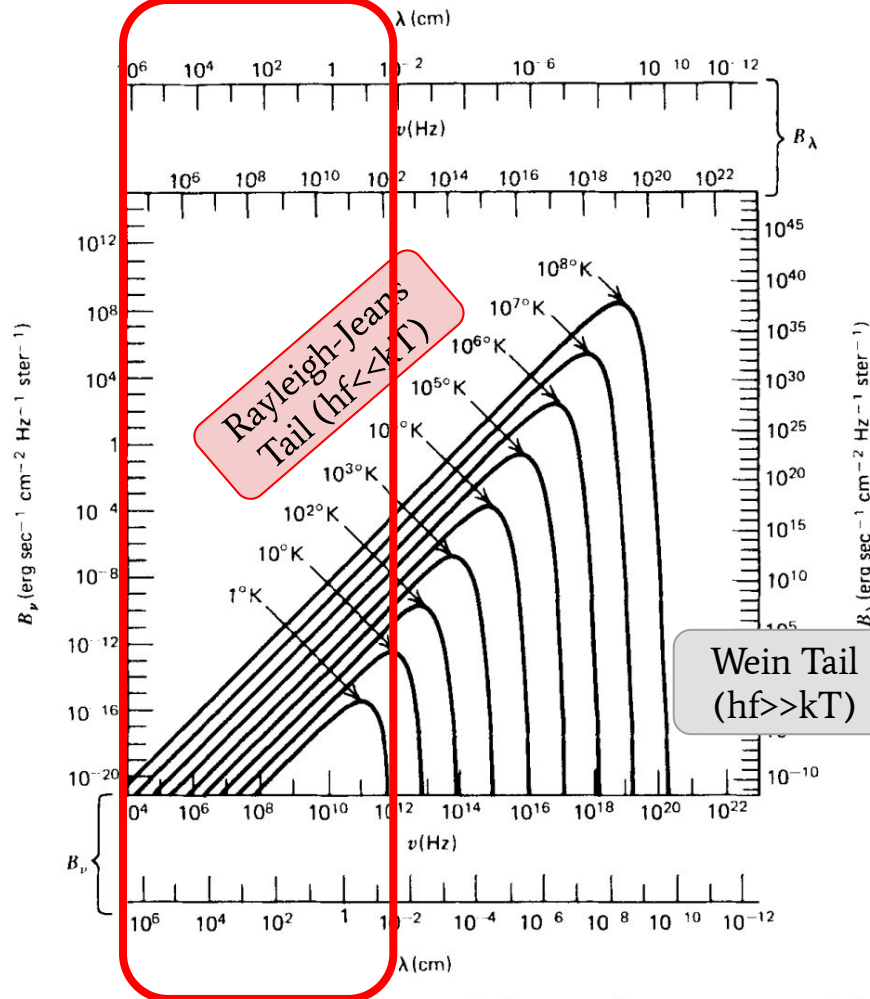
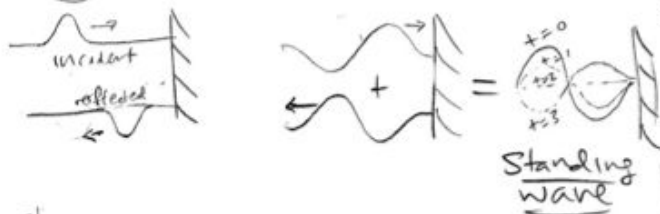


Figure 1.11 Spectrum of blackbody radiation at various temperatures (taken from Kraus, J. D. 1966, Radio Astronomy, McGraw-Hill Book Company)

3.3

Antenna - converts radiation in space into electrical current or vice versa

superposition / interference



Standing wave modes - only certain wavelengths are allowed to create standing waves!

$$\lambda_n = \frac{2L}{n}$$

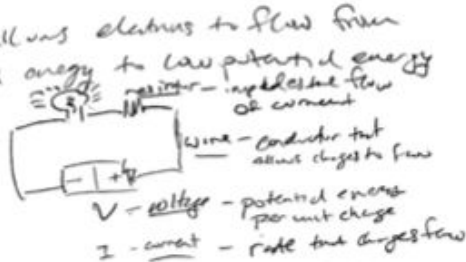
← length of string
← any number

incident and reflected wave interfere to produce a wave that appears stationary

Circuit - allows electrons to flow from high potential energy to low potential energy

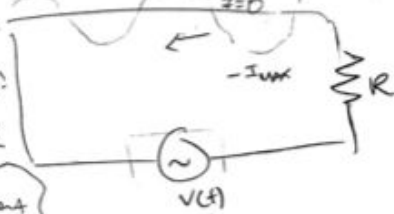
Ohm's law

$$V = IR$$



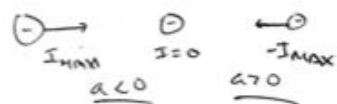
alternating current - current oscillates with time

↳ current on wire behaves like waves on a string!
↳ charges accelerate



wire with alternating current radiates (transmission)

EM waves that hit a wire induce a current (receiving)



- Terminated wire => standing wave

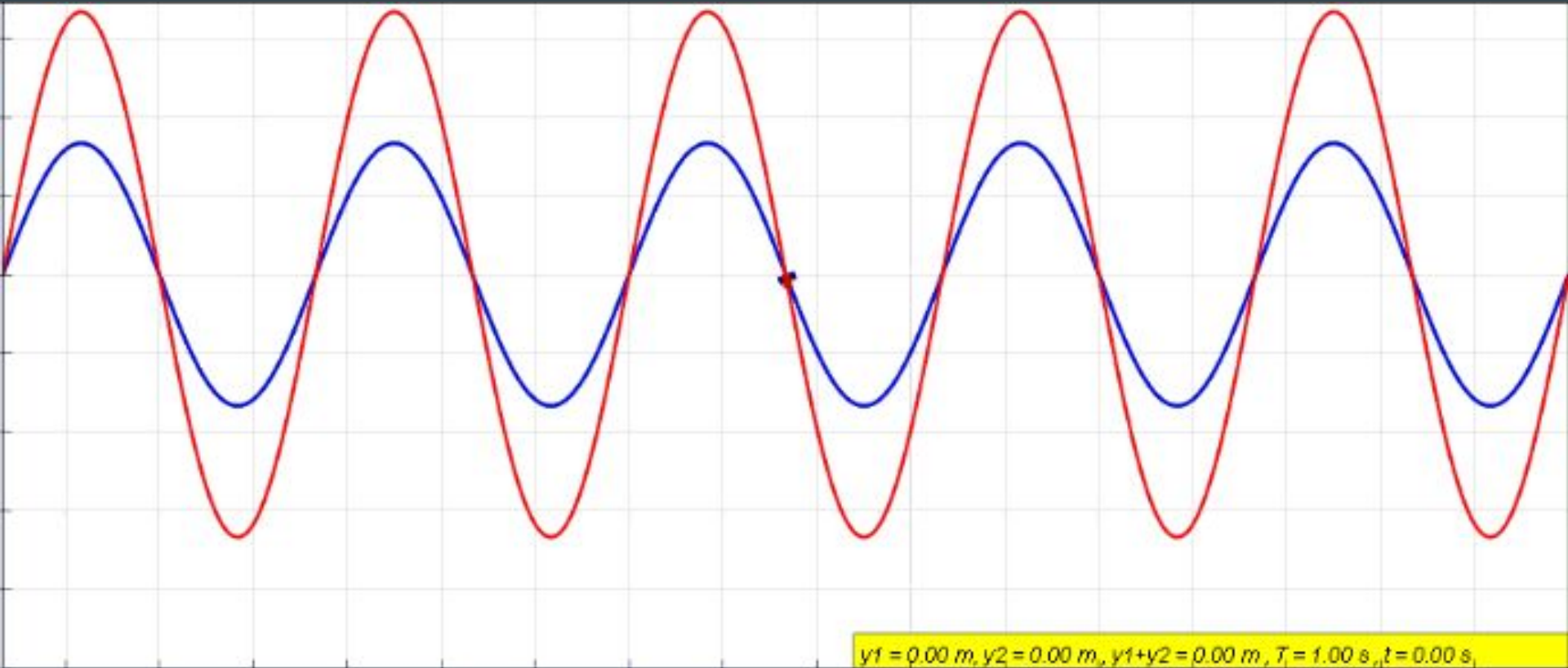


$$L = n \frac{\lambda}{2}$$

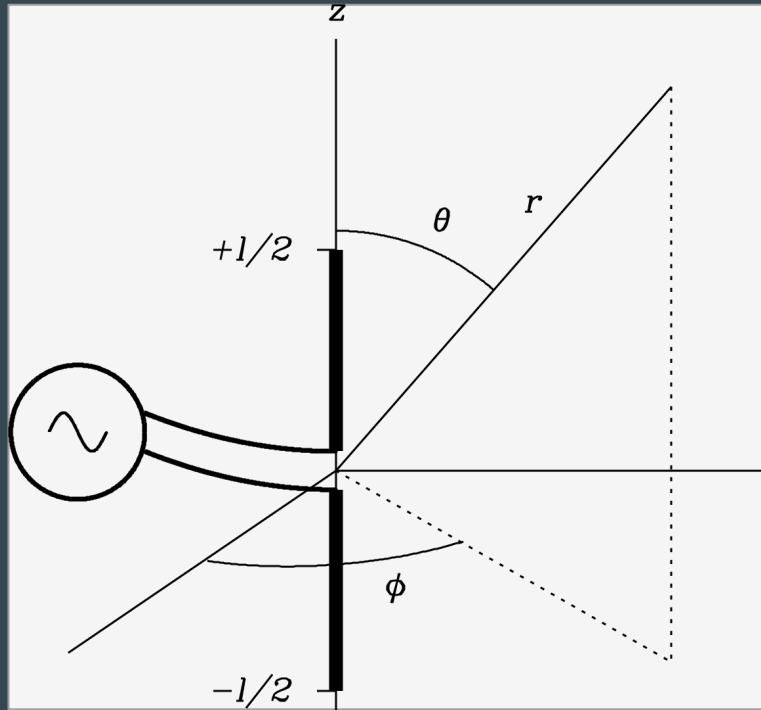
half-wave dipole: $L = \frac{\lambda}{2}$



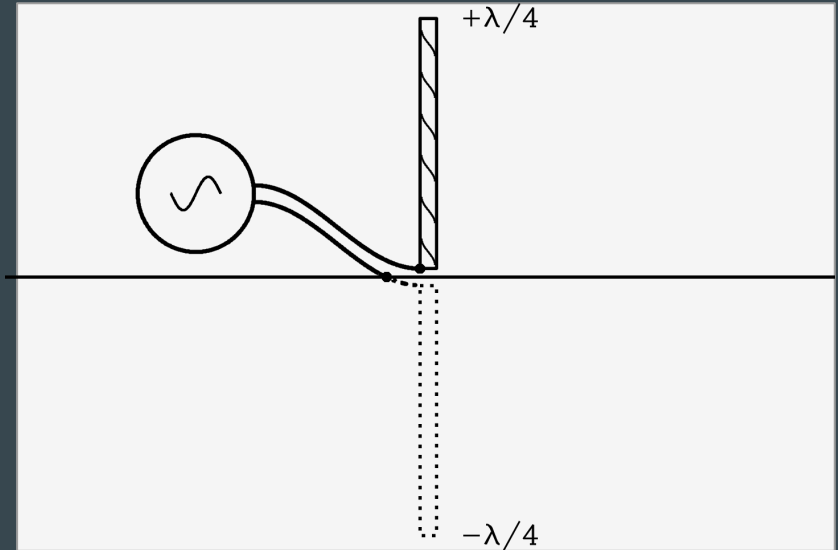
Standing Waves



Half-Wave Dipole Antenna



Ground-Plane Dipole Antenna

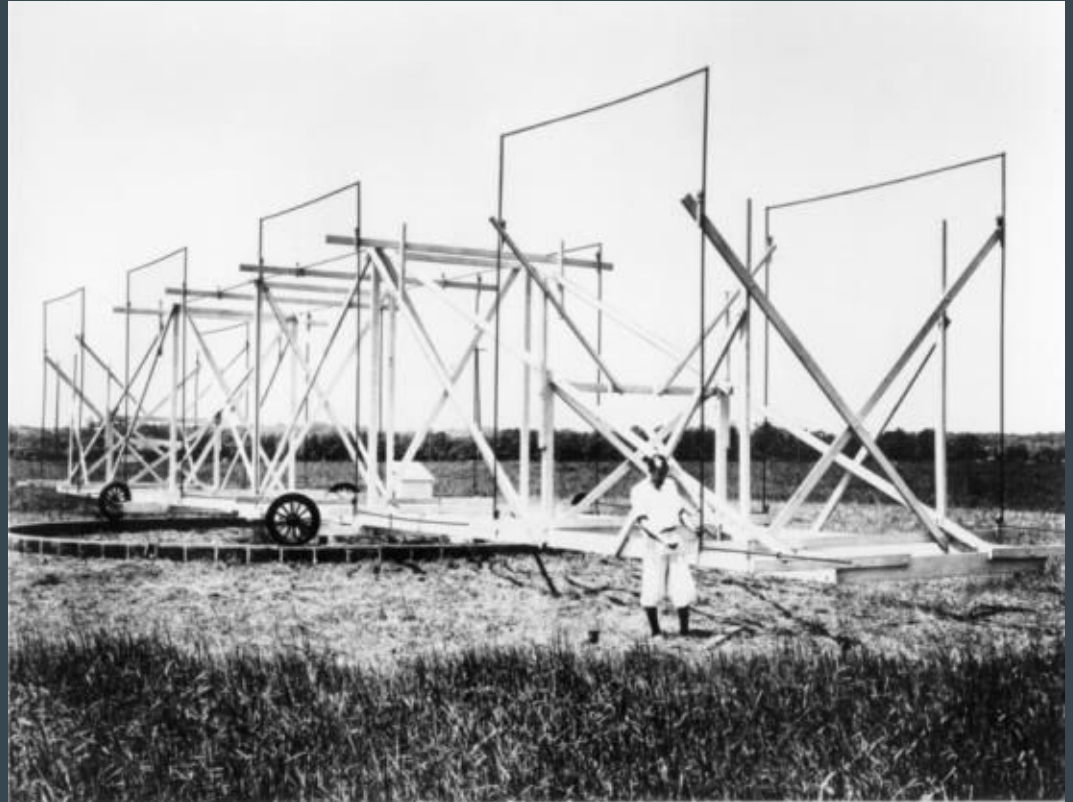


Karl Jansky's Radio Telescope (1932)

Bell Telephone Laboratories

Karl Jansky discovered “Electrical disturbances of apparently extraterrestrial origin” at 20 MHz – first evidence of astrophysical radio waves!

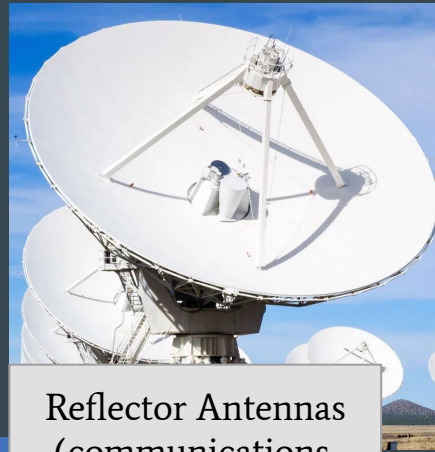
Unit of flux density: **Jansky (Jy)**



The Antenna Family



Horn Antennas
(radar)



Reflector Antennas
(communications,
astronomy)



Wide Band Antennas
(adjustable
wavelength range)



Loop Antennas
(direction finders,
radio receivers)



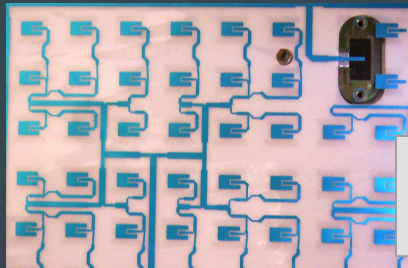
Yagi Antennas
(VLF, LF)



Helical antennas
(weather, GPS,
astronomy)



Lens antennas
(mm-wavelengths)



Patch, Microstrip Antennas
(cell phones)

3.4

Dish - reflects & focuses radio waves towards the antenna

↳ Bigger dish = higher sensitivity
= higher resolution

↳ Antenna capacitance - capacitive of resistor dissipating some power output by antenna

Redman's Equation: $\sigma_T \approx \frac{T_{\text{ant}} + T_{\text{rx}} + T_{\text{sys}}}{\sqrt{2 \times BW \times t_s}}$

↑ noise temperature ↑ range of frequency ↑ sampling time

→ minimum signal we can detect



(antenna pattern)



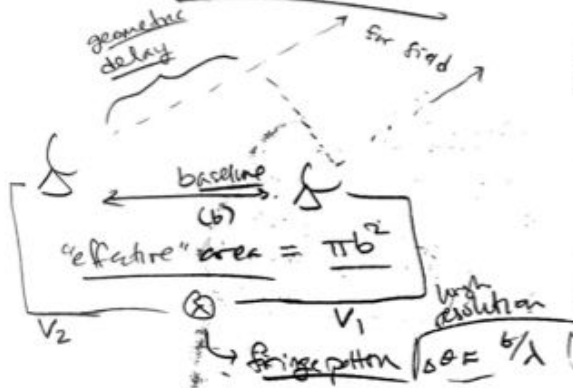
Interferometer - 2 or more radio antennas combined to increase the area

↳ cross correlation - multiply and average signals from 2 antennas

↳ interferometer sensitivity for N antennas:

$$\sigma_T = \frac{T_{\text{ant}} + T_{\text{rx}} + T_{\text{sys}}}{\sqrt{N(N-1) \Delta V t_s}}$$

large N = low σ_T = high sensitivity



Single-Dish Telescopes

305 Meter Arecibo Telescope
(Arecibo, Puerto Rico)



Five-Hundred-Meter Aperture
Spherical Telescope (FAST;
Guizhou, China)



Parkes Murriyang 64 Meter
Telescope (Parkes Australia)



Green Bank 100 Meter Telescope
(Green Bank, West Virginia)

Fringe patterns

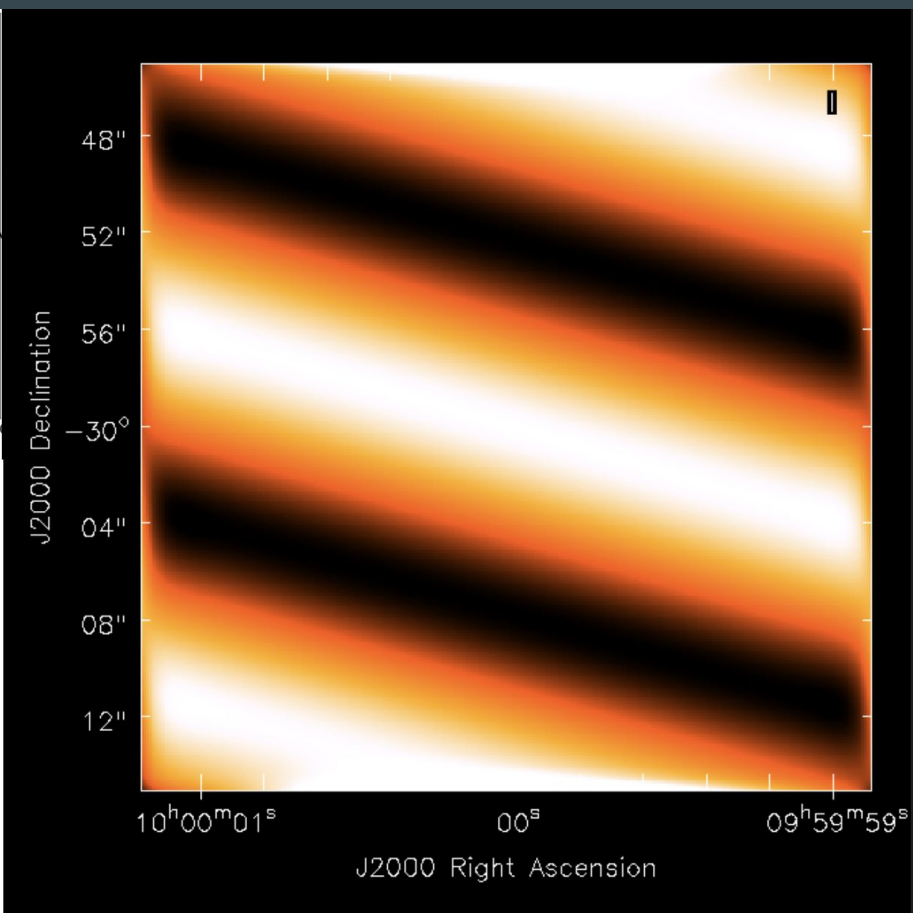
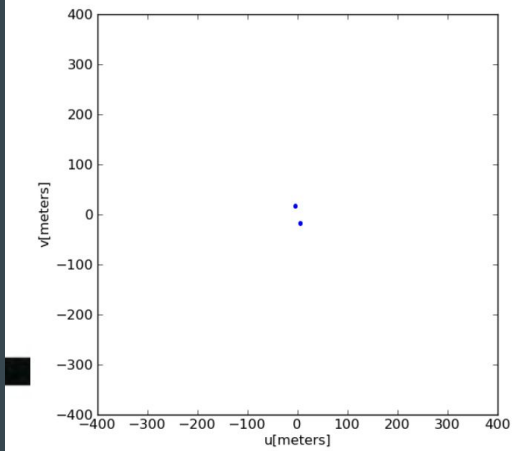
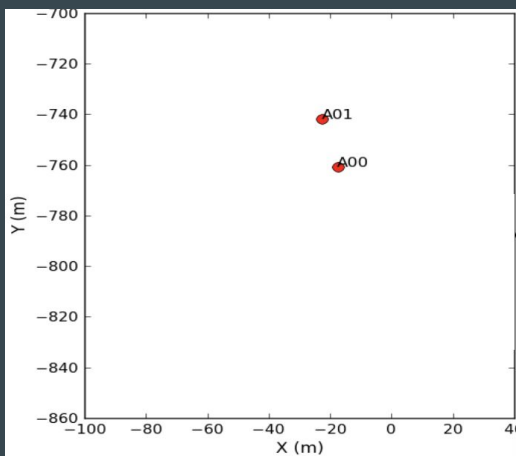
NRAO

Introduction to
Radio

Astronomy –

Cassie Reuter:

https://science.nrao.edu/facilities/atma/naasc-works-hops/nrao-cd-northernwestern19/Interferometry_Basics.pdf



Fringe patterns

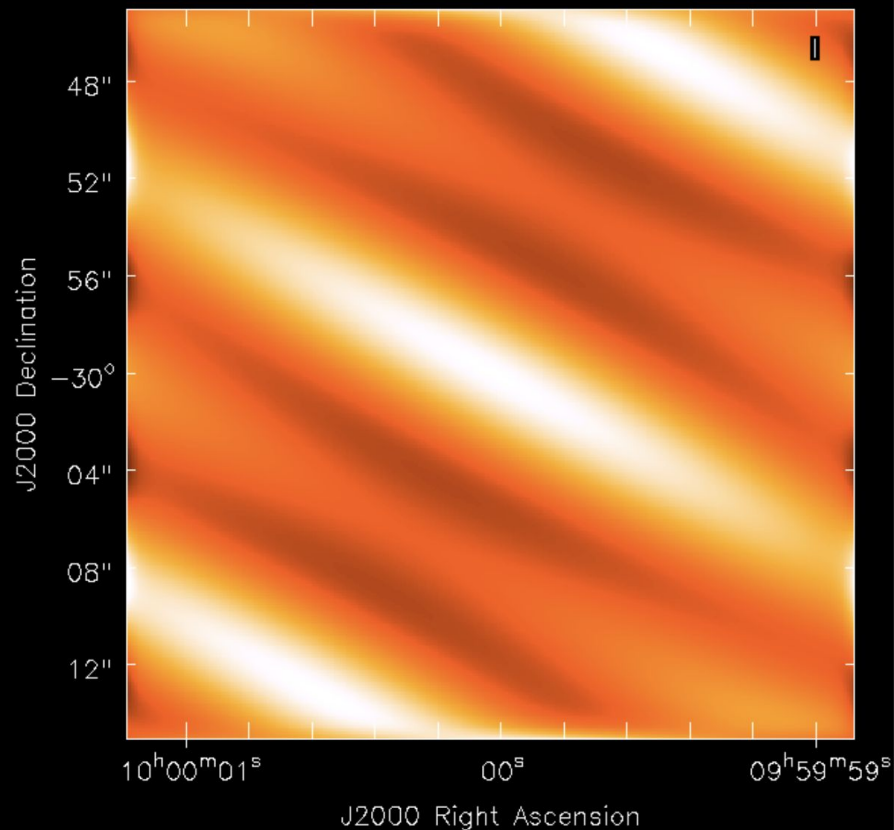
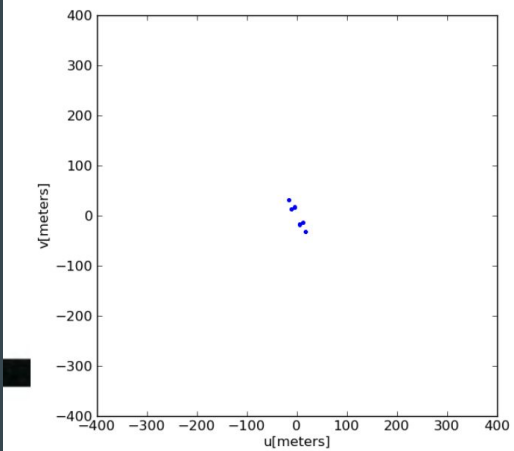
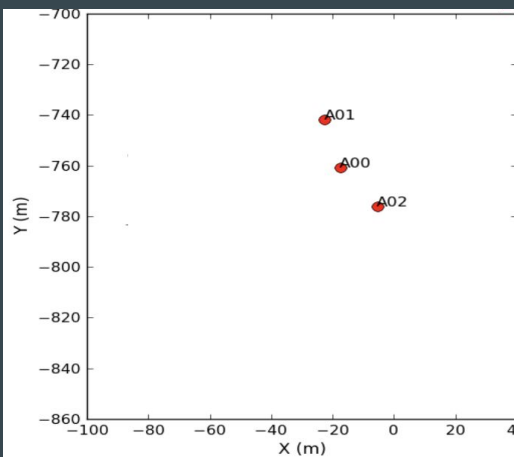
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Fringe patterns

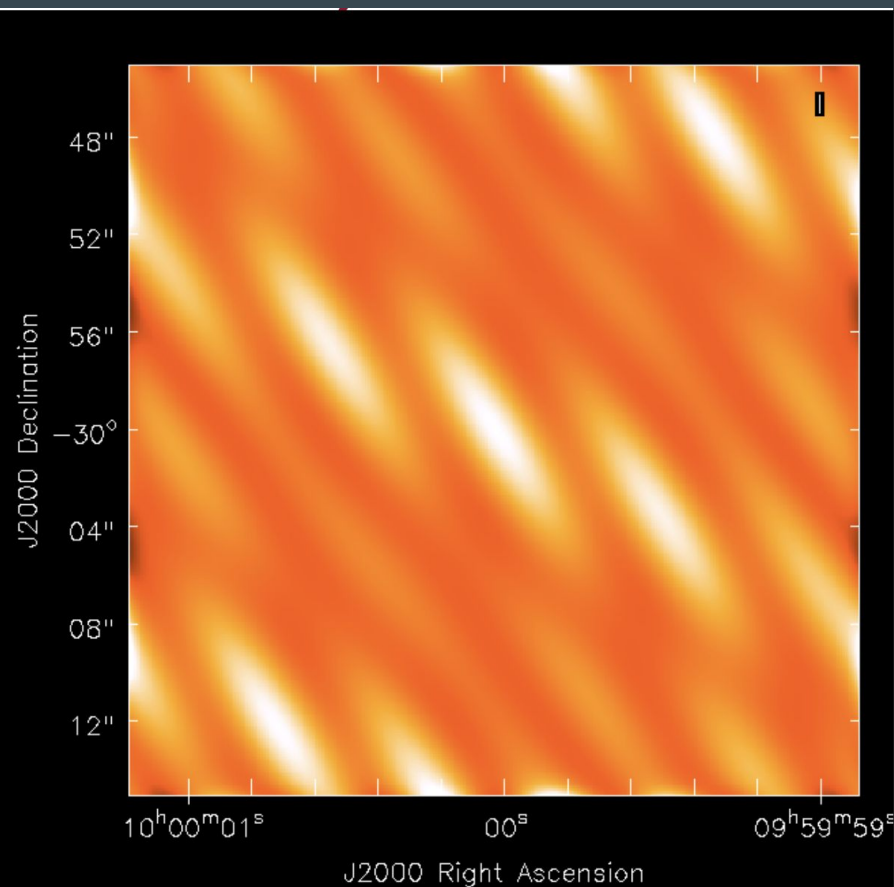
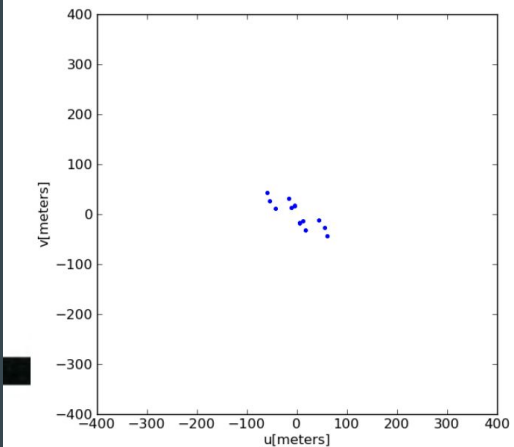
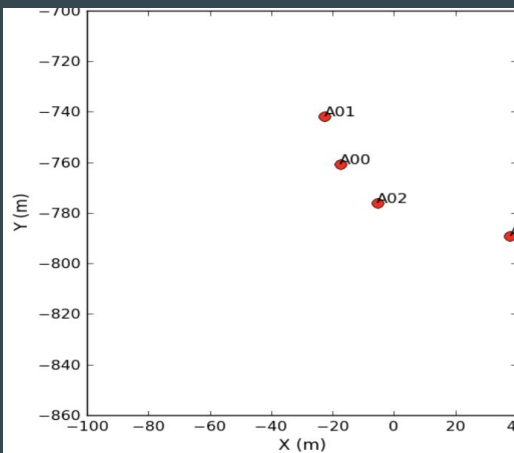
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Fringe patterns

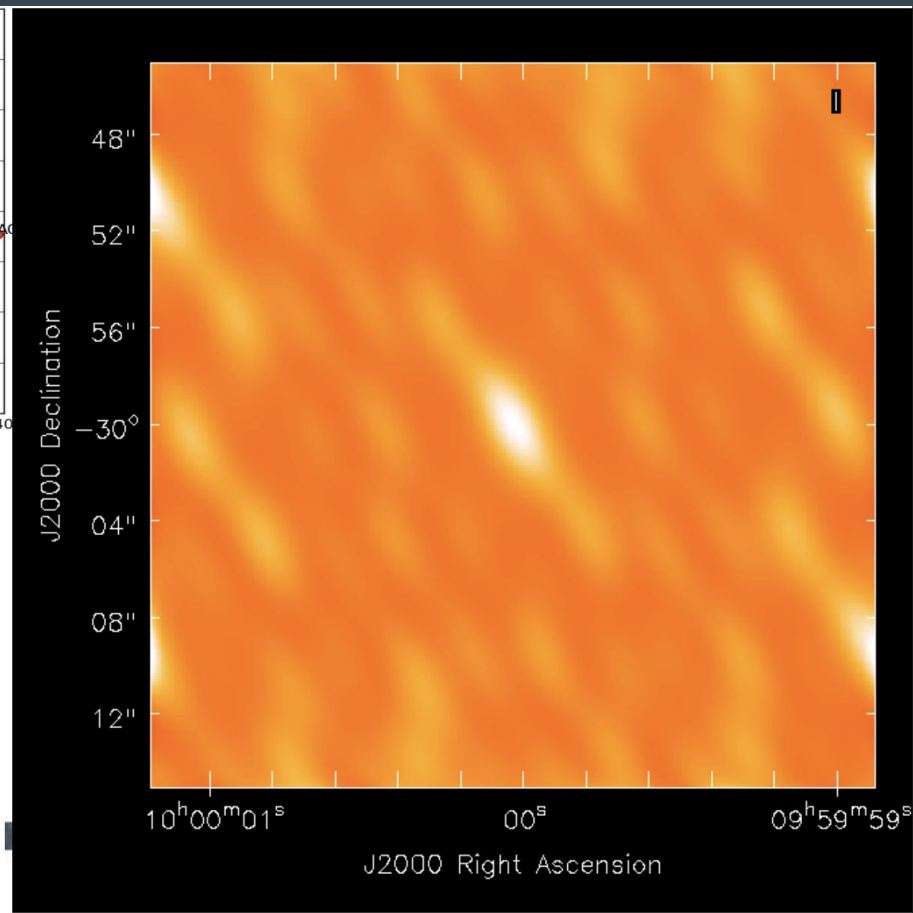
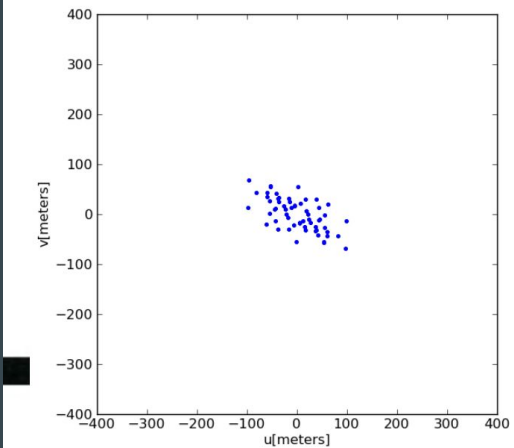
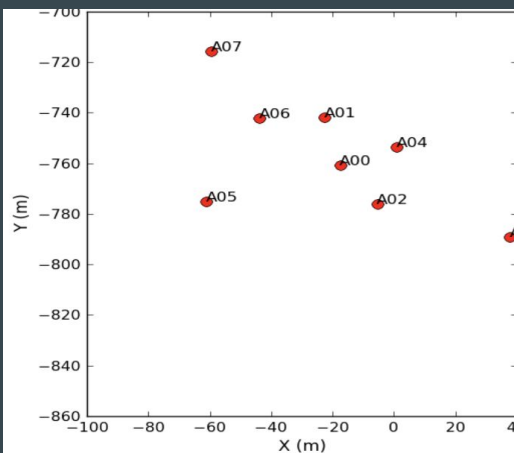
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Fringe patterns

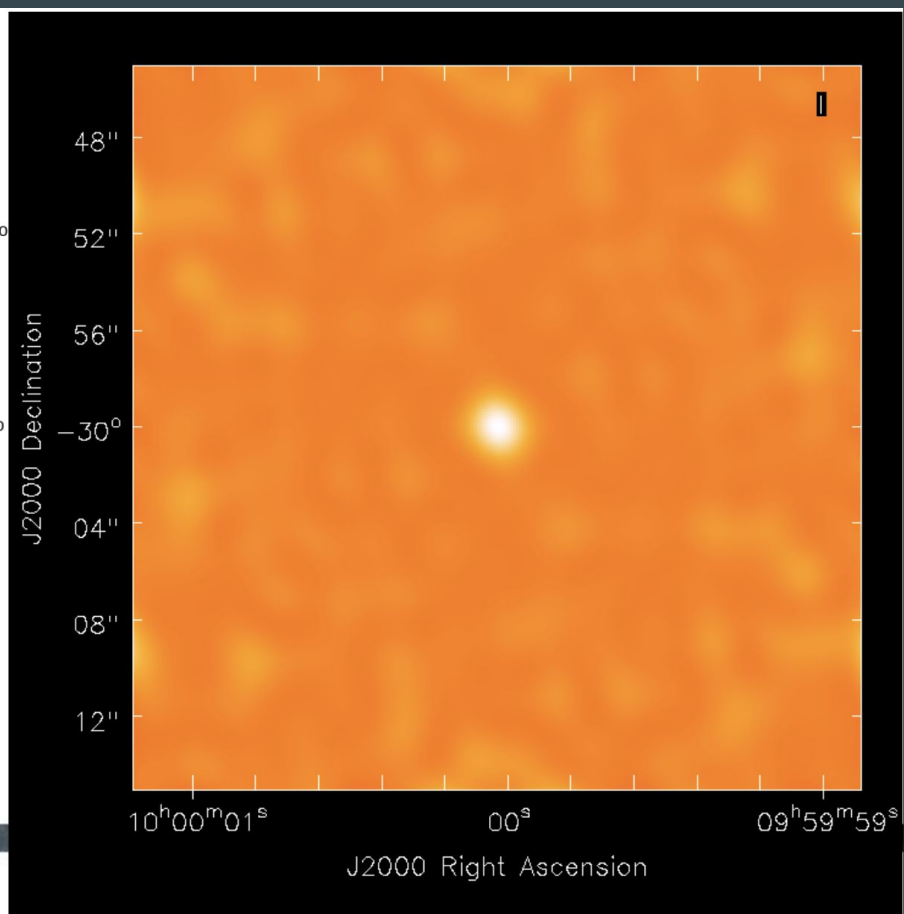
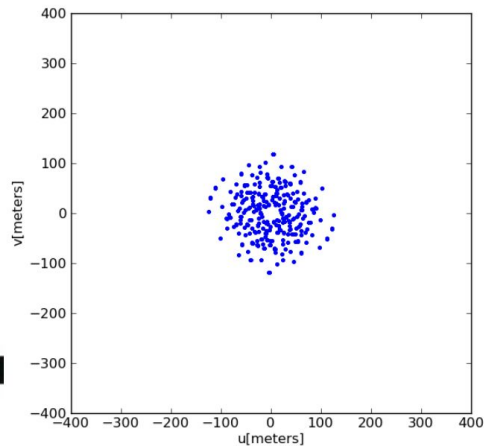
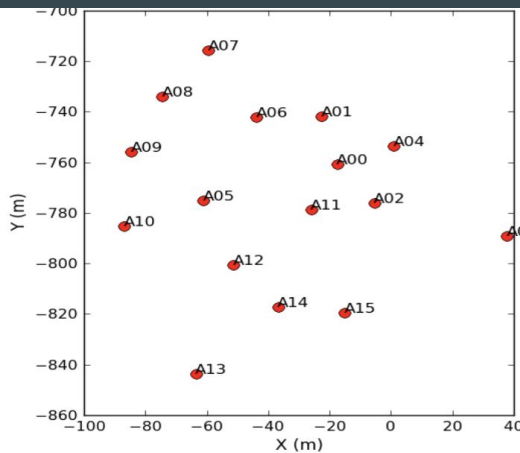
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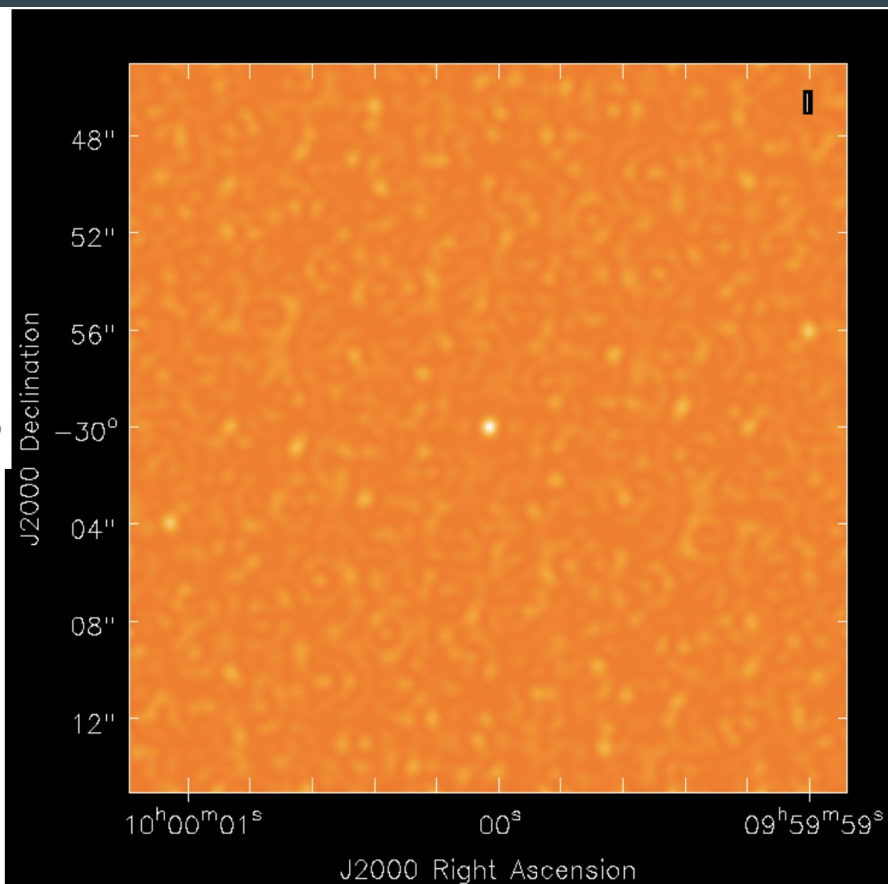
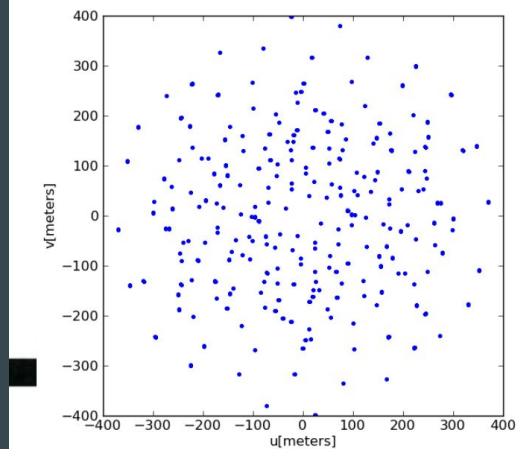
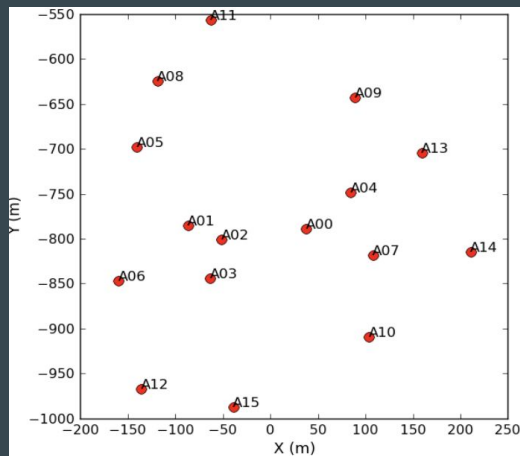
Cassie Reuter:

https://science.nrao.edu/facilities/alma/naasc-works-hops/nrao-cd-northernwestern19/Interferometry_Basics.pdf



Fringe patterns

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https://science.nrao.edu/facilities/atma/naasc-works-hops/nrao-cd-northernwestern19/Interferometry_Basics.pdf



Demo: Let's experiment with our own miniature interferometer!

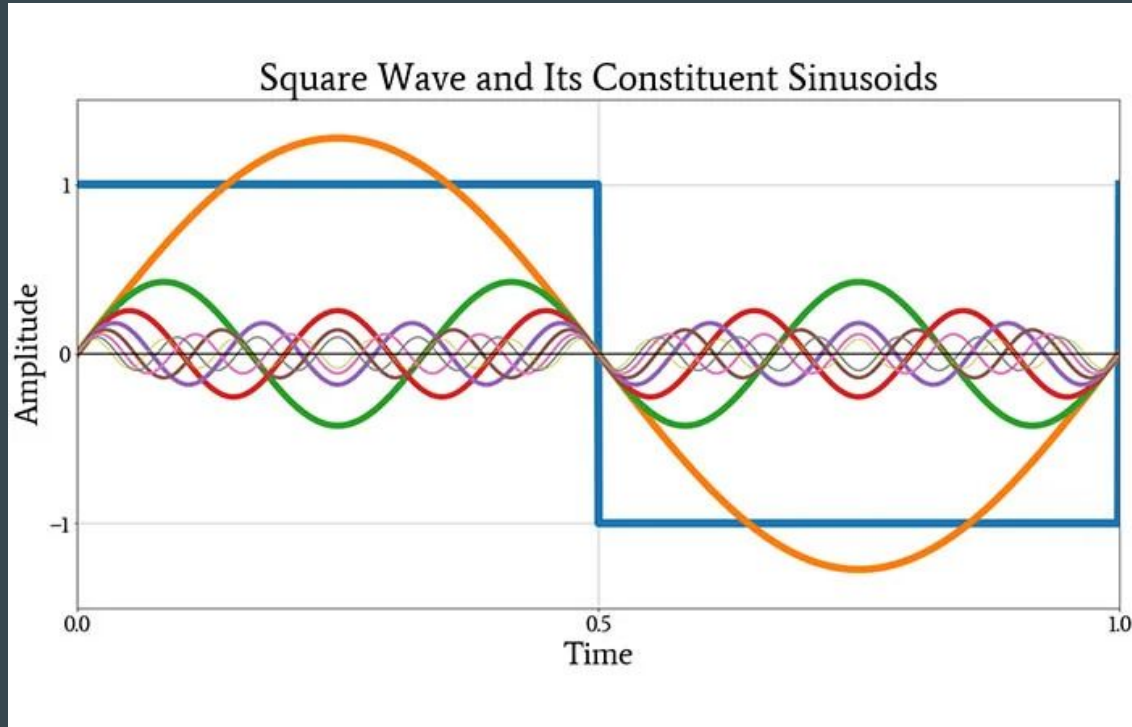
What happens when we add/remove components of the interferometer?

What allows us to build such a small optical interferometer, while radio interferometers can span hundreds of miles?

Fourier Representation of Signals

Any real signal can be represented by a sum of sinusoids with **fourier amplitudes** →

Any **complex** signal can be represented by a sum of complex exponentials with **fourier amplitudes**



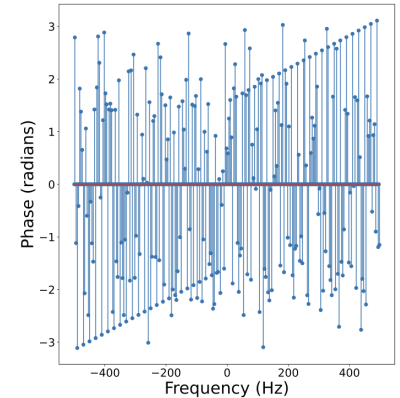
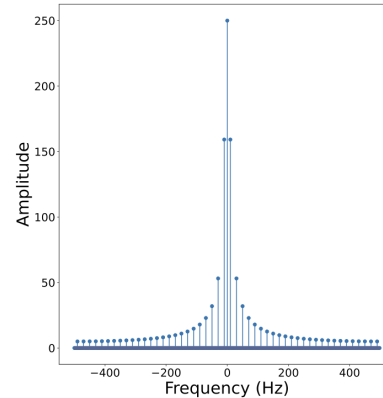
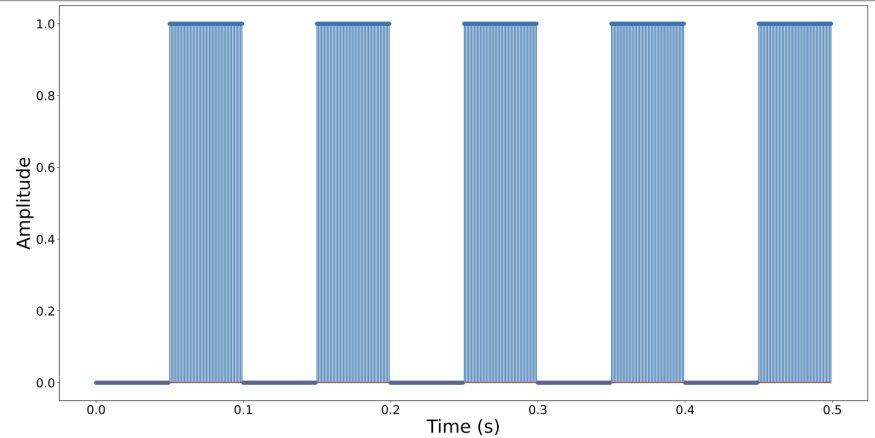
Fourier Representation of Signals

Discrete Fourier Transform
converts time domain signal to
fourier domain (frequency)
representation:

$$\text{DFT: } F[k] = \sum f[x] e^{-2\pi i k x / N}$$

$$\text{iDFT: } f[x] = (1/N) \sum F[k] e^{2\pi i k x / N}$$

Fast Fourier transform is an
algorithm to compute the
DTFT quickly and efficiently

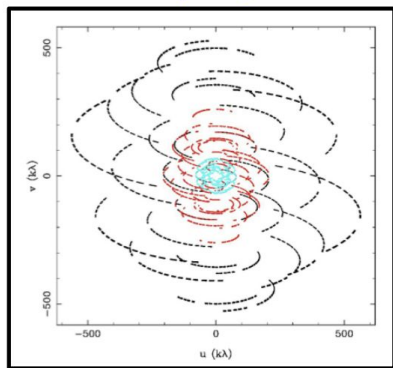


Radio Imaging

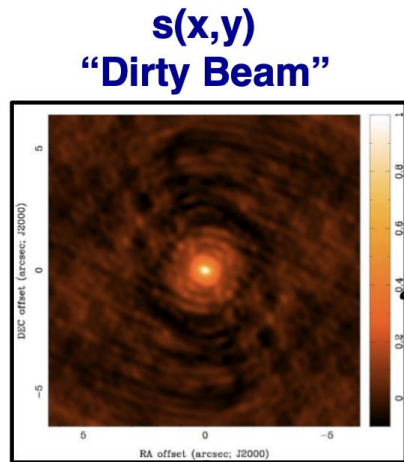
Stages of Imaging:

1. Grid to UV plane
2. FFT
3. “Clean”
(convolve with PSF)

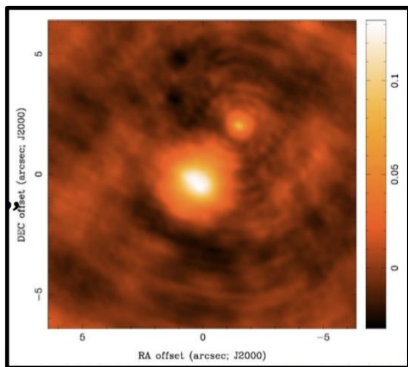
The Dirty Beam



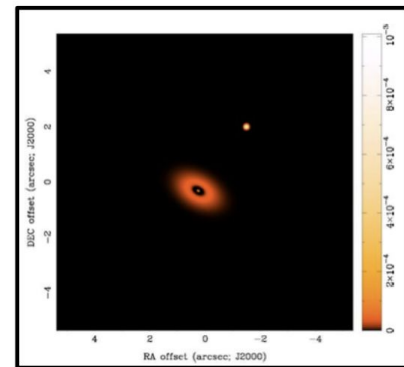
FT →



*(Convolution)



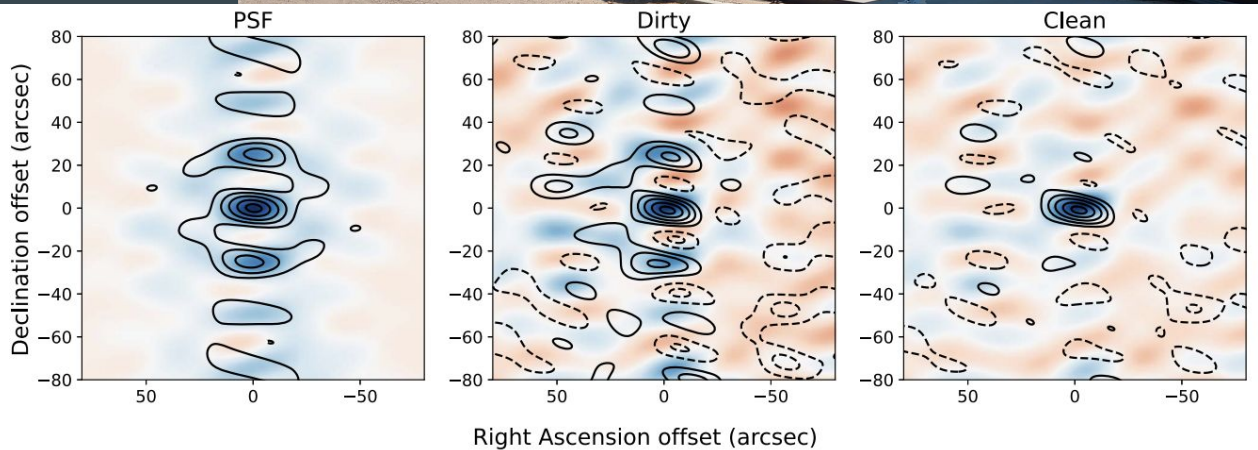
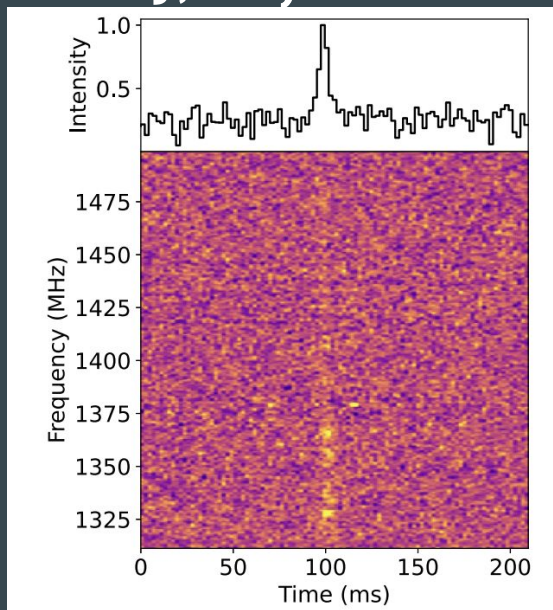
←



$T_D(x,y)$
“Dirty Image”

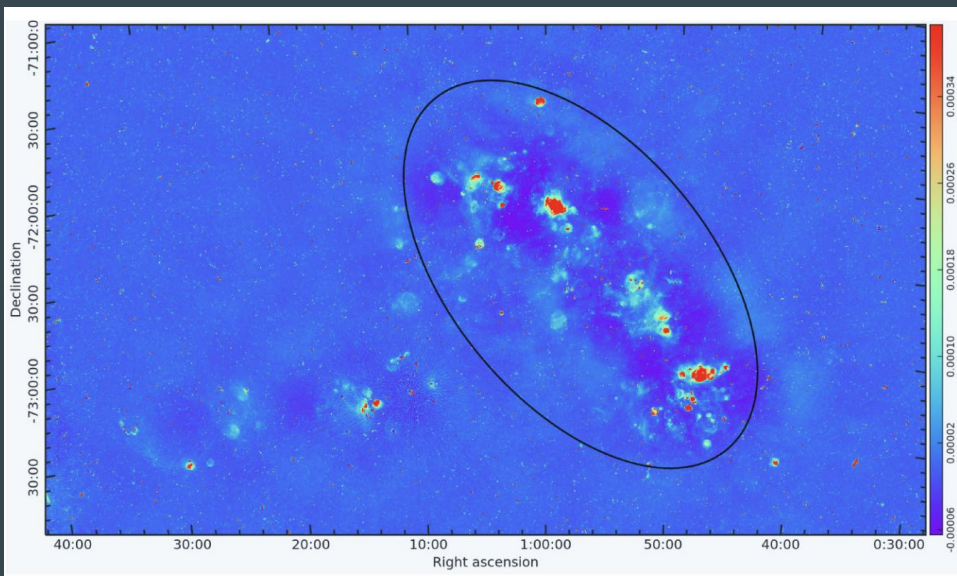
$T(x,y)$

Examples: DSA-110 (97x10 meter antennas, Owens Valley, CA)

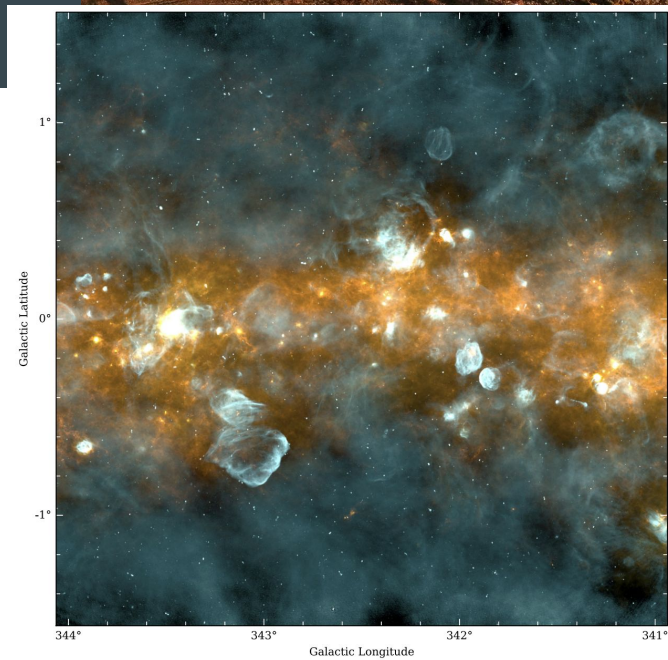


Fast Radio Burst (FRB) detected and localized by the DSA-110 (Ravi et al., 2023)

Examples: MeerKAT (64x13.5 meter antennas, South Africa)



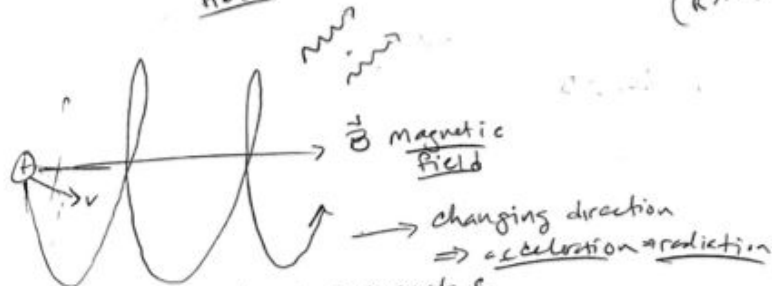
Radio Image of the Small Magellanic Cloud (Cotton et al., 2024)



IR + Radio Image of Galactic Plane (Goedhart et al., 2024)

3.7 |

Radiation - electromagnetic waves from an accelerating charged particle detectable in the far field



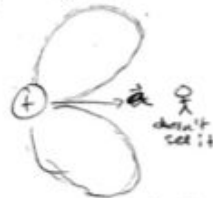
a charged particle in a magnetic field moves in a helix

Cyclotron radiation

charged particle in \vec{B} field moves non-relativistically ($v \ll c$)

$$v_c = \frac{qB}{2\pi m}$$

$$P = \frac{2}{3} \frac{q^2 a^2}{c^3}$$



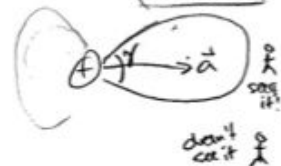
Synchrotron radiation

charged particle in \vec{B} field moves relativistically ($v \approx c$)

$$v_s = \frac{qB}{2\pi \gamma m}$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

relativistic factor



Incoherent radiation - N particles radiate separately relativistic boost

$$P_{total} = N \times P$$

coherent radiation - N particles radiate together

$$P_{total} = N^2 \times P$$

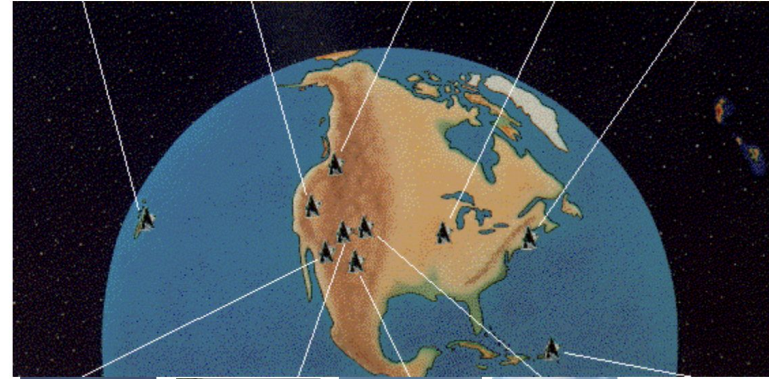
observe radiation on astronomical scales

$$P = \frac{2}{3} \frac{q^2 a^2}{c^3} \gamma^2$$

coherent boost

Very-Long Baseline Interferometry (VLBI)

Combines data from antennas around the world (maximum baselines ~1000 km) to achieve high angular resolution (~milliarcseconds)



Very Long Baseline Array (VLBA)

Tracking Active Galactic Nuclei with Austral Milliarcsecond Interferometry (TANAMI) Array

Example: Event Horizon Telescope (EHT)

1.3 mm Images of the Black Hole M87 in the Andromeda Galaxy (EHT Collab. 2017)

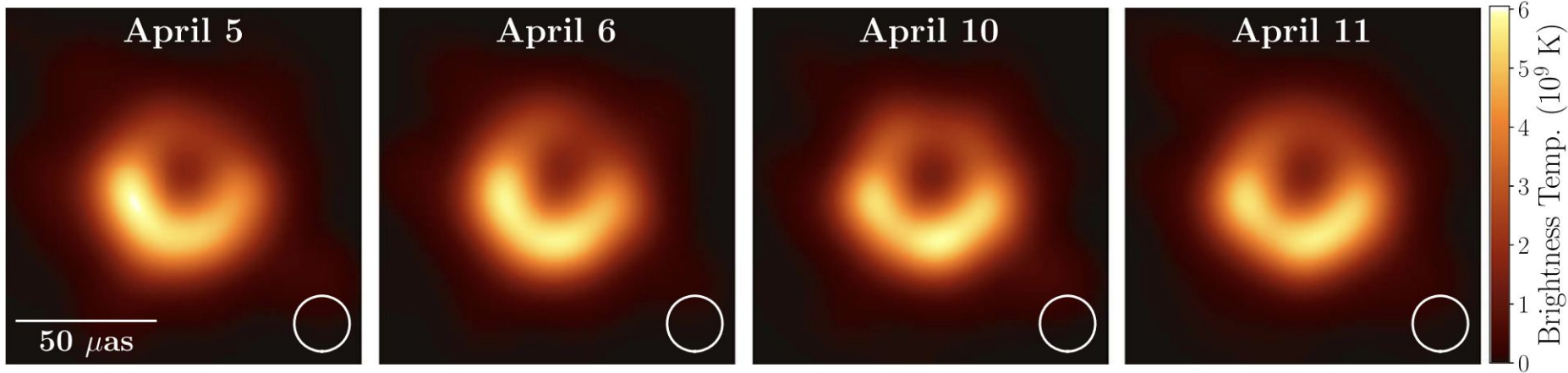


Figure 15. Averages of the three fiducial images of M87 for each of the four observed days after restoring each to an equivalent resolution, as in Figure 14. The indicated beam is $20 \mu\text{as}$ (i.e., that of DIFMAP, which is always the largest of the three individual beams).

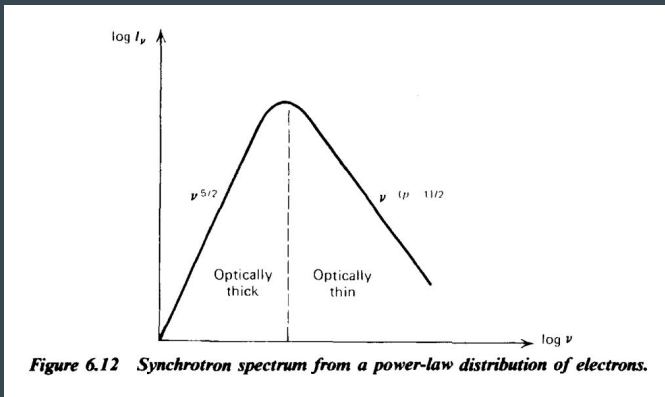
Think-Pair-Share

Compare and contrast the properties of single-dish antennas and interferometers.

Why don't we use interferometry in other areas of astronomy? E.g. why don't we have optical or x-ray interferometers?

ISM Cyclotron and Synchrotron Radiation

Free electrons moving in the magnetized, ionized ISM produce radiation emission in dense regions



Synchrotron radiation comes from charges moving relativistically

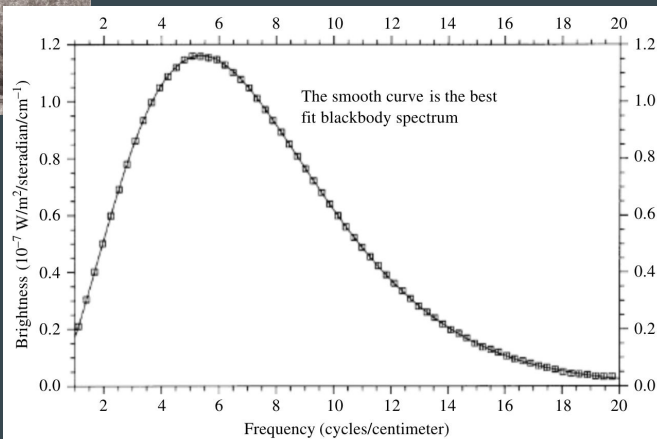
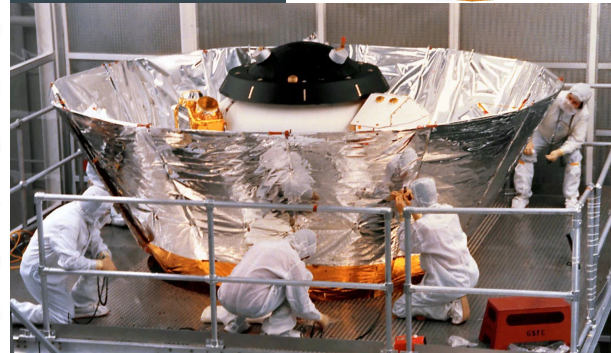
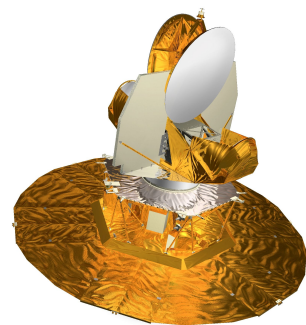
Cyclotron radiation comes from charges moving non-relativistically



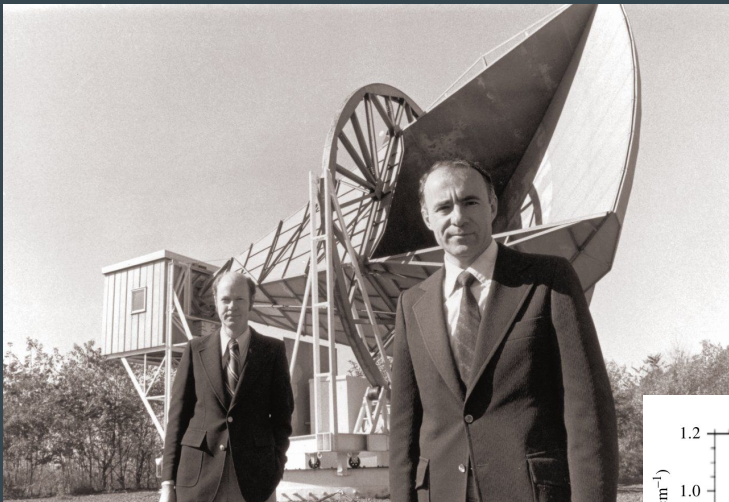
Cosmic Microwave Background (CMB)

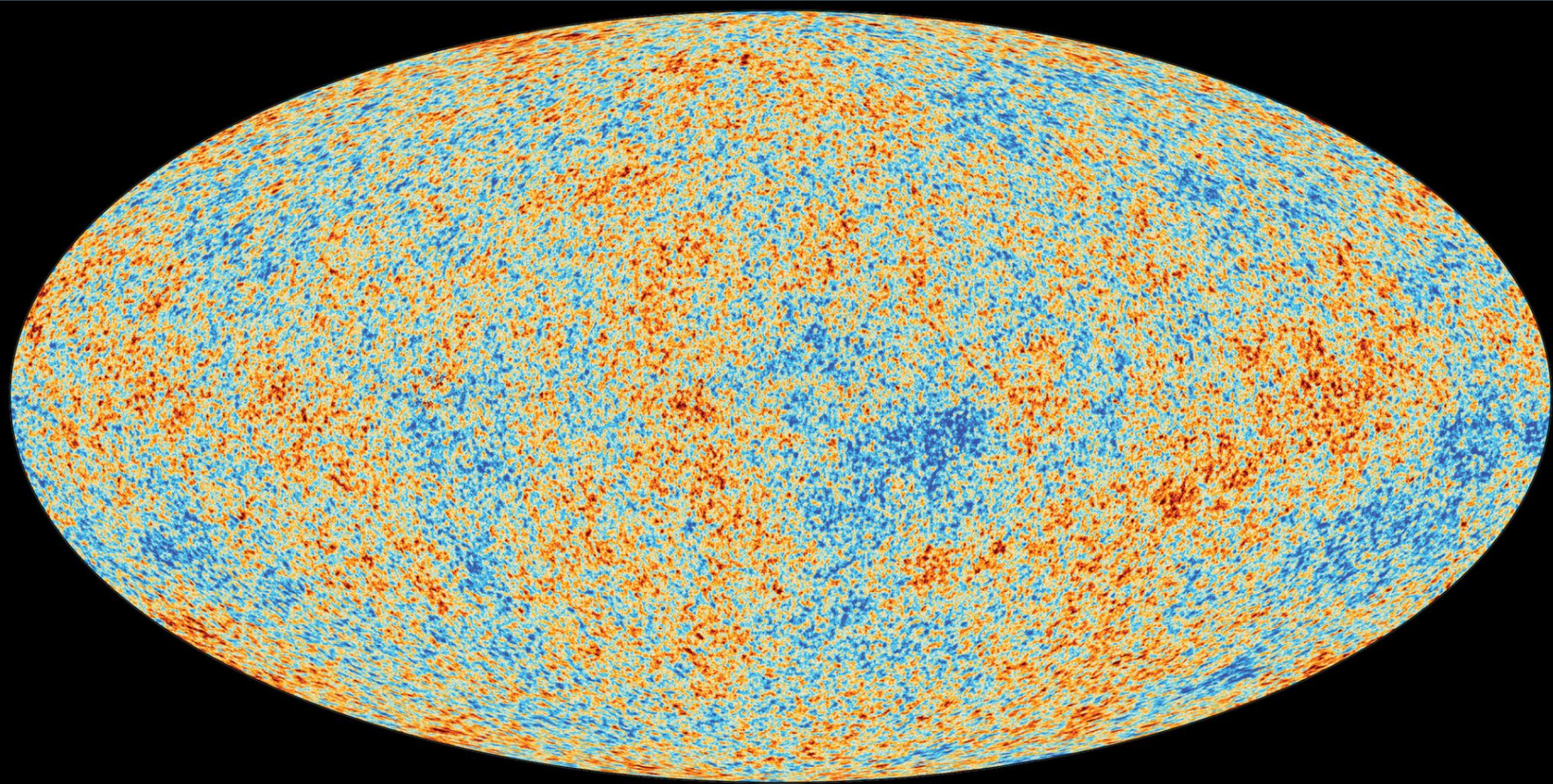
2.725 K Blackbody radiation from dense, early universe in thermal equilibrium

The COsmic Background Explorer (COBE), Wilkinson Microwave Anisotropy Probe (WMAP) and the Max Planck Telescope characterized the CMB with Microwave and IR detectors



Arno Penzias and Robert Wilson at the Holmdel Horn Antenna used to detect the noise temperature of the CMB (Penzias & Wilson 1967)



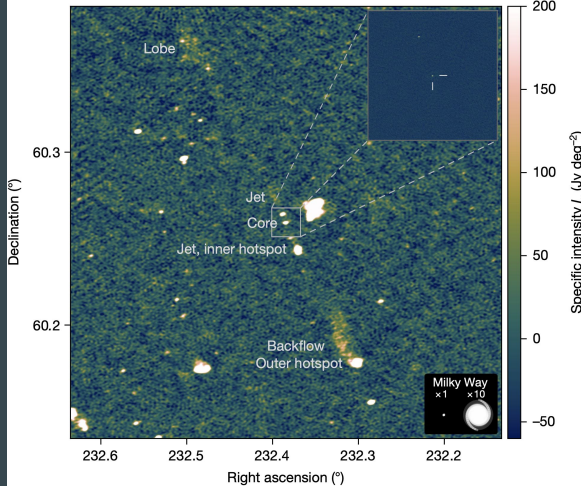


Supermassive Black Hole (SMBH) Jets

Active Galactic Nuclei - Matter falling gravitationally into SMBH at center of galaxy creates a radio-loud **accretion disk**

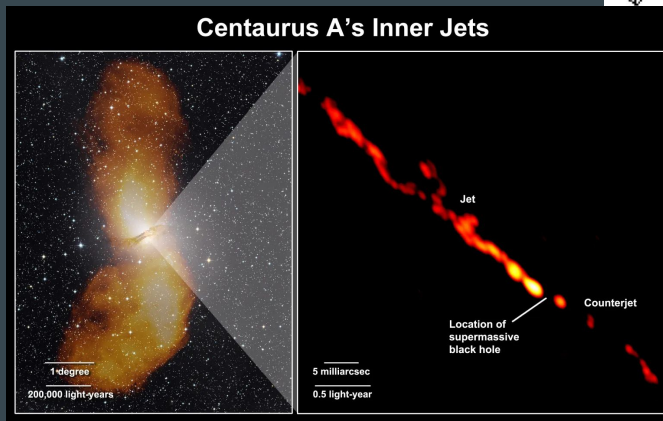
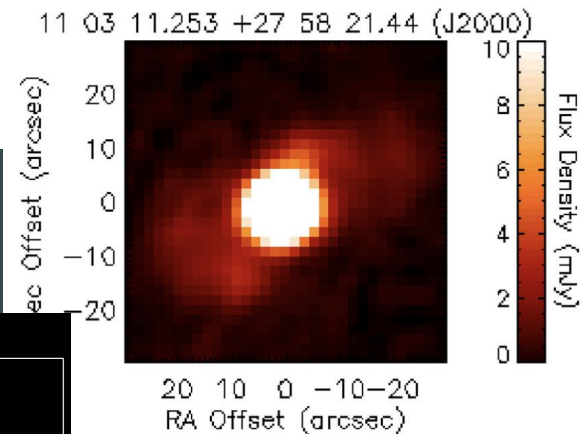
Magnetic field of the black hole can collimate matter into a powerful **jet** of relativistic charges radiating coherently in **radio, X-rays and gamma rays**

Jet can also form turbulent **shocks** with surrounding matter that generates synchrotron emission



Largest Known (7 Mpc) Radio Jet at $\lambda=1.02$ m from the Porphyriion SMBH Detected by the International LOw Frequency ARray (LOFAR) Telescope (ILT; Oei et al., 2024)

VLBA image of an AGN at the center of a spiral galaxy at $\lambda=20$ cm (Kaviraj et al., 2015)



Radio shock fronts (left) and radio jet (right) from SMBH at center of Centaurus A galaxy at 8.4 GHz (Müller et al., 2014)

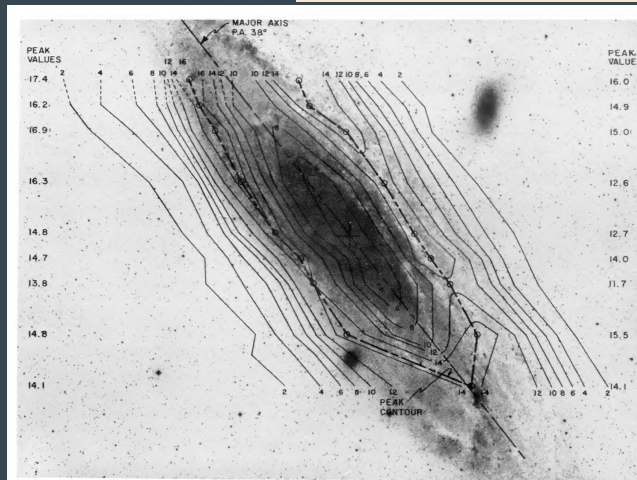
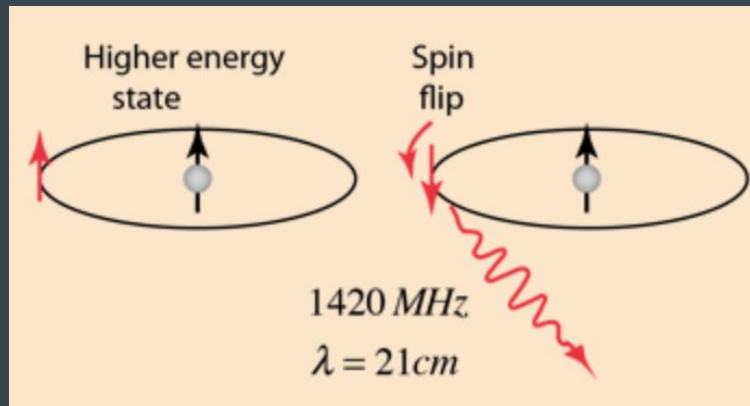
21 cm Hyperfine Hydrogen Spin-Flip Emission Line

Spin: quantum mechanical property of particles

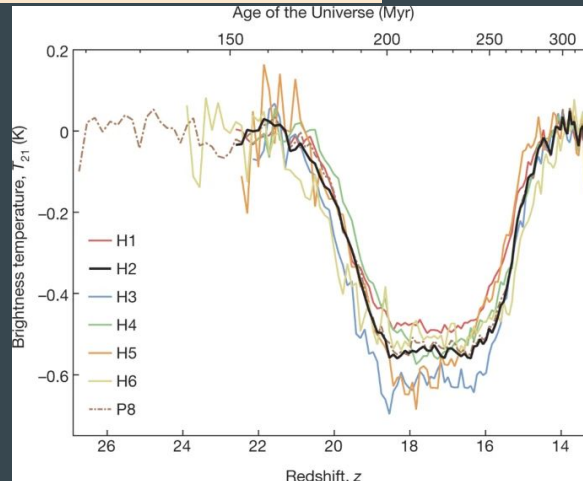
- **fermions** (e.g. electrons, positrons) - spin- $\frac{1}{2}$ particles which can have $s=\pm\frac{1}{2}$
- **bosons** (e.g. protons, neutrons) - spin-1 particles which can have $s=0,\pm 1$

21-cm transition - “hyperfine” transition of Hydrogen electron from $s=+\frac{1}{2}$ to $s=-\frac{1}{2}$

- **Primary tracer of star formation in galaxies**



High-resolution H-I absorption map of the Andromeda Galaxy from the GBT 100-m telescope (Roberts et al., 1966)



Possible detection of 21 cm Hydrogen line from early universe by EDGES Experiment (Bowman et al., 2018)

Think-Pair-Share

We mentioned that white dwarfs, neutron stars, and black holes have 'radio emission'; what do you think that means? Why do we not detect them on our car radios?

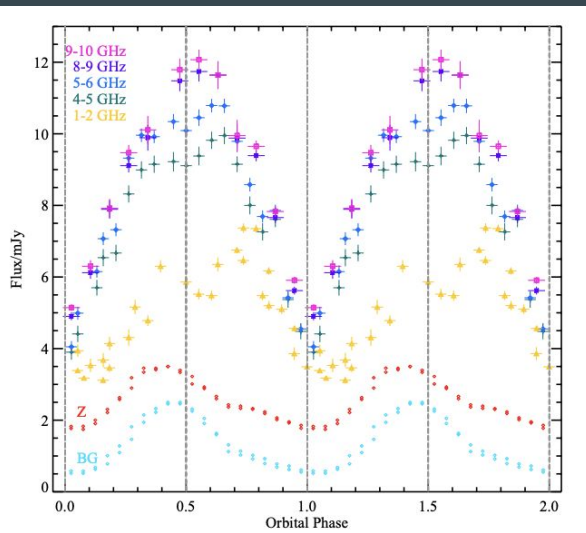
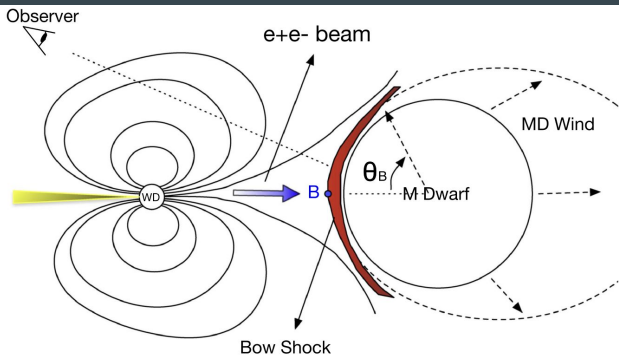
Demo: Let's explore the radio sky!

**What sounds different between the signals we play?
Do pulsars sound different than FRBs? From
magnetars?**

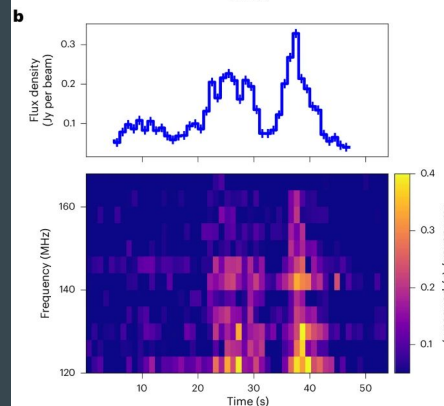
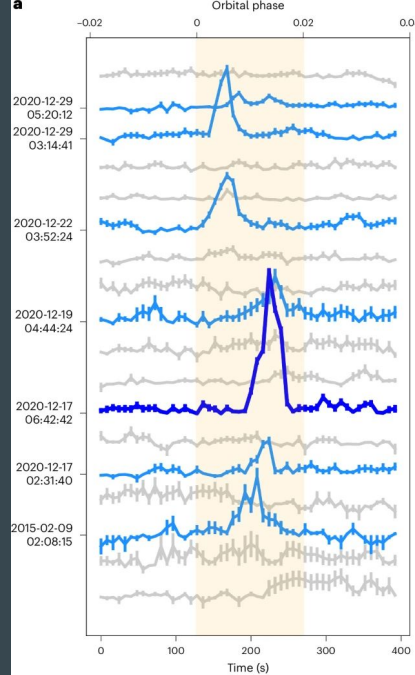
Polars (White Dwarf-M Dwarf Binaries)

Polars are White Dwarf - M Dwarf binaries which produce coherent, periodic radio emission by streaming charged particles between the stars' magnetic poles.

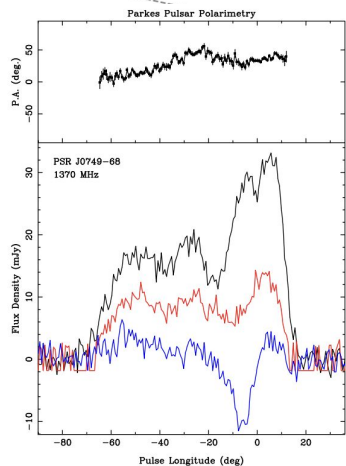
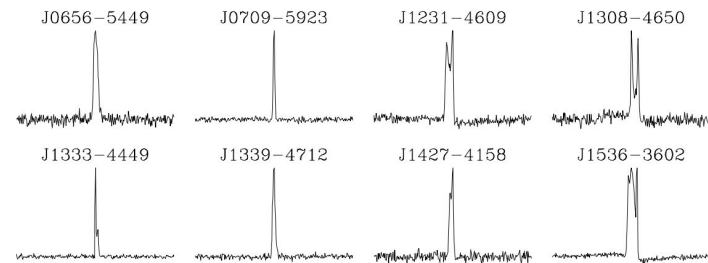
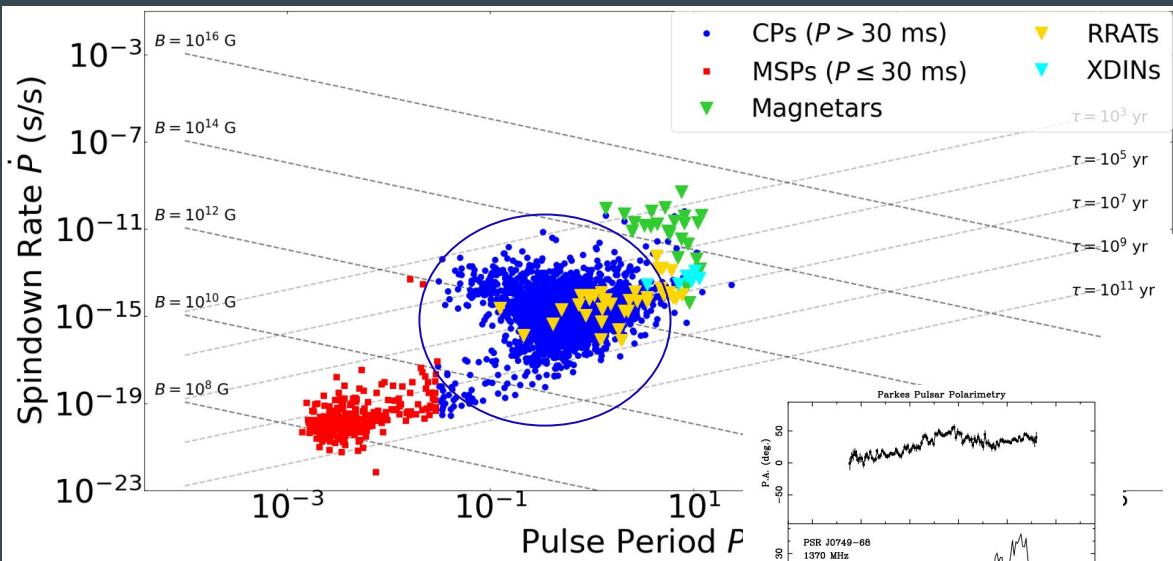
E.g. AR Scorpii produces radio emission at beat frequencies between the 3.6 hour orbital period and 1.95 rotation period (Geng et al., 2016; Stanway et al., 2018)



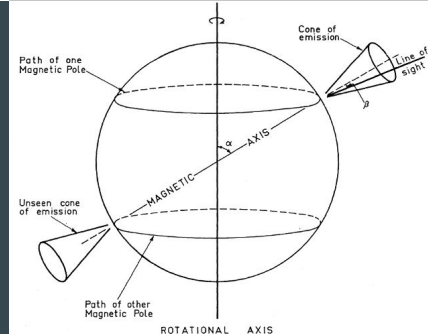
Long Period Radio Transients (LPTs or LPRTs) were discovered in 2022; at least 2 are intermediate polars with hour-scale periods, but are **magnetically locked**. E.g. ILT 1101+5521 has a 2-hour period suspected to be the orbital period (de Ruiter et al., 2025)



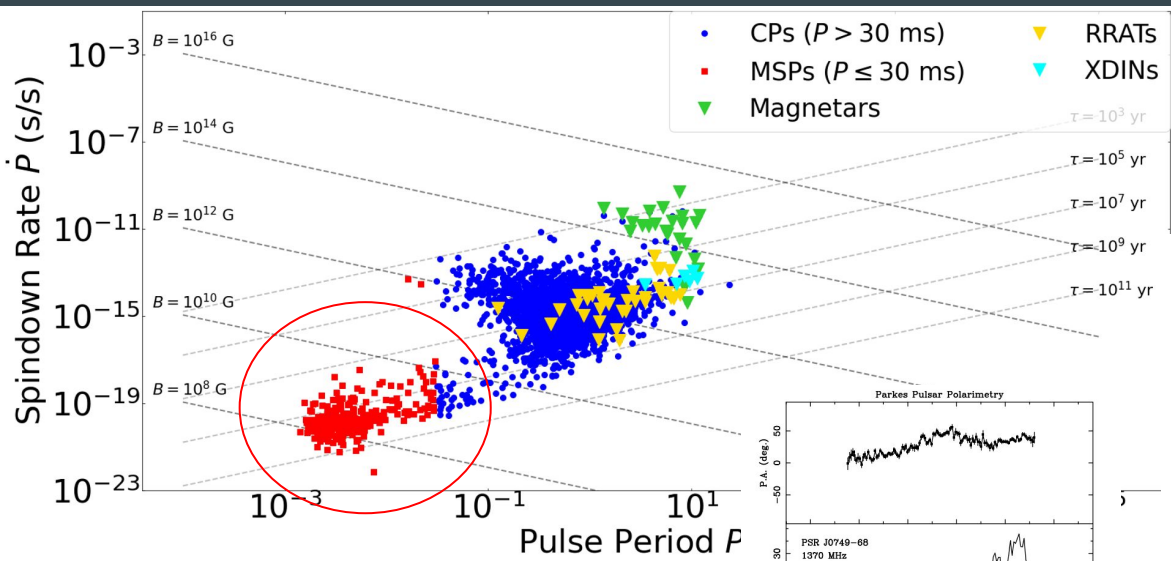
Neutron Stars: Pulsars, Radio Magnetars, RRATs, magnetars



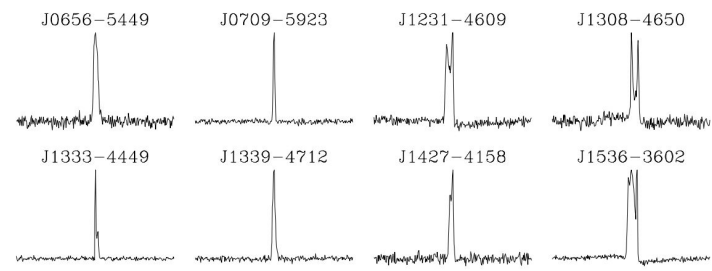
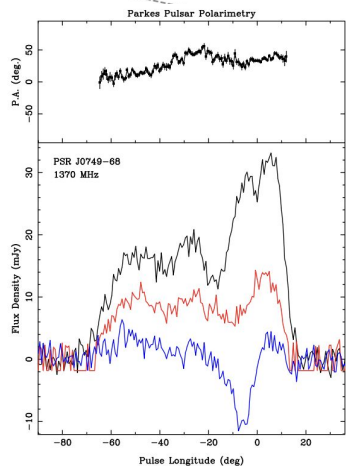
Slow Pulsars
(0.3-10 s): produce coherent radio emission from magnetic poles via charged particle 'avalanche'



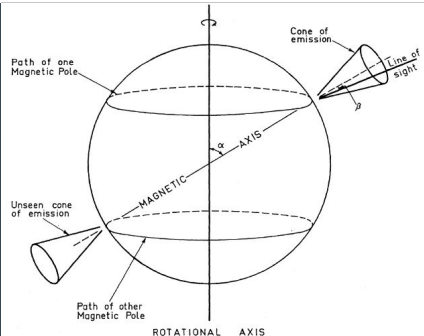
Neutron Stars: Pulsars, Radio Magnetars, RRATs, magnetars



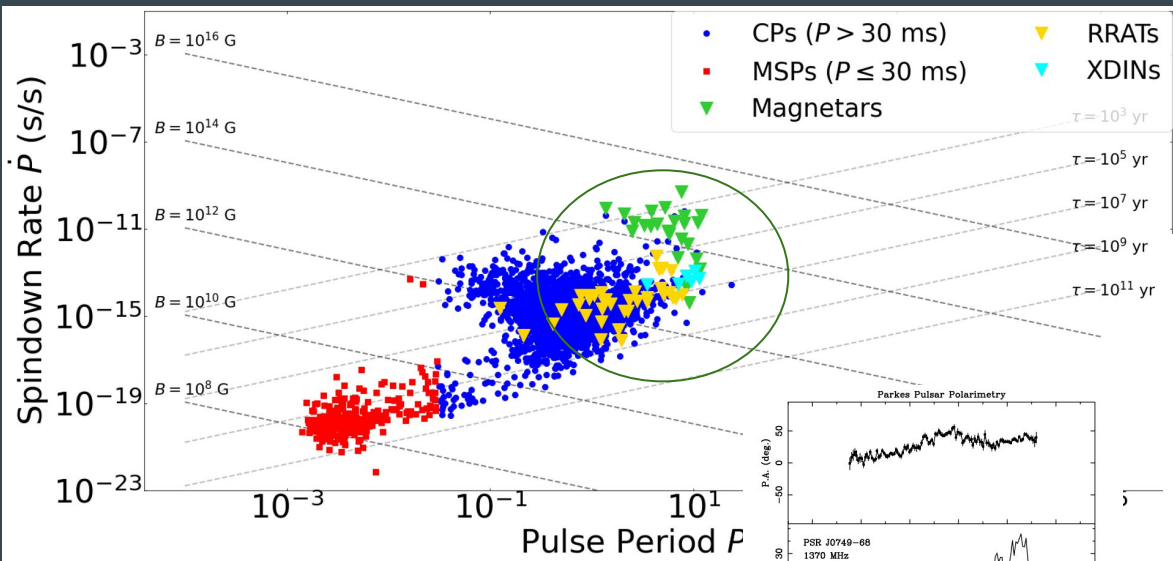
Millisecond Pulsars (<0.3 s):
initially lost their rotational energy,
then accreted from companion to
spin up to millisecond periods



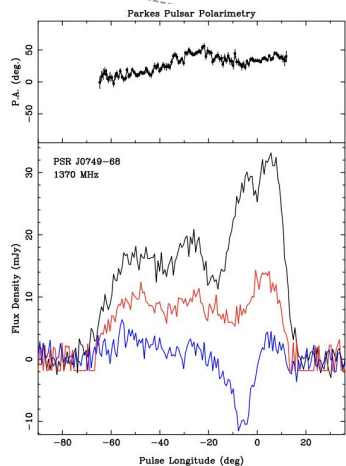
Slow Pulsars (0.3-10 s): produce coherent radio emission from magnetic poles via charged particle 'avalanche'



Neutron Stars: Pulsars, Radio Magnetars, RRATs, magnetars

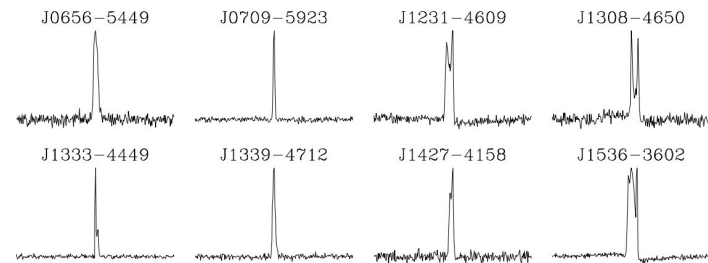


Millisecond Pulsars (<0.3 s):
initially lost their rotational energy,
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spin up to millisecond periods

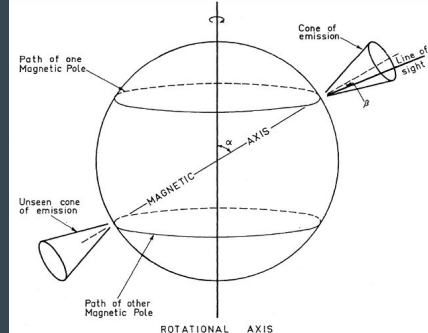


Rotating Radio Transients (RRATs):
only detectable through single pulses
because of irregular nulling

Magnetars (>2s): largest magnetic
fields, produce giant flares and pulses
that exceed rotational energy

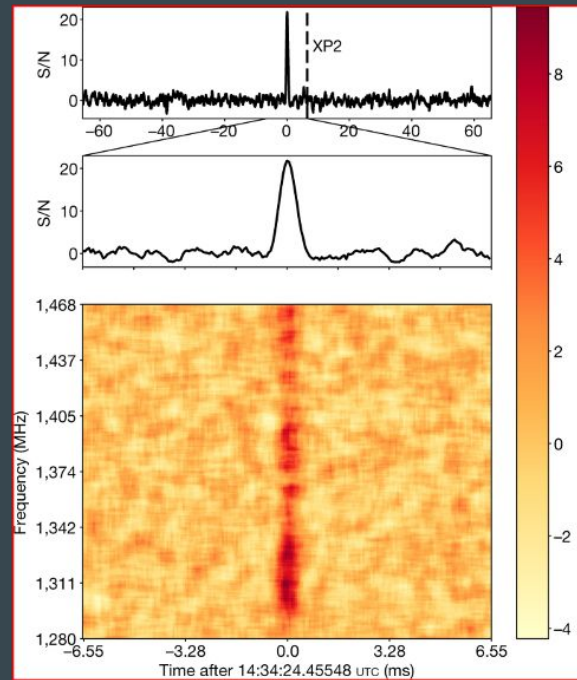
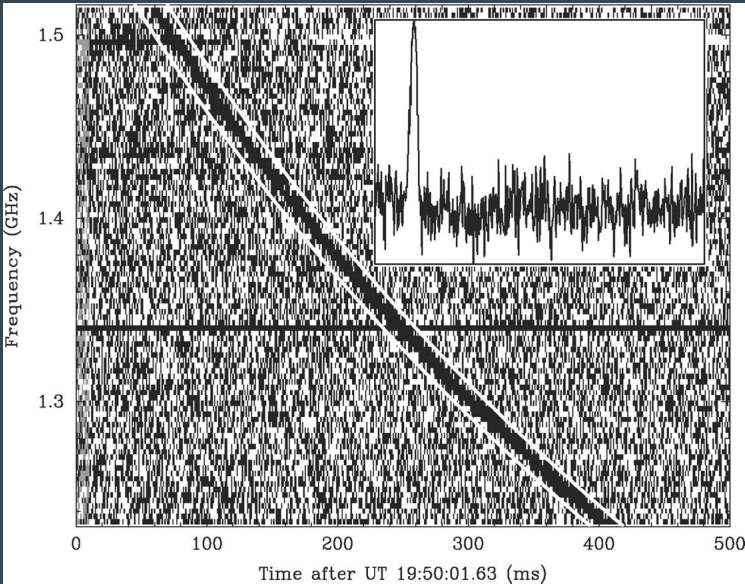


Slow Pulsars (0.3-10 s): produce
coherent radio
emission from
magnetic poles via
charged particle
'avalanche'



Fast Radio Bursts (FRBs)

Extragalactic radio bursts lasting <1ms with unknown source mechanism; leading candidates are magnetars



In 2020, an FRB-like burst was detected from a Galactic magnetar, **SGR J1935+54**, making magnetars the primary candidates (e.g. Bochenek et al., 2020)

First FRB (The Lorimer Burst), detected by the Parkes telescope, was determined extragalactic due to the large frequency-dependent **dispersive delay**

$$I\left(t + \frac{e^2 DM}{2\pi m_e c} (\nu_0^{-2} + \nu^{-2}), \nu\right)$$

At-Home Astronomy: Quick-look Radio Images

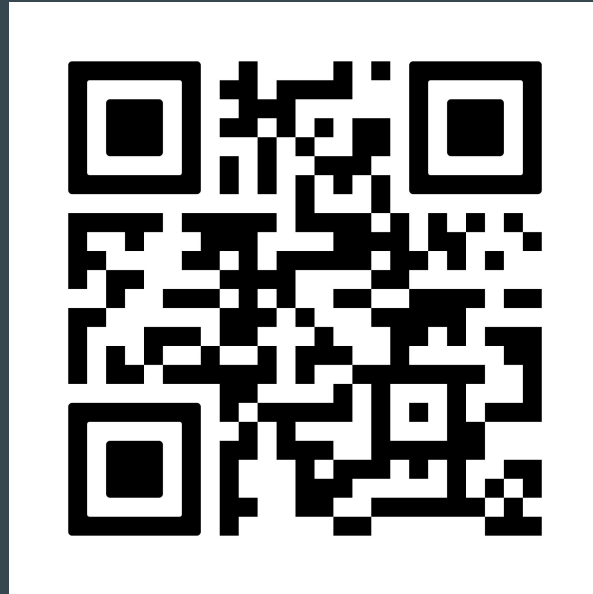
Images from the Very Large Array (VLA) and Australia Square Kilometre Array Pathfinder (ASKAP) interferometers:

- VLASS, RACS, NVSS Quick-look images: <https://cutouts.cirada.ca/>
- MeerKAT SAO Survey:
<https://archive-gw-1.kat.ac.za/public/repository/10.48479/3wfd-e270/index.html>

Owens Valley Radio Observatory: <https://www.ovro.caltech.edu/>

Questions, Comments, or Concerns?

<https://forms.gle/ywP1THADKCq1nDPy9>



Lecture 4: Large-Scale Structure and Cosmology

...

Learning Objectives and Overview

By the end of this course, students will be able to:

...identify major stars and constellations in the night sky, recount the life-cycle of a star from the Main Sequence to supernova, and distinguish between White Dwarfs, Neutron Stars, and Black Holes.

...describe the basic components of an optical telescope, explain the major differences between optical, infrared, and UV astronomy, describe why X-ray and gamma ray telescopes operate differently from OIR and UV telescopes.

...describe the basic components of a radio antenna, explain how radio interferometers work, and list the astrophysical sources of radio waves.

...describe the components of a galaxy (disk, bulge, ISM, halo, CGM), define cosmology, how it is studied (redshift, CMB, 21 cm cosmology, simulations, FRBs), explain how distance, redshift, and time are related within general relativity, and understand how the presence of dark matter and dark energy affect our picture of the Universe.

...list some of the major questions in astronomy today and refer to resources to continue exploring astronomy within and around Pasadena.

Galaxy Morphology

A **Galaxy** is a gravitationally-bound collection of stars, gas, and dust, like our galaxy, the **Milky Way**

Globular Clusters

Dwarf Galaxies



dSph

dE

Hubble's Galaxy Classification Scheme

Ellipticals

"Normal"

*Irregulars
(e.g. Magellanic Clouds)*

Lenticulars

Spirals

"Barred"

E0

E3

E6

S0

Sa

Sb

Sc

Irr

SB0

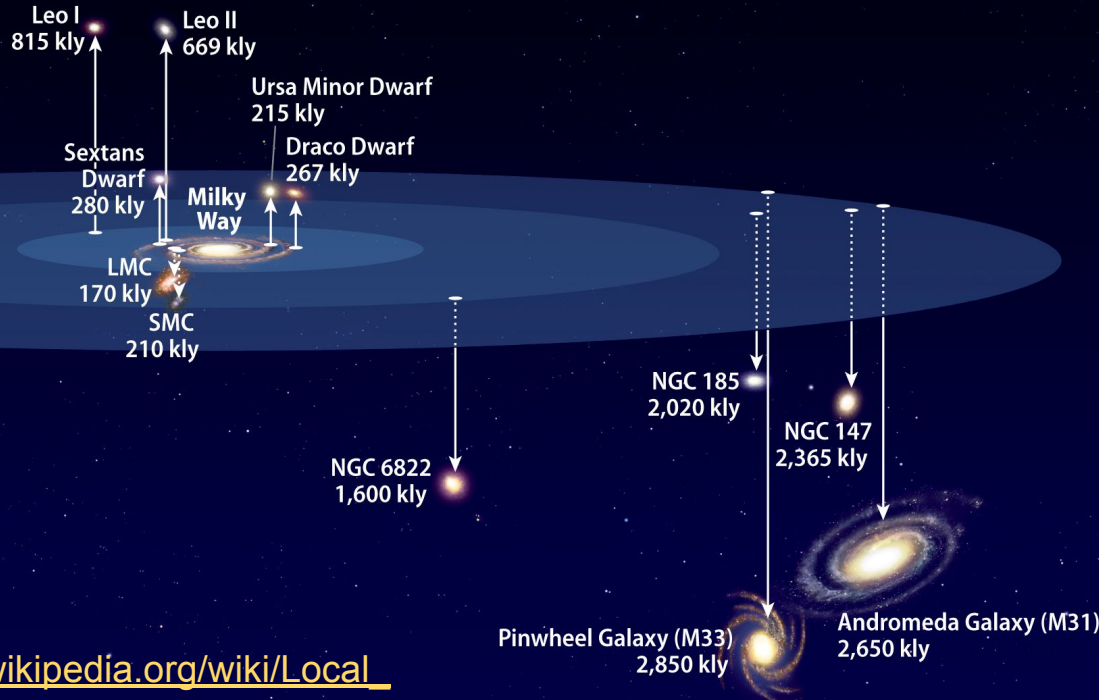
SBa

SBb

SBc

The Local Group

Local Group Galaxies and Classifications (McConnachie 2012)

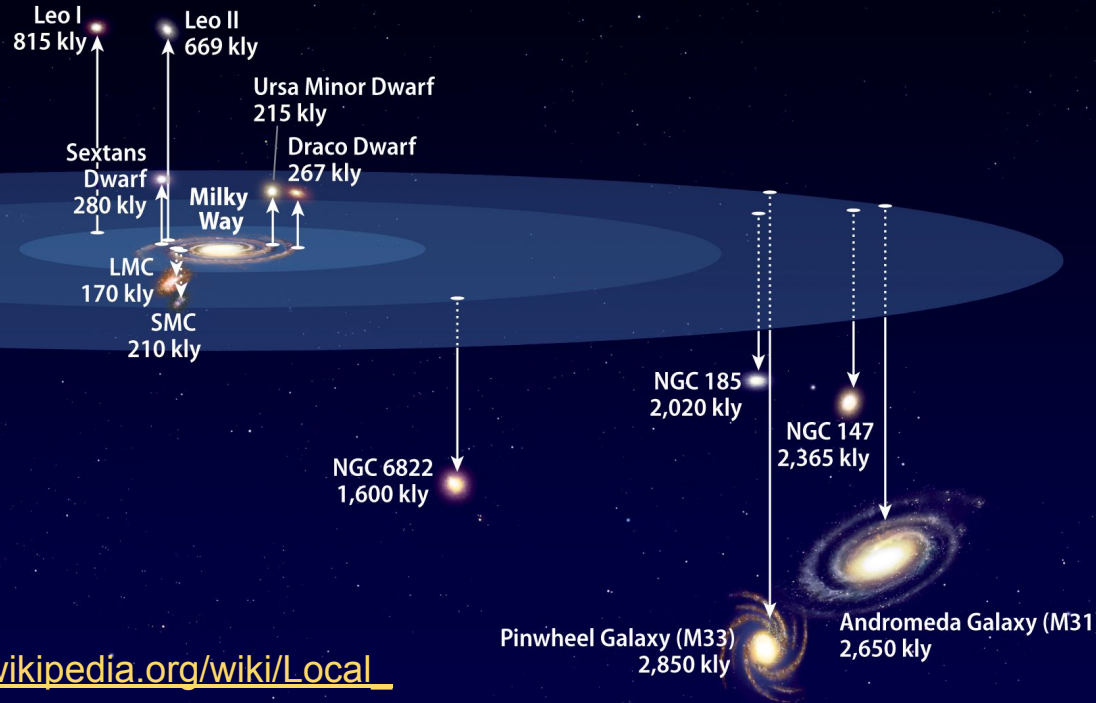


(1) Galaxy	(2) Other Names	(3)	(4)
The Galaxy	The MW	G	S(B)bc
Canis Major		G	????
Sagittarius dSph		G	dSph
Segue (I)		G	dSph
Ursa Major II		G	dSph
Bootes II		G	dSph
Segue II		G	dSph
Willman 1	SDSS J1049+5103	G	dSph
Coma Berenices		G	dSph?
Bootes III		G	dSph?
LMC	Nubecula Major	G	Irr
SMC	Nubecula Minor NGC 292	G	dIrr
Bootes (I)		G	dSph
Draco	UGC 10822 DDO 208	G	dSph
Ursa Minor	UGC 9749 DDO 199	G	dSph
Sculptor		G	dSph
Sextans (I)		G	dSph
Ursa Major (I)		G	dSph
Carina		G	dSph
Hercules		G	dSph
Fornax		G	dSph
Leo IV		G	dSph
Canes Venatici II	SDSS J1257+3419	G	dSph
Leo V		G	dSph
Pisces II		G	dSph
Canes Venatici (I)		G	dSph
Leo II	Leo B UGC 6253 DDO 93	G	dSph
Leo I	UGC 5470 DDO 74 Regulus Dwarf	G/L	dSph
Andromeda	M31 NGC 224 UGC 454	A	Sb
M32	NGC 221 UGC 452	A	cE
Andromeda IX		A	dSph

https://en.wikipedia.org/wiki/Local_Group

The Local Group

Local Group Galaxies and Classifications (McConnachie 2012)

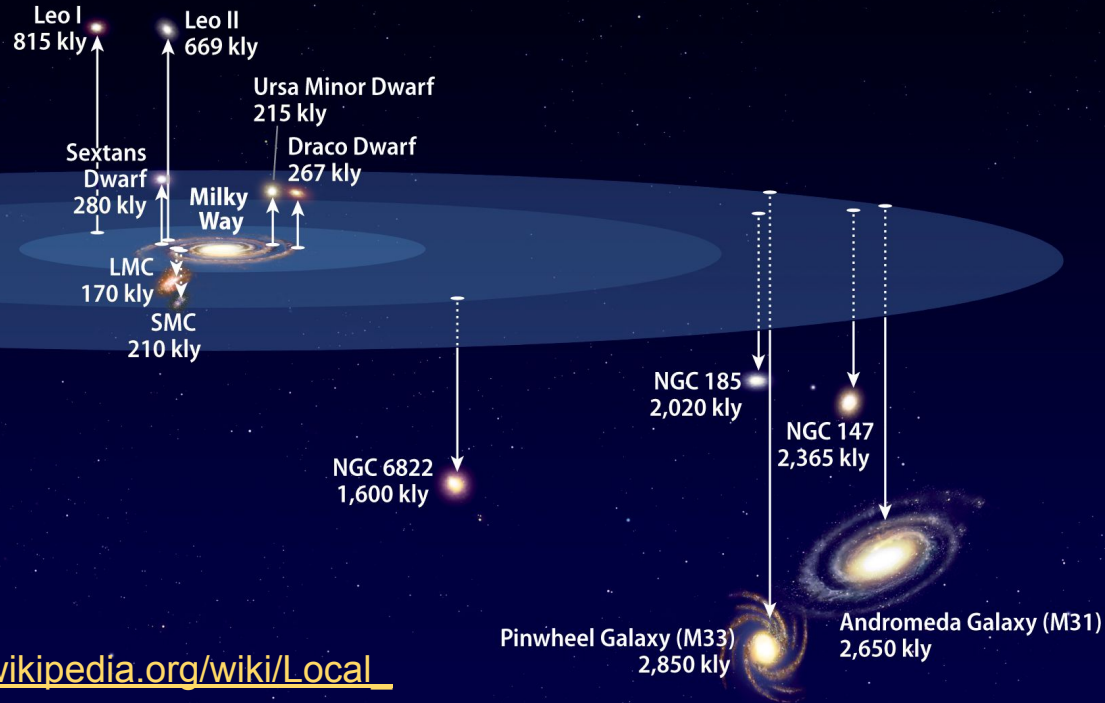


(1) Galaxy	(2) Other Names	(3)	(4)
NGC 205	M110 UGC 426	A	dE/dSph
Andromeda XVII		A	dSph
Andromeda I		A	dSph
Andromeda XXVII		A	dSph
Andromeda III		A	dSph
Andromeda XXV		A	dSph
Andromeda XXVI		A	dSph
Andromeda XI		A	dSph
Andromeda V		A	dSph
Andromeda X		A	dSph
Andromeda XXIII		A	dSph
Andromeda XX		A	dSph
Andromeda XII		A/L	dSph
NGC 147	UGC 326 DDO 3	A	dE/dSph
Andromeda XXI		A	dSph
Andromeda XIV		A/L	dSph
Andromeda XV		A	dSph
Andromeda XIII		A	dSph
Andromeda II		A	dSph
NGC 185	UGC 396	A	dE/dSph
Andromeda XXIX		A	dSph
Andromeda XIX		A	dSph
Triangulum	M33 NGC 598 UGC 1117	A	Sc
Andromeda XXIV		A	dSph
Andromeda VII	Casseopia dSph	A	dSph
Andromeda XXII		A	dSph
IC 10	UGC 192	A	dIrr
LGS 3 (Local Group Suspect 3)	Pisces (I)	A	dIrr/dSph
Andromeda VI	Pegasus dSph	A	dSph
Andromeda XVI		A/L	dSph
The rest of the Local Group			
Andromeda XXVIII		A/L	dSph?
IC 1613	DDO 8 UGC 668	L	dIrr
Phoenix		L/G	dIrr/dSph
NGC 6822	IC 4895 DDO 209 Barnard's Galaxy	L/G	dIrr

https://en.wikipedia.org/wiki/Local_Group

The Local Group

Local Group Galaxies and Classifications (McConnachie 2012)

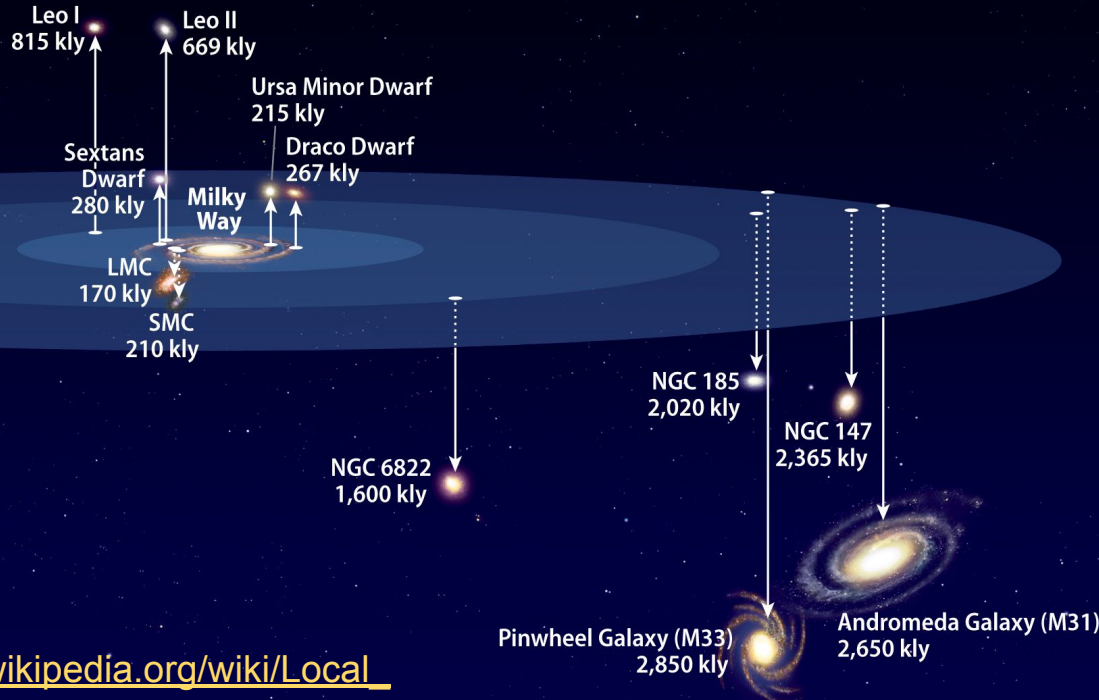


(1) Galaxy	(2) Other Names	(3)	(4)
Cetus		L	dSph
Pegasus dIrr	UGC 12613 DDO 216	L/A	dIrr/dSph
Leo T		L/G	dIrr/dSph
WLM (Wolf-Lundmark- -Melotte)	UGCA 444 DDO 221	L	dIrr
Leo A	Leo III UGC 5364 DDO 69	L	dIrr
Andromeda XVIII		L	dSph
Aquarius	DDO 210	L	dIrr/dSph
Tucana		L	dSph
Sagittarius dIrr	UKS 1927-177	L	dIrr
UGC 4879	VV 124	L	dIrr/dSph
NGC 3109	DDO 236 UGC 194 UGC 5373 DDO 70	N	dIrr
Sextans B		N	dIrr
Antlia		N	dIrr
Sextans A	UGC 205 DDO 75	N	dIrr
HIZSS 3(A)		N	(d)Irr?
HIZSS 3B		N	(d)Irr?
KKR 25		N	dIrr/dSph
ESO 410- G 005	UKS 0013-324	N	dIrr/dSph
NGC 55		N	Irr
ESO 294- G 010		N	dIrr/dSph
NGC 300		N	Sc
IC 5152		N	dIrr
KKH 98		N	dIrr
UKS 2323-326	UGCA 438	N	dIrr
KKR 3	KK 230	N	dIrr
GR 8	UGC 8091 VV 558 DDO 155	N	dIrr
UGC 9128	DDO 187	N	dIrr
UGC 8508		N	dIrr
IC 3104	ESO 020- G 004 UKS 1215-794	N	dIrr
DDO 125	UGC 7577	N	dIrr
UGCA 86		N	dIrr
DDO 99	UGC 6817	N	dIrr
IC 4662	ESO 102- G 014	N	dIrr

https://en.wikipedia.org/wiki/Local_Group

The Local Group

Local Group Galaxies and Classifications (McConnachie 2012)



(1) Galaxy	(2) Other Names	(3)	(4)
DDO 190	UGC 9240	N	dIrr
KKH 86		N	dIrr
NGC 4163	UGC 7199 NGC 4167 ^k	N	dIrr
DDO 113	UGCA 276 KDG 90	N	dIrr

Galaxy Luminosity Function

Luminosity Function - number of galaxies with luminosity between $L \rightarrow L+dL$ (distribution)

Schechter Function - originally proposed to be a universal Galaxy Luminosity Function, but now we see it varies with:

- Morphology
- Galaxy density (void, cluster, supercluster)

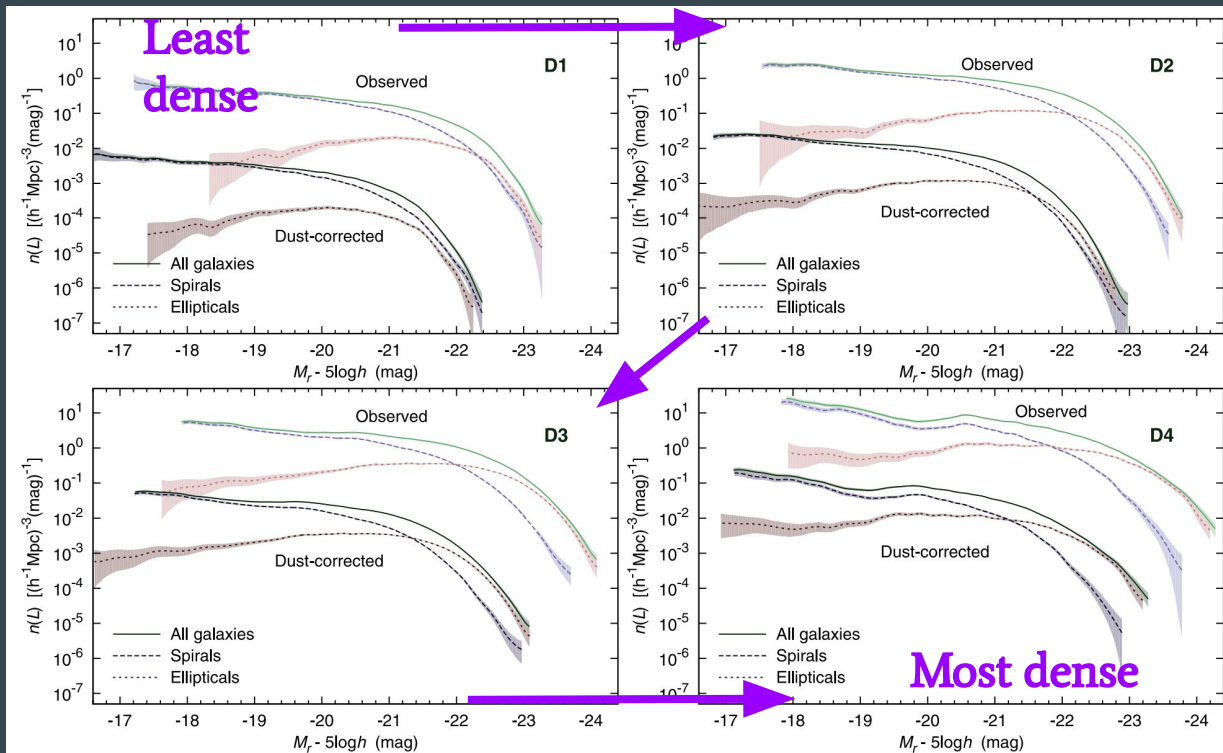
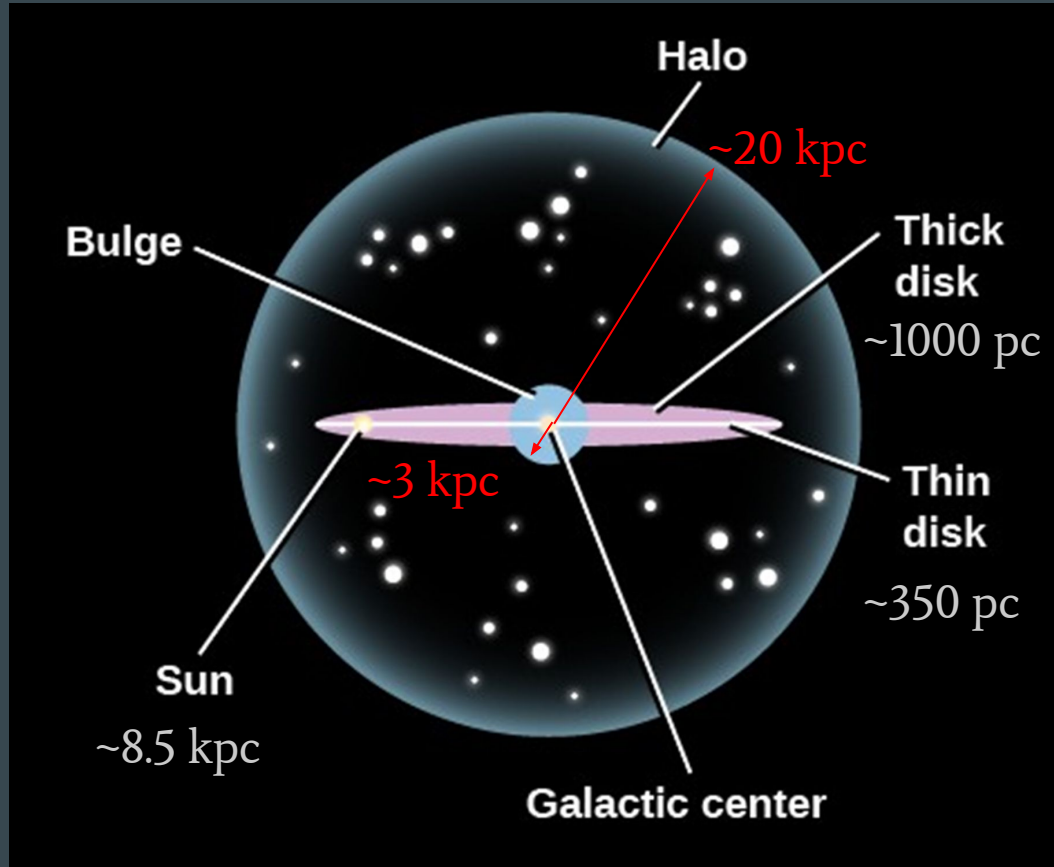


Fig. 13. LFs for different types of galaxies in different environments: *upper left* panel shows the least dense environment (D1) and *bottom right* panel shows the most dense environment (D4). Green solid lines show the LFs for all galaxies; blue dashed lines show the LFs for spiral galaxies; red dotted lines show the LFs for elliptical galaxies. The *upper* LFs in each panel are the observed LFs that are shifted up two units in logarithmic scale and right by one mag. The *lower* LFs in each panel are the attenuation-corrected LFs. Filled areas show the 95% confidence regions. The panels D1 to D4 show different global environmental regions: D1 are void regions and D4 are supercluster regions. The LFs have been normalised to the volume of each sample.

Luminosity functions from Sloan Digital Sky Survey Data
Release 7 (Tempel et al., 2011)

Milky Way Structure



Milky Way Star Formation and Stellar Populations

Population I Stars

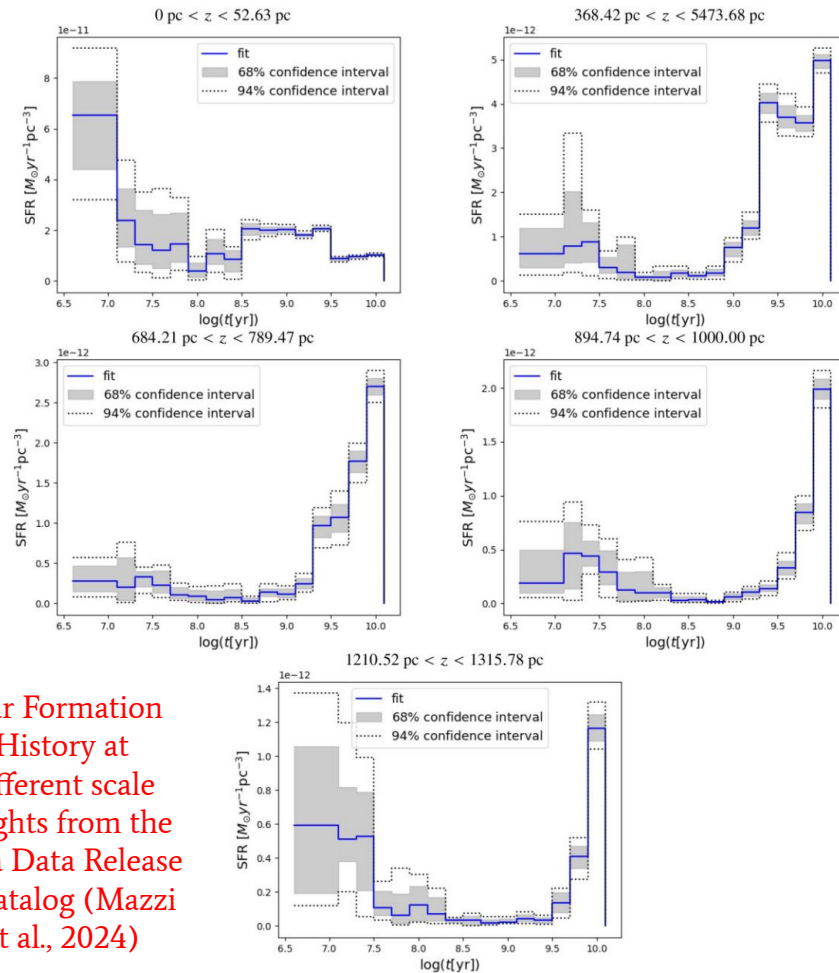
- Metal rich, formed after the explosions of the first stars
- Most in **thin disk**, high fraction of heavy metals (Fe, Si, Ti) → Type Ia SNe, younger
- Some in **bulge**, mostly oxygen, carbon → Type II SNe, older

Population II Stars

- Metal poor, formed from earliest gas in the Galaxy
- Bulge and halo

Population III (?) – theorized to form from primordial gas before galaxies formed

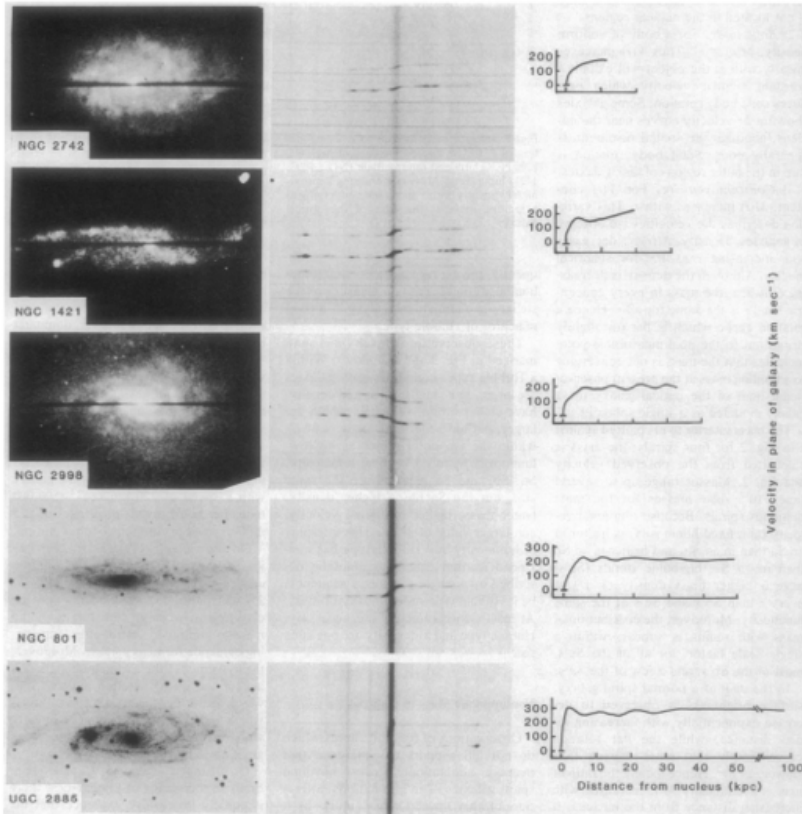
Star Formation History – star formation rate as a function of Galaxy age; remains complex, population model insufficient



Star Formation History at different scale heights from the Gaia Data Release 2 Catalog (Mazzi et al., 2024)

Figure 6. The SFR per unit volume as a function of age determined for the same slices of the sample shown in Fig. 4, also indicated on top of each panel. The blue lines represent the best fitting SFR values, while the grey-shaded areas and the dashed lines mark the 68 and 94 per cent confidence intervals, respectively. We note that the SFR at young ages ($\log(t/\text{yr}) \lesssim 7.5$) is non-zero even at large z , although it is very uncertain.

Missing Matter?



Mounting evidence for large amount of ‘non-luminous’ matter:

- 1933: Fritz Zwicky identified stellar mass of Coma cluster much lower than dynamical mass based on galaxy velocities
- 1940: Jan Oort studies of NGC 3115 dynamics imply mass distribution different than light distribution
- 1945: Martin Schwarzschild finds inconsistent rotation curve of M31
- **1962: Vera Rubin measures flat Milky Way rotation curve from 888 stars, first confirmation of a “Dark Matter Halo”**

Images, spectra, and rotation curves for a sample of galaxies showing flat rotation curves (Rubin et al. 1962, 1983)

Think-Pair-Share

How do you think galaxies formed?

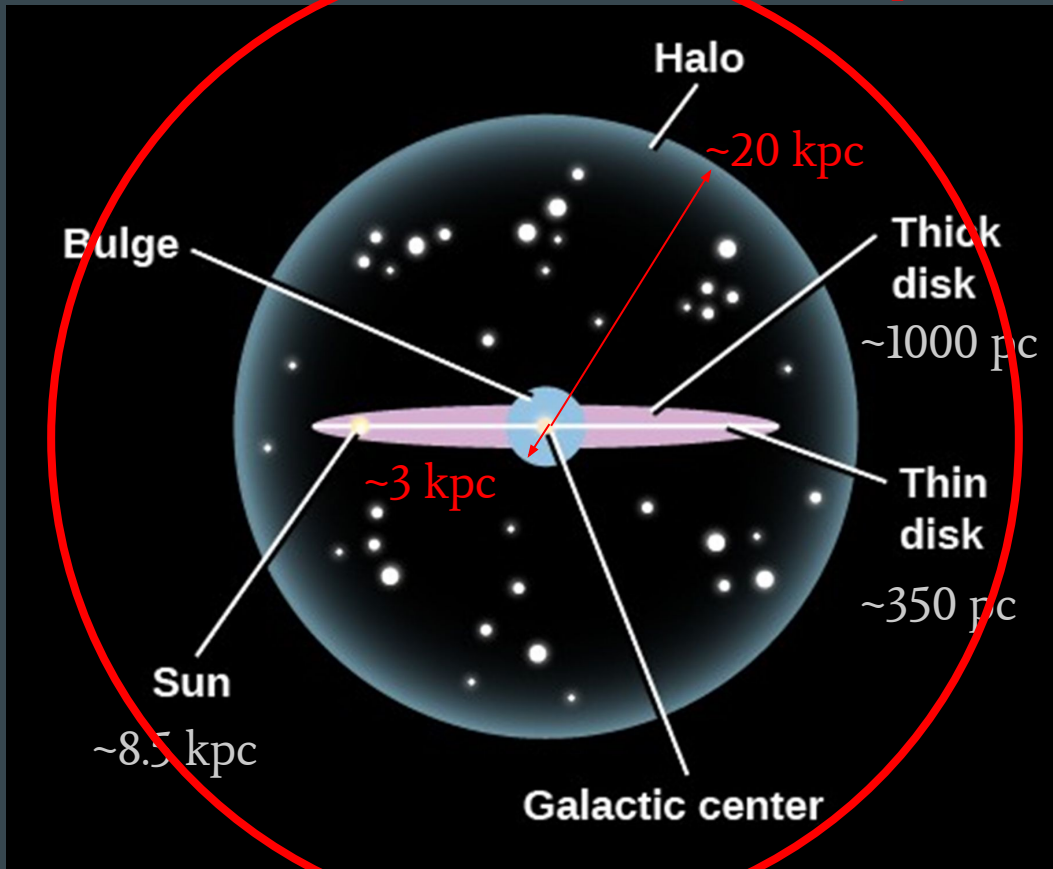
What role do you think dark matter plays in galaxy formation?

Milky Way Structure

Hierarchical (bottom-up) galaxy formation:

[1] Dark matter perturbations ($10^{12}M_{\text{sun}}$) define where galaxies will form → **cosmic web**

[2] Within DM perturbations, first small clusters (10^6M_{sun}) collapse, begin forming stars and globular clusters → **bulge**



Dark Matter Halo
~100 kpc

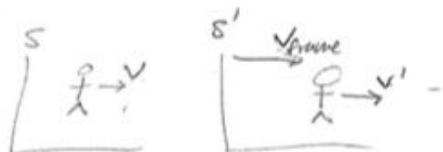
[3] Collisions between small clusters disrupt star formation, collide into larger ($10^{10}M_{\text{sun}}$) proto-galaxies → **stellar halo**

[4] Residual torque from collisions and gravitational interactions induce angular momentum, causes matter to settle into disk → **thick disk**

[5] Cool gas settles into smaller scale height → **thin disk**

4.1) Special Relativity

Newtonian relativity →



$$v' = v - v_{\text{frame}}$$

↳ but what happens if $v = c$, the speed of light?

↳ Newtonian physics breaks down when $v \rightarrow c$

Einstein's Postulates

① Principle of Relativity - laws of physics apply in all inertial reference frames

② Speed of Light in a vacuum is $c = 3 \times 10^8$ m/s in all inertial reference frames



frames: if you're on the train, how long for light to reach the ground?

$$\Delta t = 2d/c$$

Lorentz Factor:

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

frame S': if you observe at rest, how long for light to reach the ground?

$$d' = \sqrt{d^2 + (v\Delta t')^2}$$

$$\Delta t' = \frac{2d'}{c} = 2 \frac{\sqrt{d^2 + (v\Delta t')^2}}{c}$$

$$\frac{c^2 \Delta t'^2}{4} = d^2 + \frac{v^2}{4} \Delta t'^2$$

$$(c^2 - v^2) \Delta t'^2 = 4d^2$$

$$\Delta t' = \frac{2d}{\sqrt{c^2 - v^2}} = \frac{\Delta t}{\sqrt{1 - \frac{v^2}{c^2}}}$$

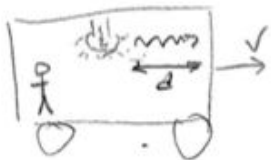
Time Dilation

$$\Delta t' = \gamma \Delta t$$

"moving clocks run slow"

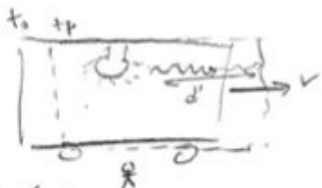
4.2

Ex.



Frame S: how long does it take for light to reach end of the train?

$$\Delta t = \frac{d}{c}$$



Frame S': how long does it take if we observe from the platform?

$$\Delta t' = \frac{d'}{c}$$

$\frac{d'}{\Delta t'} = \frac{d}{\Delta t}$ since c is the same in both frames

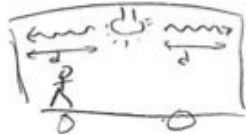
$$d' = d \left(\frac{\Delta t'}{\Delta t} \right) = \gamma d$$

Length contraction

$$d' = \gamma d$$

“Length of moving objects are shorter”

Ex.



Frame S: When does the light hit each side of the train?

$$t_1 = d/c \quad t_2 = d/c$$

$$t = t_1 = t_2 = d/c$$



Frame S': When does the light hit each side of the train?

$$t'_1 = \frac{d'}{c} = \frac{d' - vt'_1}{c}$$

$$t'_2 = \frac{d'}{c} = \frac{d' + vt'_2}{c}$$

$$t'_1 \left(1 + \frac{v}{c} \right) = \frac{\gamma d}{c}$$

$$t'_2 \left(1 - \frac{v}{c} \right) = \frac{\gamma d}{c}$$

$$t'_1 = \frac{\gamma d}{c \left(1 + \frac{v}{c} \right)}$$

$$t'_2 = \frac{\gamma d}{c \left(1 - \frac{v}{c} \right)}$$

$$\Rightarrow t'_1 = \frac{1 - \frac{v}{c}}{1 + \frac{v}{c}} t_2$$

Relativity of simultaneity

“events that are simultaneous in one frame are not simultaneous in another”

4.3

Lorentz transformations

- to convert from frame S to frame S'
moving at velocity v relative to S in X direction

$S \rightarrow S'$

$$\begin{aligned} ct' &= \gamma(ct - \beta x) \\ x' &= \gamma(x - \beta ct) \\ y' &= y \\ z' &= z \end{aligned}$$

$S' \rightarrow S$

$$\begin{aligned} ct &= \gamma(ct' + \beta x') \\ x &= \gamma(x' + \beta ct') \\ y &= y' \\ z &= z' \end{aligned}$$

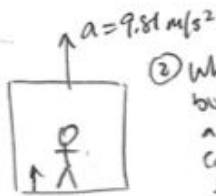
What if frame S' is accelerating?

- ① Inside box at no windows on the ground



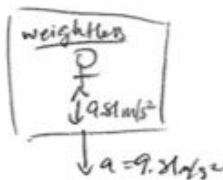
gravity and acceleration are equivalent

... (equivalence principle)



- ② What if the box is pulled at 9.81 m/s^2 ? Can you tell the difference?

- ③ What if the box is falling under gravity?



Momentum: measurement of an object's inertia ($p = mv$)

- relativistic \Rightarrow use proper velocity measured in rest frame:

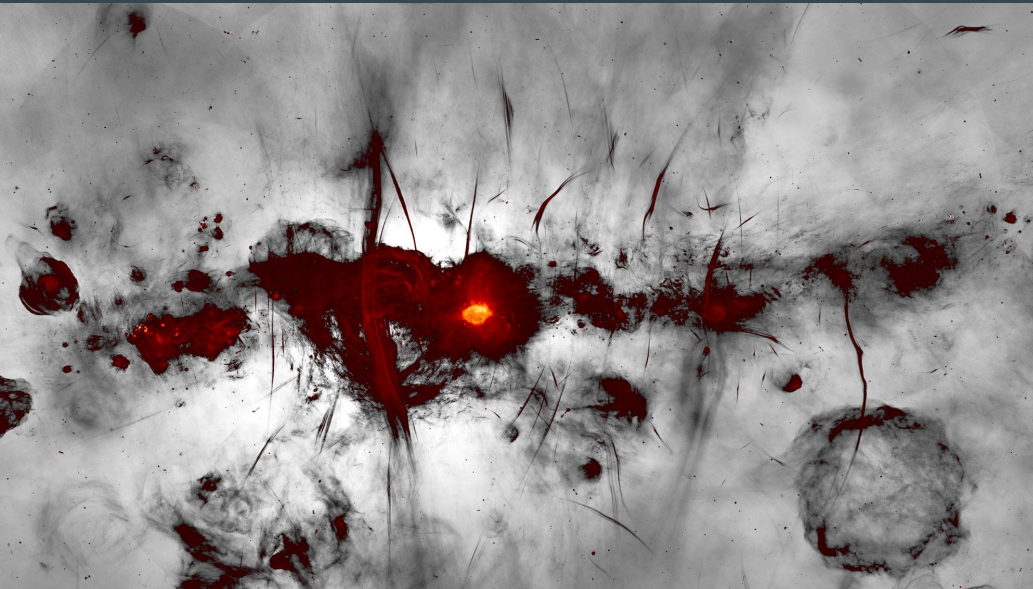
$$p = \gamma m v$$

$$\text{Energy} = \boxed{E = \gamma m c^2 = (pc)^2 + (mc^2)^2}$$

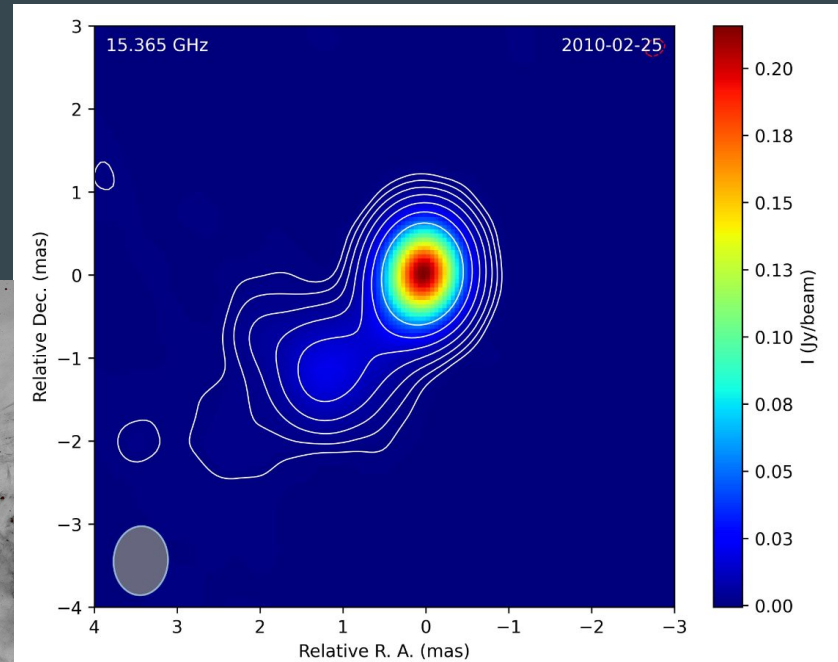
- rest energy: for $\gamma = 1$

$$\boxed{E_{\text{rest}} = mc^2}$$

Special Relativity in Astronomy



Synchrotron Radiation (MeerKAT
1.3 GHz; Heywood+2024)



Superluminal Motion
(Blazar J1429+5406;
Koller & Frey 2025)

Think-Pair-Share

Let's do a thought experiment: say there are two twins who start on earth. If one twin starts travelling very fast, he experiences time passing more slowly than the one on earth. After a long time, he turns around and comes back at the same speed. When he arrives, will he be older, younger, or the same age as his twin?

Why?

The Twin Paradox

It's not really a paradox!

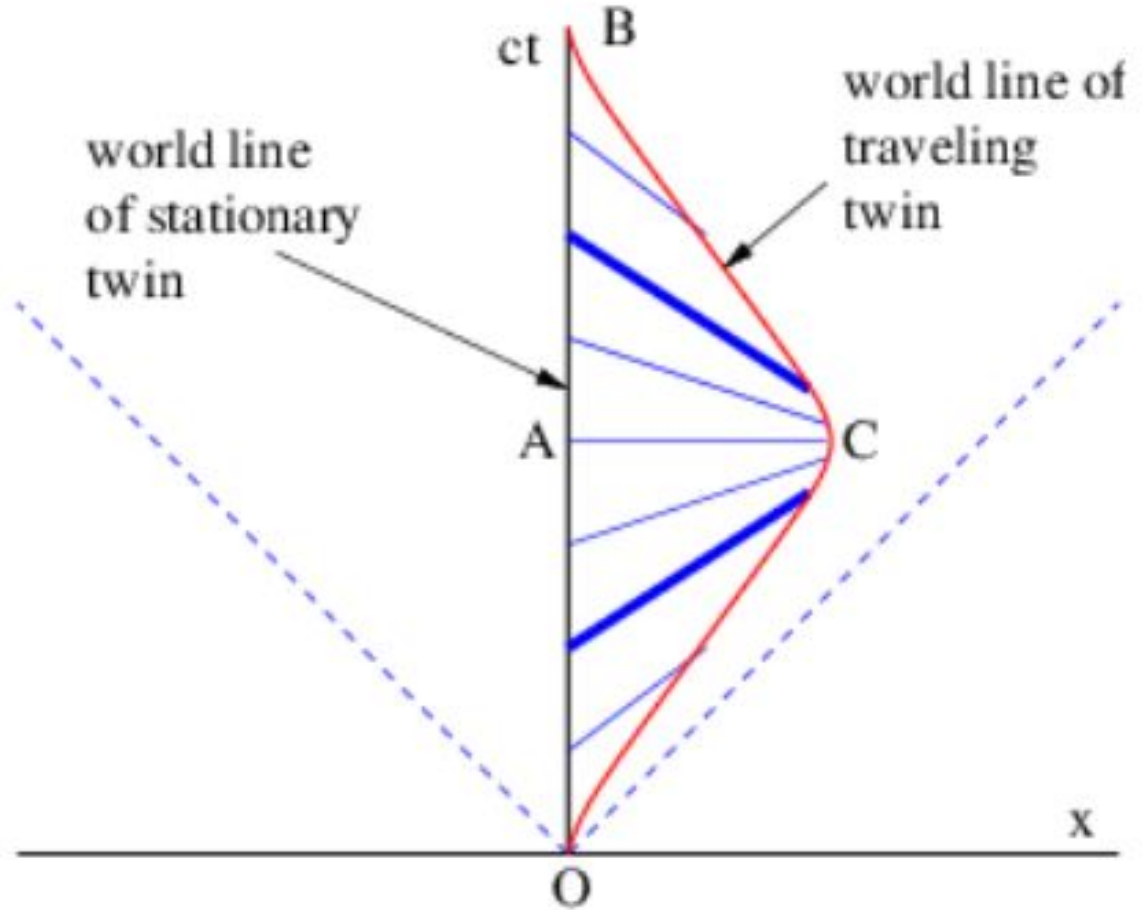
While the twin is traveling, his clock runs **slower** than the stationary twin → traveling twin is younger

But to the traveling twin, the stationary twin is moving → stationary twin is younger

How can both be true?

When the moving twin turns around, they're **accelerating**, so their reference frame changes → the stationary twin is correct!

<https://www.sciencealert.com/in-space-scott-kelly-aged-more-slowly-than-his-brother-on-earth-and-here-s-why>

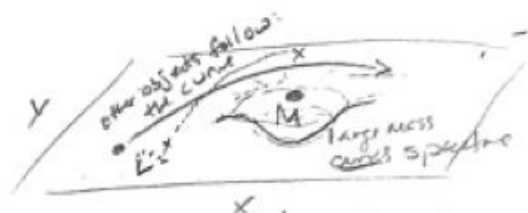
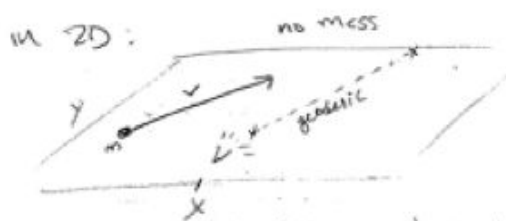


4.4

General Relativity - geometric description of spacetime including gravity

- spacetime: x, y, z, ct

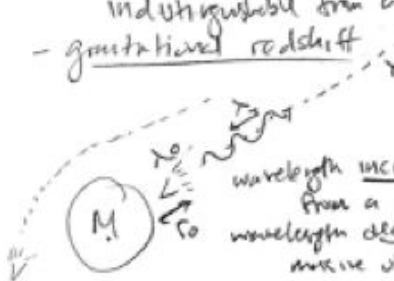
- ① Mass tells spacetime how to curve,
Spacetime tells mass how to move



- geodesic - shortest path between 2 points within a given geometry
- light always follows geodesic, which is curved in curved spacetime

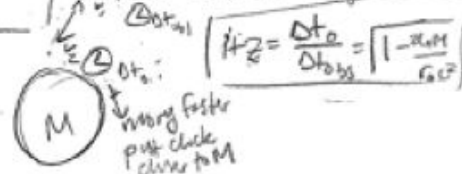
- ② Equivalence Principle - gravitational & inertial mass are the same, i.e. gravity is indistinguishable from acceleration

- gravitational redshift



$$1+z = \frac{\lambda_{obs}}{\lambda_0} = \frac{\gamma_0}{\gamma_{obs}} = \sqrt{\frac{1-\frac{2GM}{rc^2}}{1-\frac{2GM}{r_0c^2}}}$$

- gravitational time dilation
time runs more slowly near massive objects



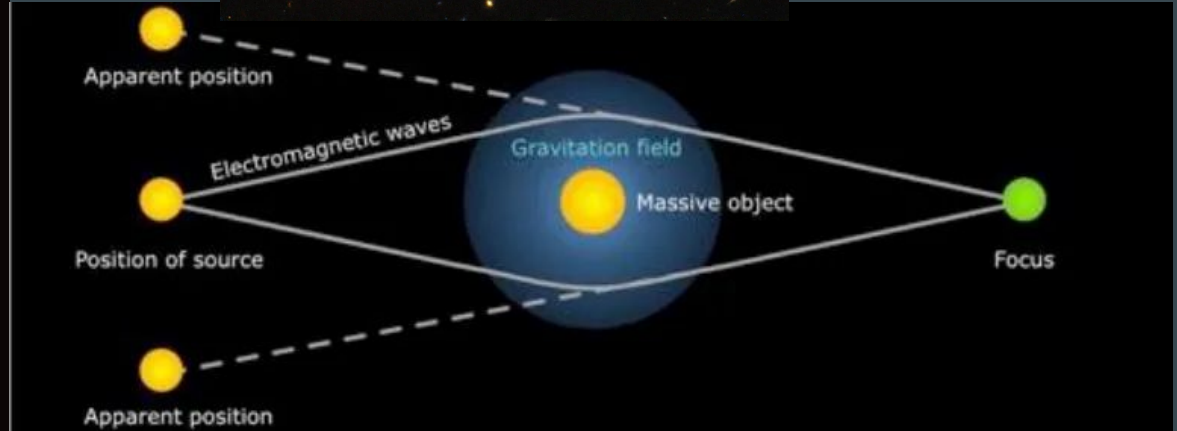
$$1+z = \frac{\Delta t_0}{\Delta t_{obs}} = \sqrt{\frac{1-\frac{2GM}{rc^2}}{1-\frac{2GM}{r_0c^2}}}$$

General Relativity in Astronomy

1.3 mm Image of the Black Hole M87 in the Andromeda Galaxy (EHT Collab. 2017)

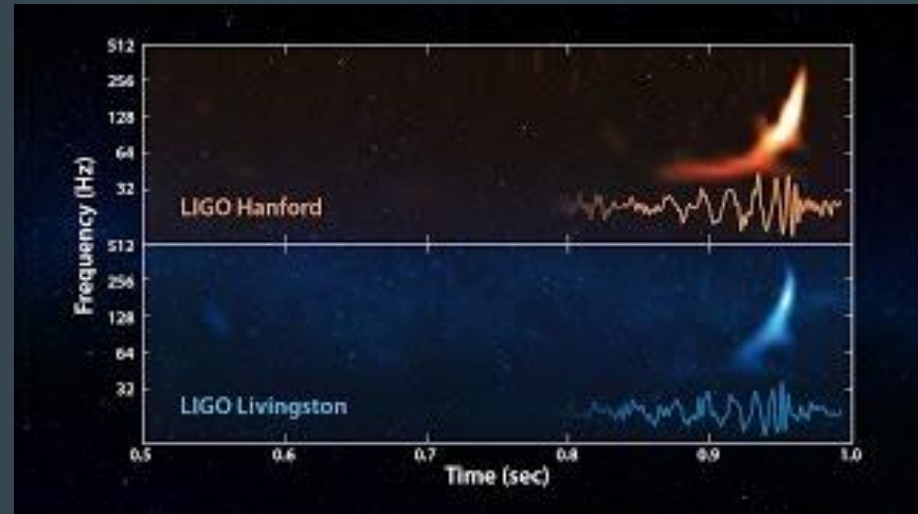
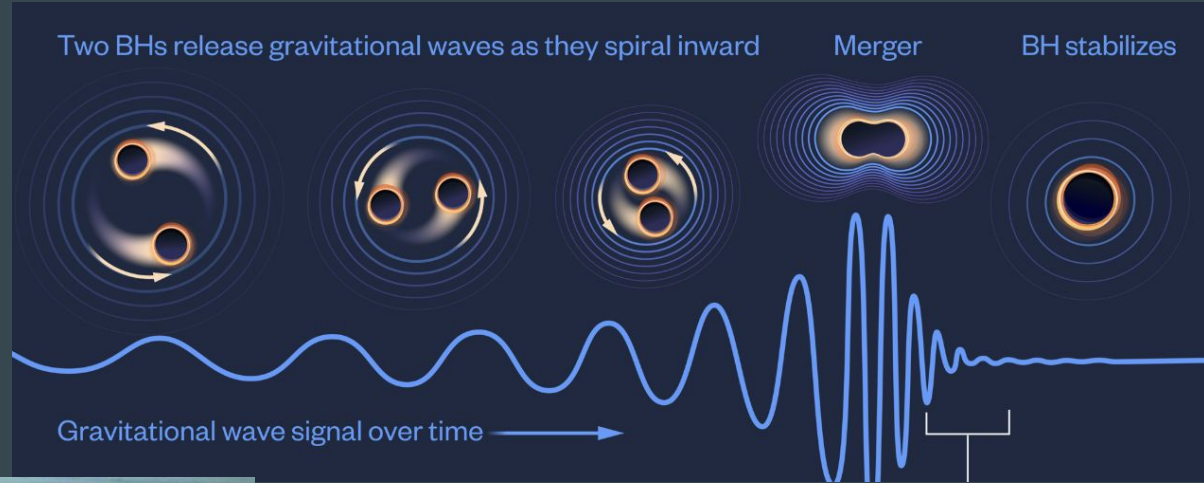


Gravitational Lensing
Observed by the
Hubble Telescope



Gravitational Waves

Laser Interferometer
Gravitational-Wave
Observatory (LIGO)



At-Home Astronomy: Gravitational Lensing and Gravitational Waves

Hubble Gravitational Lensing Image Archives:

<https://esahubble.org/images/archive/category/cosmology/>

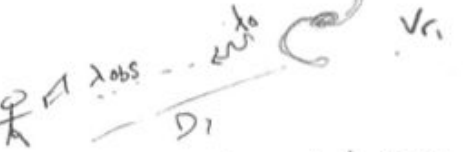
Gravitational Waves:

- Open Source Catalog and Tutorials on Accessing LIGO/VIRGO/KAGRA data:
<https://gwosc.org/tutorials/>
- Gravitational Wave alerts on your phone:
<https://www.ligo.caltech.edu/page/GWPhoneAlerts>

4.5



Edwin Hubble



↳ observed all spectral lines redshifted \Rightarrow galaxies all moving away from us

↳ more distant galaxies moving away faster: $D_3 > D_2 > D_1$
 $v_3 > v_2 > v_1$

Hubble's law
 Cosmological redshift: $v_r \approx cz \approx \frac{H_0}{c} D$

← Hubble's constant
 $H_0 \sim 70 \text{ km/s/Mpc}$

- isotropic - universe has no preferred center or direction
 \Rightarrow galaxies are all moving away from each other

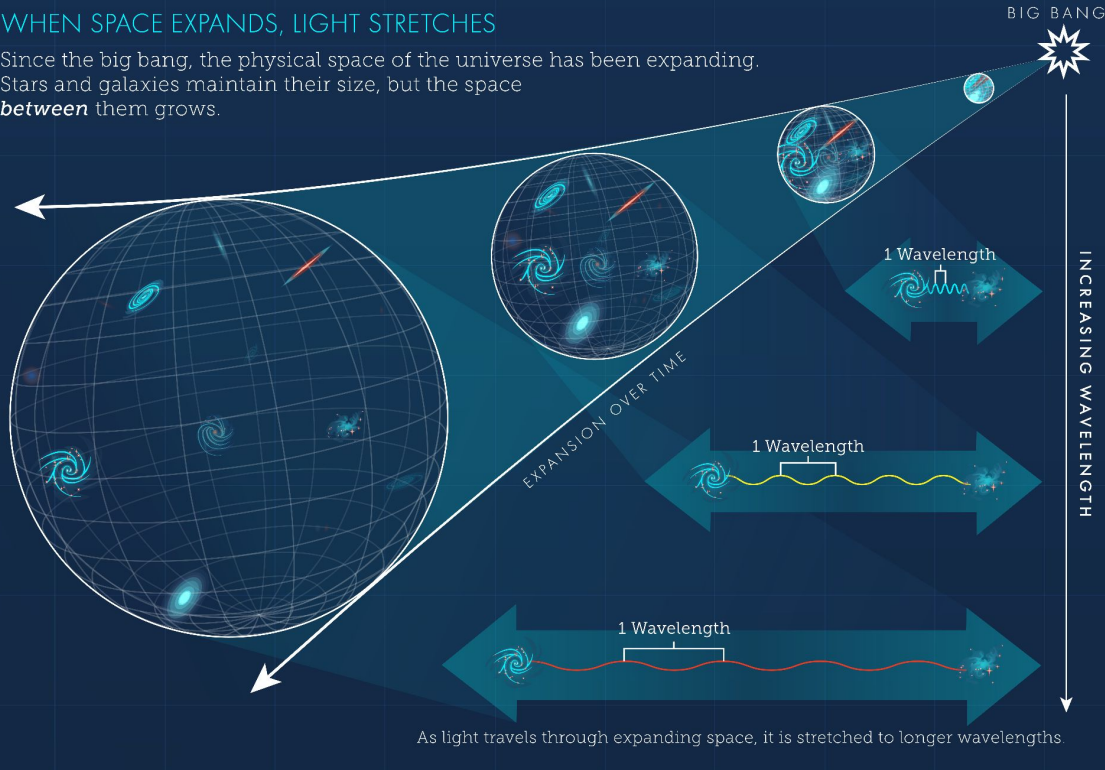


- expansion is accelerating \rightarrow driven by dark energy

The Expanding Universe

WHEN SPACE EXPANDS, LIGHT STRETCHES

Since the big bang, the physical space of the universe has been expanding. Stars and galaxies maintain their size, but the space *between* them grows.

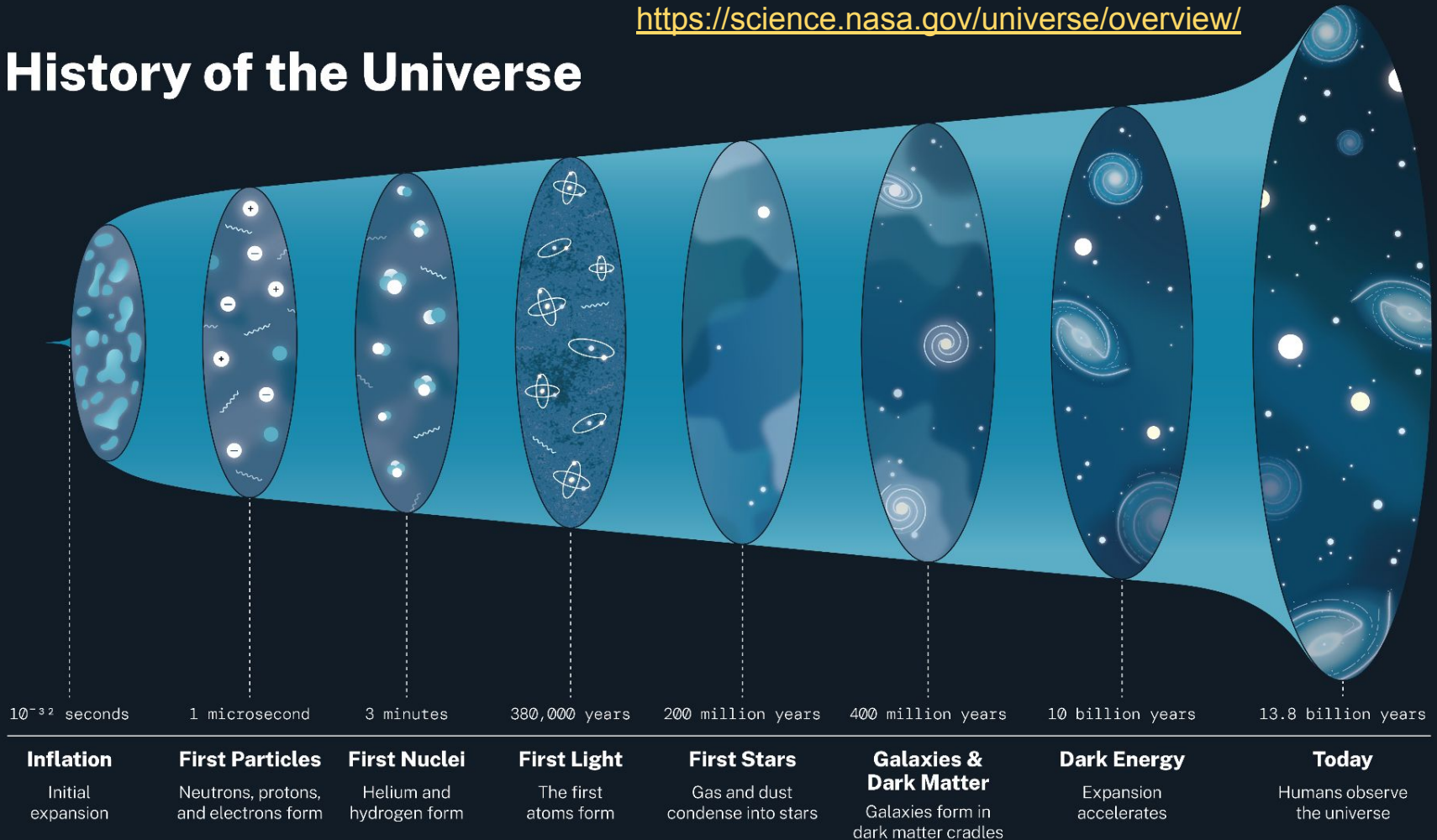


<https://science.nasa.gov/mission/hubble/science/science-behind-the-discoveries/hubble-cosmological-redshift/>

Think-Pair-Share

If the Universe is expanding, why don't we see evidence of it on Earth?

History of the Universe



Questions, Comments, or Concerns?

<https://forms.gle/ywP1THADKcQ1nDPy9>

